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Investigation of the Magnetic and Magneto-dielectric  
Properties of few Complex Spinel

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A Thesis Submitted to  
Indian Institute of Technology Guwahati  
for the degree of

**Doctor of Philosophy**

By

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***Dedicated to my father Late Mr. Swapan Kumar Nayak,  
Mother Smt. Iva Nayak, my Elder Brother and Bhabi***





**INDIAN INSTITUTE OF TECHNOLOGY GUWAHATI**

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### **Declaration**

*“Investigation of the magnetic and magneto-dielectric properties of few complex spinels”* is the result of my own doctoral research work. This work was carried out under the supervision of Dr. Subhash Thota at the Department of Physics, Indian Institute of Technology Guwahati. To the best of my knowledge, the work presented in this thesis has not been submitted to any other Institute/University for the award of any degree.

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### Certificate

It is certified that the work described in this thesis, entitled “*Investigation of the magnetic and magneto-dielectric properties of few complex spinels*”, done by Mr. Sanjib Nayak, a Ph.D. student of Department of Physics, Indian Institute of Technology Guwahati, for the award of degree of Doctor of Philosophy has been carried out under my supervision. This work has not been submitted elsewhere for the award of any degree.

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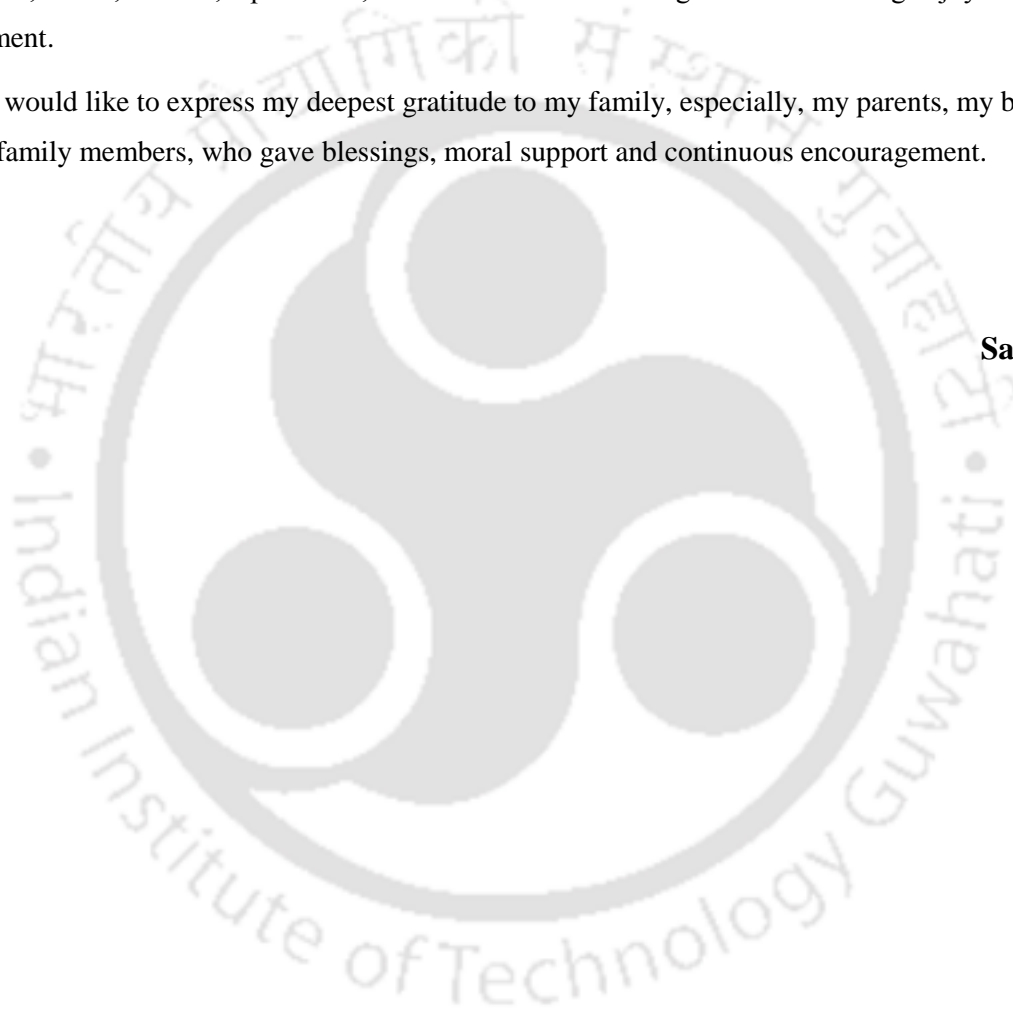
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by  
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## Synopsis Report

Spinel oxides ( $AB_2O_4$ ) and their composites have proven to be an abundant research field due to their fascinating magnetic, electronic, chemical and optical properties [1-6]. The atomic arrangement in spinel compounds is interpreted as a pseudo-close-packed arrangements of the oxygen anions with divalent cations occupying tetrahedral A-lattice sites (T( )) and trivalent cations residing at the octahedral B-sites (O[ ]) of the cubic unit-cell of space group  $Fd\bar{3}m$  [7, 8]. A spinel with the configuration  $(A^{2+}) [B_2^{3+}] O_4$  is termed as ‘normal-spinel’ while the other possible configuration  $(B^{3+}) [A^{2+}B^{3+}] O_4$  is called ‘inverse-spinel’. Magnetic-spinels are well-established systems because of their remarkable applications in microwave devices, isolators, circulators, super-capacitors and phase-shifters [3, 8, 9]. Ferrites ( $Fe_3O_4$ ) and Mn and Co-based spinels are widely investigated systems owing to the possibility of forming extremely large variety of solid solutions allowing a precise tailoring of their physical properties, which is a major advantage for microwave technology and other industrial applications [3, 9 - 16]. In the magnetic spinels alone, materials such as tricobalt tetroxide ( $Co_3O_4 =$  Cobalt (II, III) oxide), cobalt-orthostannate ( $Co_2SnO_4$ ), cobalt-orthotitanate ( $Co_2TiO_4$ ), and Hausmannite ( $Mn_3O_4$ ) exhibit rich phase diagrams involving charge, orbital, geometrical frustration, canted Yafet-Kittle type and spiral antiferro/ferromagnetic orderings. Besides such rich magnetic properties, the low-temperature reentrant spin-glass transitions and sign-reversal exchange bias phenomena often occur which are associated with the competing exchange interactions and strong coupling between charges, spin and lattice degrees of freedom. Moreover, the magnetic ground state of the doped spinels are very sensitive to the average radius ratio B/A of cations ( $\langle r_A \rangle$ ) and charge fluctuations on them.

The present research work was primarily motivated by the desire to understand the magnetic structure and other physical properties of few complex inverse spinels; (i)  $Co_2SnO_4$ , (ii)  $Co_2TiO_4$ , and a tetragonally distorted normal spinel  $Mn_3O_4$ . The layout of the thesis is as follows:

Chapter 1 provides an introduction to the spinels and their applications, crystal structure of spinels, and basic concepts of magnetism. Various magnetic phenomena are discussed both from an experimental and theoretical point of view in which the underlying physical principles are first presented with a follow up macroscopic and microscopic theories appropriately. This chapter also reviews the physics of spin-glasses and other disordered magnetic phases together with the Néel two-sublattice model of ferrimagnetism. This chapter concludes with the identification of few spinels that exhibits complex magnetic ordering and some critical issues of low-temperature disordered state which are addressed in the subsequent chapters.

Chapter 2 presents a detailed overview of various experimental techniques employed in this research work including the synthesis procedure based on standard solid-state reaction method and oxalate based low-temperature sol-gel processing. The structural characterization using X-ray diffraction technique (performed by Panalytical Xpert Pro diffractometer) followed by the Rietveld refinement method using Fullprof software was discussed briefly for the verification of the phase purity of the prepared samples. Details of elemental analysis

performed in the present work using the X-ray photoelectron spectroscopy (XPS) and X-ray energy dispersive analysis (EDAX) was described thereafter. Material characterization techniques like field emission scanning electron microscopy (FESEM) and transmission electron microscopy (TEM) were discussed because these instruments are used to study the microstructure/morphology and stoichiometry. A commercial superconducting quantum interference device (SQUID) based magnetometer, which was used to measure the dc-magnetization and ac-susceptibility was introduced in the subsequent section. Basic principle of temperature dependent specific-heat ( $C_P(T)$ ) measurement procedure performed by means of a physical property measurement system (PPMS) was described. This chapter also describes the details of dielectric measurements carried out at various frequencies (10 Hz - 32 MHz) using a Novocontrol Alpha AN impedance analyzer over a wide temperature interval ( $80 \text{ K} \leq T \leq 600 \text{ K}$ ). Finally, some spectroscopic characterization techniques like Fourier transformed infrared (FTIR) spectroscopy, electron-spin resonance (ESR) and micro-Raman are illustrated.

Chapter 3 presents synthesis of cobalt-orthostannate ( $\text{Co}_2\text{SnO}_4$ ) polycrystals at different sintering temperatures and provides its structural characterization, elemental analysis using XPS, morphological and magnetization studies. A systematic comparison of the magnetic properties of  $\text{Co}_2\text{SnO}_4$  samples sintered at two different temperatures,  $1200^\circ\text{C}$  (S1200) and  $1350^\circ\text{C}$  (S1350) was reported. The role of few percent of unreacted non-magnetic  $\text{SnO}_2$  clusters on the global magnetic behavior of  $\text{Co}_2\text{SnO}_4$  samples was discussed in terms of both ac-magnetic susceptibility ( $\chi'$  and  $\chi''$ ) and dc-magnetization ( $M$ ) studies. The elemental analysis by XPS reveals the presence of divalent and tetravalent states of cobalt and tin, respectively in S1350 which confirmed the structure:  $(\text{Co}^{2+})[\text{Sn}^{4+}\text{Co}^{2+}]\text{O}_4$ . From the results of temperature dependence of  $\chi_{\text{dc}}$  and  $\chi_{\text{ac}}$  two magnetic transitions was evident: the first one is ferrimagnetic ordering with Néel temperature  $T_N \sim 41 \text{ K}$  with a follow-up freezing of the spins at  $39 \text{ K}$ . Such co-existence of longitudinal ferrimagnetic order below  $T_N = 41 \text{ K}$  and transverse spin-glass state below  $T_{\text{SG}}$  is suggested to result from the presence of non-magnetic  $\text{Sn}^{4+}$  ions on the octahedral 'B' sites. The ferrimagnetic ordering is suggested to result from different magnetic moments of  $\text{Co}^{2+}$  on the A- sites ( $3.87 \mu_B$ ) and B-sites ( $4.91 \mu_B$ ) with antiferromagnetic molecular field constants  $N_{\text{AA}} = 21.56$ ,  $N_{\text{BB}} = 10.68$  and  $N_{\text{AB}} = 33.20$  (S1350). This chapter also deals with the origin of low-temperature exchange bias and temperature dependent vibration excitations in  $\text{Co}_2\text{SnO}_4$  inverse spinel.

Chapter 4 deals with the complex magnetic ordering of cobalt-orthotitanate ( $\text{Co}_2\text{TiO}_4$ ) inverse spinel. Initial part of this chapter contains the literature review, synthesis procedure and crystal structure analysis. The electronic structure obtained from XPS analysis reveals the presence of  $\text{Ti}^{3+}$  instead of  $\text{Ti}^{4+}$  in the B-sites ( $(\text{Co}^{2+})_A[\text{Ti}^{3+}\text{Co}^{3+}]_B\text{O}_4$ ), which significantly contribute to the overall magnetic moment. The  $\chi_{\text{dc}}$  versus  $T$  data shows the existence of ferrimagnetic long-range ordering with  $T_N \sim 47.4 \text{ K}$ , and a crossover in sign for  $\chi(\text{ZFC})$  and  $\chi(\text{FC})$  at a compensation temperature  $\sim 32 \text{ K}$  ( $T_{\text{COMP}}$ ), where the magnetization of the two sublattice ( $M_A$  and  $M_B$ ) balance each other. The weak anomalies noticed in specific heat versus temperature data at  $47.4 \text{ K}$  ( $T_N$ ) and  $31.7 \text{ K}$  ( $T_{\text{COMP}}$ ) supports the existence of ordering temperatures in the system estimated from the magnetization measurements. From the analysis of temperature dependence of inverse dc paramagnetic susceptibility, the magnetic moments

$\mu(A) = 3.87 \mu_B$  and  $\mu(B) = 5.19 \mu_B$  on the A and B sites are determined with  $\mu(B)$  in turn yielding  $\mu(Ti^{3+}) = 1.73 \mu_B$  and  $\mu(Co^{3+}) = 4.89 \mu_B$ . This chapter also discusses the frequency ( $f$ ) dispersion of the cusp observed in  $\chi_{ac}$  versus  $T$  which was analyzed using two scaling laws: (i) the Vogel-Fulcher law, which is given by the expression

$$\tau = \tau_0 \exp\left(\frac{E_a}{k_B(T-T_0)}\right),$$

where  $\tau_0$  is the relaxation time constant,  $T_0$  is a measure of the interaction between magnetic clusters,  $k_B$  is the Boltzmann constant and  $E_a$  is an activation energy parameter; and (ii) the Power-law,

$$\tau = \tau_0 \left(\frac{T}{T_g} - 1\right)^{-z\nu}$$

, where  $T_g$  is the freezing temperature,  $\tau_0$  is related to the relaxation of the individual cluster magnetic moment and

$z\nu$  is a critical exponent. Here  $\tau = \frac{1}{\omega} = \frac{1}{2\pi f}$ . The best fits of experimental data to the Vogel-Fulcher law, gives

$T_0 = 45.8 \text{ K}$  and  $\tau_0 = 3.2 \times 10^{-16} \text{ s}$ . However, an attempt to fit the data using Power-law, yielded the fit parameters ( $\tau_0 \sim 10^{-33} \text{ s}$  and  $z\nu > 16$ ), indicates deviation from a proper spin-glass transition. Moreover, the temperature dependence of  $M_{FC}$  and  $M_{ZFC}$  data in  $Co_2TiO_4$  measured using different cooling fields was interpreted in terms of frozen spin clusters which are responsible for the large magnitudes of the coercivity  $H_C \sim 20 \text{ kOe}$  and exchange bias  $H_{EB} \sim -20 \text{ kOe}$  observed below  $10 \text{ K}$ .

Chapter 5 presents a systematic comparison of the magnetic properties of both the compounds  $Co_2SnO_4$  and  $Co_2TiO_4$  with a special emphasis on the compensation point  $T_{COMP}$  and low-temperature anomalous magnetic behavior. This chapter also summarizes the similarities and differences in the phonon spectra (for  $T \leq T_N$ ) and other physical properties of these compounds. The role of ‘Sn’ substitution on the ‘Ti’ site of  $Co_2TiO_4$  and the corresponding changes in the magnetic structure was discussed in detail. Issues like; (i) random anisotropy and random distribution of cations in the A and B-sites, (ii) different temperature dependence of magnetic moments  $\mu(A)$  and  $\mu(B)$ , (iii) pseudo first-order transition below  $15 \text{ K}$  involving Arrot-plot analysis, (iv) giant bipolar exchange bias ( $H_{EB}$ ) obtained under ZFC condition, and (v) dynamical spin-fluctuation of spin-liquid state exiting in both the compounds are also discussed.

Chapter 6 discusses the phonon spectra, electronic spin resonance, magnetization, dielectric studies of the two-phase composites comprising  $(1-x) Co_3O_4 + x Co_2TiO_4$  ( $0 \leq x \leq 1$ ). Major changes occurring in the bond-angles and bond-lengths due to higher ionic size of ‘Ti’ ions ( $1.34 \text{ \AA}$ ) than ‘Co<sup>3+</sup>’ ions ( $1.09 \text{ \AA}$ ) are highlighted. Hipschometric shift ( $\sim 6.3 \text{ cm}^{-1}$ ) of  $A_{1g}$  phonon mode and a giant bathochromic red-shift ( $\sim 25.3 \text{ cm}^{-1}$ ) of  $F_{2g}$  Raman modes were discussed as the crystal structure of the system transform from complete normal spinel ( $Co_3O_4$ ) to inverse spinel ( $Co_2TiO_4$ ). The temperature variation of peak positions of  $A_{1g}$  and  $F_{2g}$  vibrational modes of both  $Co_2TiO_4$  and  $Co_3O_4$  shifts towards high frequencies with clear anomalies across the ferrimagnetic ordering ( $\sim 48 \pm 5 \text{ K}$ ) and antiferromagnetic  $T_N \sim 30 \pm 10 \text{ K}$ , respectively. A detailed compositional dependence of magnetic exchange interactions in these two-phase spinel composites was discussed in detailed. This chapter also deals with

the high frequency ( $500 \text{ Hz} \leq f \leq 10 \text{ MHz}$ ) temperature variation ( $80 \text{ K} \leq T \leq 573 \text{ K}$ ) of broadband dielectric-spectroscopic studies with a special emphasis on the; ac-conductivity  $\sigma_{ac}(T)$ , dielectric permittivity  $\epsilon_r(T)$  and loss-tangent ( $\tan \delta$ ). These studies reveal the dominance of Arrhenius like conductivity instead of variable range hopping of charge carriers. Whereas, the frequency variation of ac-conductivity  $\sigma_{ac}(f)$  was found to increase progressively with increasing  $f$  which follows Power-law relation ( $\sigma_{ac} = A\omega^b$ ). Possible origins of such anomalous changes occurring in the  $\sigma_{ac}(T)$  and  $\epsilon_r(T)$  are discussed in this chapter in a very detailed manner.

Chapter 7 is devoted to the tetragonally distorted normal spinel  $\text{Mn}_3\text{O}_4$  (Hausmannite). This chapter reports the magneto-dielectric ( $\Delta\epsilon_r/\epsilon_r(H)$ ) and ac-magnetic ( $\chi_{ac}(f,T)$ ) response of the sequential magnetic transitions occurring below the  $T_N = 42.5 \text{ K}$ . The zero-field temperature dependence of relative dielectric permittivity ( $\epsilon_r(T)$ ) curves exhibits a large hysteresis of about  $\sim 5.15 \text{ K}$  in consonance with the first-order nature of spiral incommensurate to commensurate planar transition taking place at  $33 \text{ K}$  ( $T_2$ ). This chapter also deals with the Arrott plot ( $H/M$  versus  $M^2$ ) criterion to distinguish the nature of all the sequential transitions occur below  $T_N$ . All the complex magnetic transitions occurring below  $T_N$  including the field-induced structural transition at  $33 \text{ K}$  and lock-in transition at  $38 \text{ K}$  was successfully probed by means of  $\chi_{ac}(f_{ac}, H)$  and ( $\epsilon_r$  versus  $T$ ). The meta-magnetic like features in the M-H isotherms near to  $T_2$  are discussed which are associated with first-order nature of the transition at  $T_2$ . This chapter also clearly demonstrates the evidence of magneto-electric coupling in  $\text{Mn}_3\text{O}_4$  system in which the electric polarization ( $P \sim 3 \times 10^{-6} \text{ C/m}^2$ ) takes maximum value below the spiral-incommensurate to commensurate transition at  $33 \text{ K}$ .

Chapter 8 presents a brief summary of the important findings of our experiments on all the three investigated systems. In this chapter we also identify some open issues which are potentially interesting for the future studies.

## List of Publications:

### (a) In Peer Reviewed Journals:

- (1) S. Thota, K. Singh, **S. Nayak**, Ch. Simon, J. Kumar and W. Prellier, “*The ac-magnetic susceptibility and dielectric response of complex spin ordering processes in  $Mn_3O_4$* ”. J. Appl. Phys. **116**, 103906 (2014).
- (2) S. Thota, V. Narang, **S. Nayak**, S. Sambasivam, B. C. Choi, T. Sarkar, M. S. Andersson, R. Mathieu and M. S. Seehra, “*On the nature of magnetic state in the spinel  $Co_2SnO_4$* ”. J. Phys.: Condens Matter **27**, 166001 (2015).
- (3) **S. Nayak**, S. Thota, D. C. Joshi, M. Krautz, A. Waske, A. Behler, J. Eckert, T. Sarkar, M. S. Andersson, R. Mathieu, V. Narang, M. S. Seehra, “*Magnetic compensation, field-dependent magnetization reversal, and complex magnetic ordering in  $Co_2TiO_4$* ”. Phys. Rev. B **92**, 214434 (2015).
- (4) **S. Nayak**, D. C. Joshi, M. Krautz, A. Waske, J. Eckert, S. Thota, “*Reentrant spin-glass behavior and bipolar exchange-bias effect in ‘Sn’ substituted cobalt-orthotitanate*”. J. Appl. Phys. **119**, 043901 (2016).
- (5) **S. Nayak**, K. Dasari, D. C. Joshi, P. Pramanik, R. Palai, A. Waske, R. N. Chauhan, N. Tiwari, T. Sarkar, S. Thota “*Low-temperature anomalous magnetic behavior of  $Co_2TiO_4$  and  $Co_2SnO_4$* ”. J. Appl. Phys. **120**, 163905 (2016).
- (6) **S. Nayak**, K. Dasari, D. C. Joshi, P. Pramanik, R. Palai, V. Sathe, R. N. Chauhan, N. Tiwari, S. Thota “*Spectroscopic studies of  $Co_2TiO_4$  and  $Co_3O_4$  two-phase composites*”. Phys. Stat. Sol. (b) **253**, 2270 (2016).
- (7) **S. Nayak**, D. C. Joshi, P. Pramanik, A. Banerjee and S. Thota “*Tunable Exchange-Bias and Magnetic Compensation Temperature of Two-Phase Spinel Composites  $(1-x) (Co_3O_4) + x (Co_2TiO_4)$* ”. [to be communicated].
- (8) **S. Nayak**, J. Dhillon, S. K. Deshpande, and S. Thota “*Dielectric studies of  $Co_3O_4$ - $Co_2TiO_4$  two phase composites*” [to be communicated].
- (9) **S. Nayak**, K. Dasari and S. Thota “*Spectroscopic studies and dielectric properties of  $Co_2SnO_4$* ” [to be communicated].

### (b) Conference Presentations:

- (1) **S. Nayak**, D. C. Joshi and S. Thota “*Micro-Raman and Electron Spin Resonance studies of  $Co_{3-x}Ti_xO_4$* ”, 2nd International Conference on Nanotechnology ICNT-2015 & Indo-USA joint symposium, Haldia (W.B), India.
- (2) **S. Nayak**, D. C. Joshi, M. Krautz, A. Waske, J. Eckert, S. Thota, “*Reentrant spin-glass behavior and bipolar exchange-bias effect in ‘Sn’ substituted cobalt-orthotitanate*” International Conference on Magnetic Materials and Applications (ICMAGMA – 2015), VIT University, Vellore, Tamil Nadu, India.
- (3) **S. Nayak**, D. C. Joshi, P. Pramanik, M. Krautz, A. Waske and S. Thota, “*Structural and Magnetic properties of Cu doped Cobalt-Orthotitanate*” 2nd International Conference on Materials Science and Technology, (2016) St. Thomas College Pala Arunapuram, Kottayam, Kerala, India.
- (4) S. Thota, K. Dasari, **S. Nayak**, D. C. Joshi, P. Pramanik, A. Waske, T. Sarkar, M. Andersson and R. Mathieu, “*Low-temperature anomalous magnetic behavior of  $Co_2TiO_4$* ” The IEEE International Conference on Microwave Magnetics 2016, University of Alabama in Tuscaloosa, USA.
- (5) **S. Nayak**, K. Dasari, D. C. Joshi, V. Sathe, R. Palai, and S. Thota, “*Temperature dependence of micro-Raman spectroscopy of  $Co_2TiO_4$ ,  $Co_3O_4$  and their composites*” 2016 MRS Fall Meeting & Exhibit, Boston, Massachusetts.
- (6) **S. Nayak**, D. C. Joshi, P. Pramanik, A. Banerjee and S. Thota “*Tunable Exchange-Bias and Magnetic Compensation Temperature of Two-Phase Spinel Composites  $(1-x) (Co_3O_4) + x (Co_2TiO_4)$* ” International Conference on Magnetic Materials and Applications (ICMAGMA – 2017), 1-3, February 2017 at Hyderabad, India.

- (7) **S. Nayak**, J. Dhillon, S. K. Deshpande, D. C. Joshi, P. Pramanik, R. George, and S. Thota “*Dynamic ac-conductivity studies of Cobalt-Orthotitanate*”, National conference on Advances on Materials Science, (2017) Gauhati University, Assam, India.



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## List of Symbols

XRD — X-ray diffraction  
XPS — X-ray Photoelectron spectroscopy  
BE — Binding Energy  
 $T_N$  — Néel temperature  
h — hours  
ZFC — Zero-Field Cooled  
FC — Field Cooled  
A, B sites — Tetrahedral, Octahedral sites  
 $M_R$  — Remanance  
 $H_C$  — Coercivity  
 $H_{EB}$  — Exchange bias  
 $T_{COMP}$  — Compensation temperature  
ASD — Antisite disorder  
FWHM — Full width at half maxima  
SOT — Second order transition  
FOT — First order transition  
Å — Angstrom  
 $\epsilon_r$  — Relative dielectric permittivity  
pm — Picometer  
nm — Nanometer  
mm — Millimeter  
cm — Centimeter  
 $\mu\text{m}$  — Micro-meter  
K — Kelvin  
 $\mu_B$  — Bohr magnetron

## Introduction to Spinel and their Complex Magnetic Structure

### 1.1 Background:

Spinel is a special class of materials with general formula  $A^{2+}B^{3+}_2X^{2-}_4$  in which the anions ( $X = O, S, Se$ ) are arranged in cubic close-packed lattice and the cations A and B occupy partially or all of the octahedral and tetrahedral sites in the lattice. Although the oxidation states of A and B in the archetypal spinel structure are +2 and +3, respectively, other combinations integrating divalent, trivalent, or tetravalent cations are also possible [1, 2]. The unit cell of a spinel contains eight units of  $AB_2X_4$  in which the atoms are located in the following positions: Equivalent positions  $(0, 0, 0; 0, \frac{1}{2}, \frac{1}{2}; \frac{1}{2}, 0, \frac{1}{2}; \frac{1}{2}, \frac{1}{2}, 0) + 8$  A cations at  $0, 0, 0; \frac{1}{4}, \frac{1}{4}, \frac{1}{4}$ ;

16 B cations at  $\frac{5}{8}, \frac{5}{8}, \frac{5}{8}; \frac{5}{8}, \frac{7}{8}, \frac{7}{8}; \frac{7}{8}, \frac{5}{8}, \frac{7}{8}; \frac{7}{8}, \frac{7}{8}, \frac{5}{8}$

and 32 anions 'X' at  $x, x, x; \frac{1}{4} - x, \frac{1}{4} - x, \frac{1}{4} - x$

$x, x, x; \frac{1}{4} - x, \frac{1}{4} - x, \frac{1}{4} - x$

$x, x, x; \frac{1}{4} - x, \frac{1}{4} - x, \frac{1}{4} - x$

In ideal spinel structure the anion parameter is 0.375 with ideal position  $\langle 111 \rangle$ . But most of the cases the anions are displaced from their ideal positions away from the tetrahedron positions. The crystal structure of spinel is quite complex. The large unit cell can be divided into eight small (octants), half of which contain tetrahedral arrangement of anions around the A cations. The anions located in half of the corners at the top and bottom of the small unit cell known as type-I structure (figure 1.1). In the other unit cell, type-II the anions are located at sites similar to those occupied by the anions in type-I cells (figure 1.2). When the cell type-I and type-II are brought together the connection between the anion tetrahedra and octahedra can be clearly seen (figure 1.3). It is interesting to note that this kind of arrangement is, quite similar to that of lattice sites in  $Cu_2Mg$  structure in which the magnesium atoms sit at the corners, at the center of the faces and in two diagonally opposite upper and two diagonally opposite lower octants of the cubic unit cell. On the other hand, the copper atoms are arranged in the tetrahedral sites of the cubic unit cell with similar atomic positions as that of spinel lattice. In the spinel structure, there are one A and three B cations around each anion. The B-X-B bond angle is about  $90^\circ$  and A-X-B is about  $125^\circ$ . The distance between A and X is  $a(x - \frac{1}{4})\sqrt{3}$  and the distance between B and X is  $a(5/8 - x)$ . These bond-angles and the bond-lengths play a crucial role in determining the magnetic properties of the spinels. The cations in the sublattice of the spinel interact among each other antiferromagnetically via non-magnetic anions known as super-exchange interactions ( $J_{ij}$ ) (will discuss in the later section). In general, the interaction between the 'A' cations in the tetrahedral sites and the 'B' cations in the octahedral sites is stronger than others (i.e.,  $J_{AB} > J_{BB}$  and  $J_{AA}$ ). Thus the cation distribution in each site plays a decisive role in various physical properties, especially magnetic and magneto-dielectric properties.

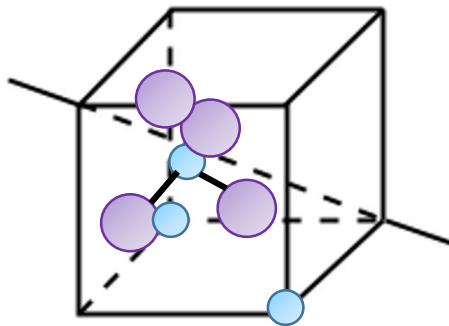


Figure 1.1: Schematic representation of Type-I octant containing cations A in the tetrahedral co-ordinations [5].

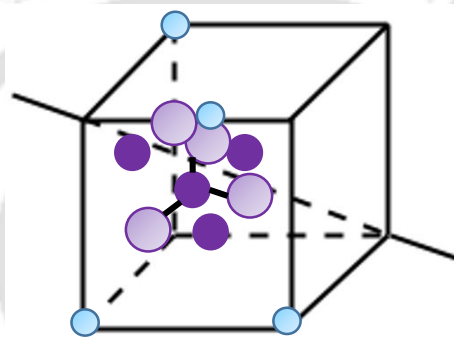


Figure 1.2: Type-II octant containing 'B' cations in octahedral co-ordinations [5].

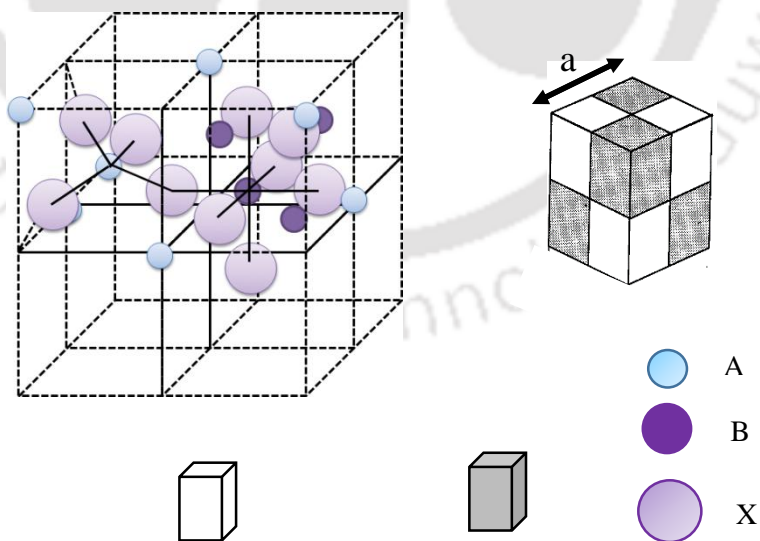


Figure 1.3: The cubic spinel structure of  $AB_2X_4$  with Type I octant containing 'A' cations in tetrahedral and Type II octant having 'B' cations in octahedral voids of oxygen ions [5].

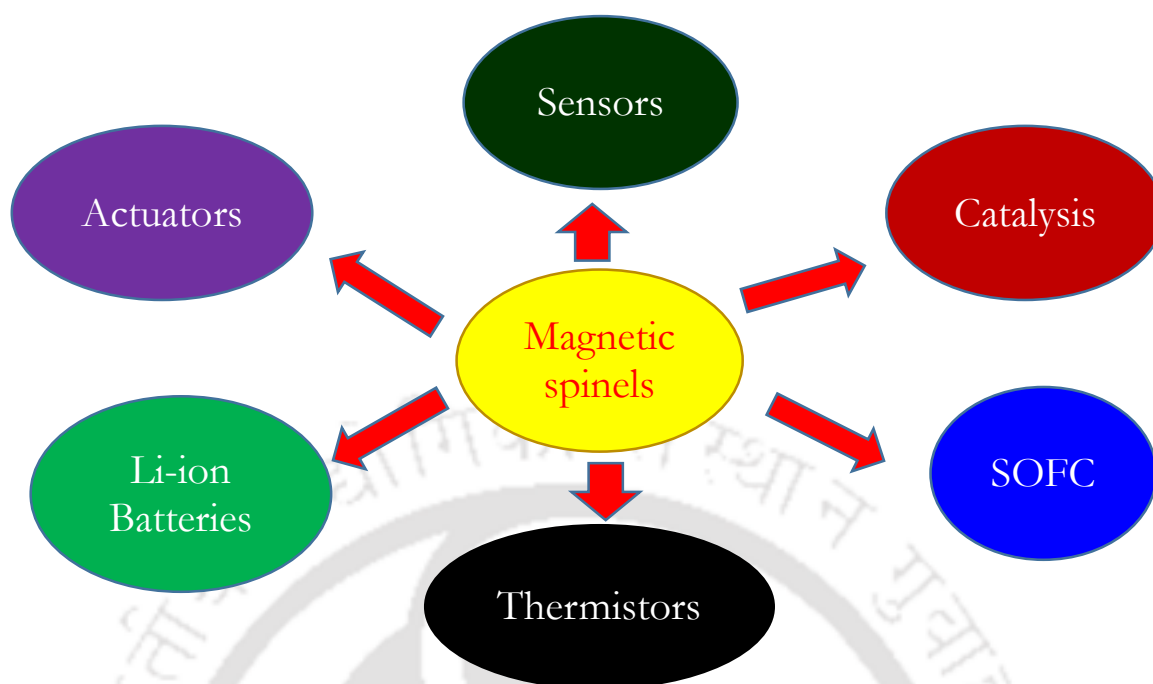
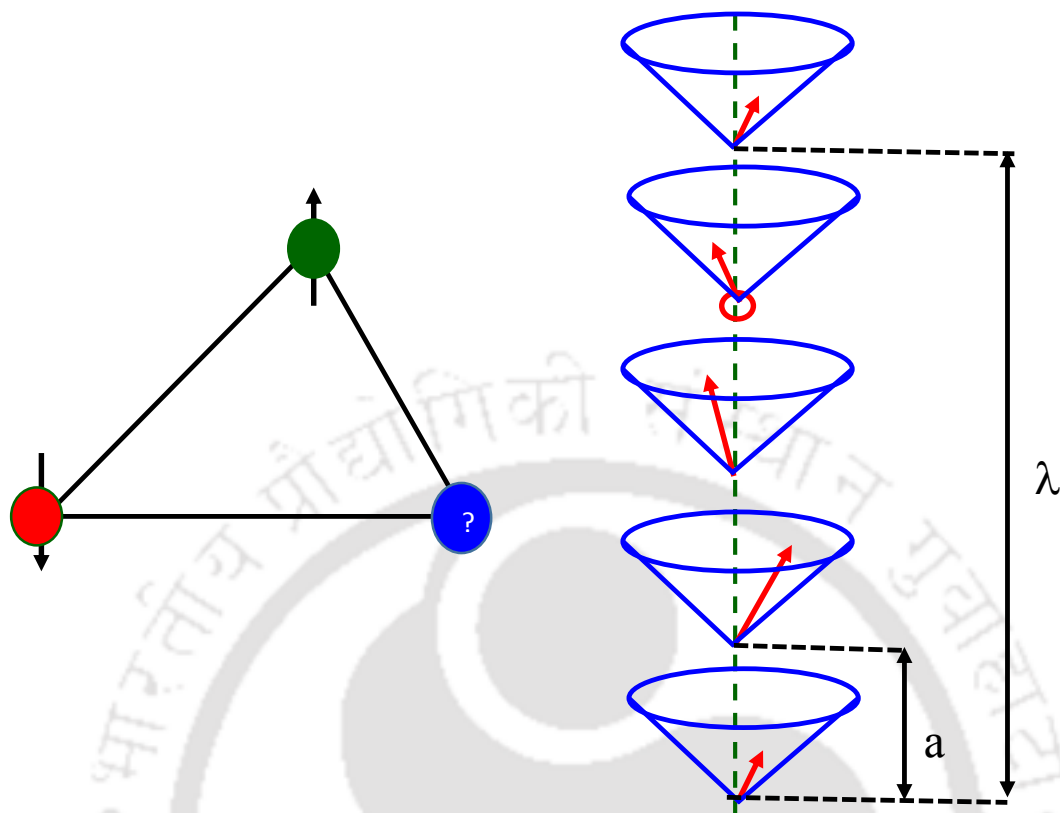


Figure 1.4: Various application of spinels

Generally, spinel can be classified into two categories (i) Normal spinels:  $(A^{2+})_{\text{tetra}}[B^{3+}_2]_{\text{oct}}X^{2-}_4$ , in this configuration all 'A' cations occupy the tetrahedral voids and all 'B' cations occupy the octahedral voids. Example:  $MgAl_2O_4$ ,  $CoCr_2O_4$ ,  $Co_3O_4$ ,  $Mn_3O_4$ , etc., (ii) Inverse spinels:  $(B^{3+})_{\text{tetra}}[A^{2+}B^{3+}]_{\text{oct}}X^{2-}_4$ , in this configuration half of the B cations occupy tetrahedral voids and rest of the 'B' cations along with 'A' sit in the octahedral voids. Examples of Inverse are  $Fe_3O_4$ ,  $Co_2TiO_4$ ,  $Co_2SnO_4$ ,  $Co_2MnO_4$ , etc. Including these two types another class of spinels is also possible that is the Mixed spinel structure where both 'A' and 'B' cations occupy the tetrahedral as well as octahedral sites, for example  $Mn_{0.8}Fe_{0.2}[Mn_{0.2}Fe_{1.8}]O_4$ ,  $Mg_{0.1}Fe_{0.9}[Mg_{0.9}Fe_{1.1}]O_4$ .

### 1.2 Applications of Spinel:

Since 1960's magnetic spinels are widely studied because of their potential applications in various research areas, including magnetic-recording and microwave devices [3-6]. Among a wide variety of spinel compounds, manganese and cobalt based oxide-spinels drawn immense attention in recent years due to their strong catalytic activity towards the oxygen reduction reaction in alkaline solutions [3-8]. The oxygen reduction reaction has been one of the most important issues of electrochemistry owing to its importance in a variety of energy applications including fuel-cells and batteries [9-12]. Due to its catalytic activity, low cost, simple fabrication and ability to accommodate wide range of dopants, these spinel oxides have been investigated extensively as electro-catalysts and electrode in solid oxide fuel cell technology [13]. Magneto-dielectric can be described as materials in which



**Figure 1.5:** Schematic diagram of triangular and spiral or canted spin-spiral arrangements.

magnetic ordering produces dielectric anomalies or alternately, materials in which the low frequency dielectric constant is sensitive to an external magnetic field [14]. Spinel which show such magneto-electric coupling also find a large number of potential applications like magnetic read-write heads, magnetically tunable capacitor, magnetic field sensors, non-volatile multi bit data storage devices and transducers (figure 1.4) [13, 15-17].

### 1.3 Magnetic Exchange Interactions using Molecular Field Theory:

It is well known that the fundamental aspect of magnetism is linked with the orbital and spin degrees of freedom of electrons and their interaction with one another. The magnetic behavior of materials can be classified into the following five main categories: (i) Diamagnetism (ii) Paramagnetism (iii) Ferromagnetism (iv) Ferrimagnetism (v) Antiferromagnetism. Materials in the first two groups are those that exhibit no collective magnetic interactions and are not magnetically ordered. Whereas, materials in the last three groups exhibit long-range magnetic order below a certain critical temperature, known as Curie temperature ( $T_C$ ) or Néel ( $T_N$ ) temperature. In the ferromagnetic systems, the moments are aligned parallel to each other and exhibits spontaneous magnetization below  $T_C$  even in the absence of external magnetic field. In antiferromagnetic compounds, the adjacent moments align antiparallel to each other in such a way that the net magnetic moment is

zero below the characteristic temperature  $T_N$ . Ferrimagnetic materials also contain antiparallel alignment of the unequal magnetic moment with the partial cancellation of the two magnetic sub-lattices with different magnetic moments and they undergo parallel alignment of intra sub-lattice moments and antiparallel alignment of inter sub-lattice moments with partial cancellation of the moment. In 1970, Louis Eugène Félix Néel proposed that antiferromagnetic and ferrimagnetic substances contain two sublattices, one of those spins tends to be antiparallel to those of each other. In case of antiferromagnetic compounds Néel assumed that the magnetic moment of the two sublattices to be equal, so that the net moment of the materials was zero. Since Néel's original hypothesis the term antiferromagnetism has been extended to include materials with more than two sublattices and those with triangular, spiral, or canted spin arrangements; the latter may have a non-zero magnetic moment (figure 1.5) [18-26].

The superexchange interaction between two cations via an intermediate oxygen ion is greatest if the three ions are collinear and if their separations are not too great. The ion arrangements in the spinels are likely to be most important are shown in figure 1.6. The first configuration is depicted in figure 1.6a; in this figure both the angle and the distance between the ions are favorable for superexchange. In all other cases, either the angle (figure 1.6c), or the distance (figure 1.6b, 1.6d), or both are unfavorable (figure 1.6e). Thus, the interaction between the sublattices is stronger than those within the sublattices and further that the interaction between ions in 'A' sites is weakest of all. This result thus supports the assumption that sublattice magnetizations are antiparallel to each other; substantial evidence for such configuration comes from neutron diffraction experiments. The molecular field theory first developed to understand the interactions in two sublattice systems ('A' and 'B') [27-30]. For simplicity, consider a body-centered-cubic lattice, in which the 'A' cations occupy the corner positions, and the 'B' cations occupy body center positions of the lattice. An atom situated on tetrahedral (A) site then has nearest neighbors that all lie on octahedral (B) sites and next nearest neighbors that all lie on 'A' sites. An equivalent picture holds for an atom positioned at 'B' site. According to the phenomenological theory of ferromagnetism the molecular field acting on an atom 'A' site

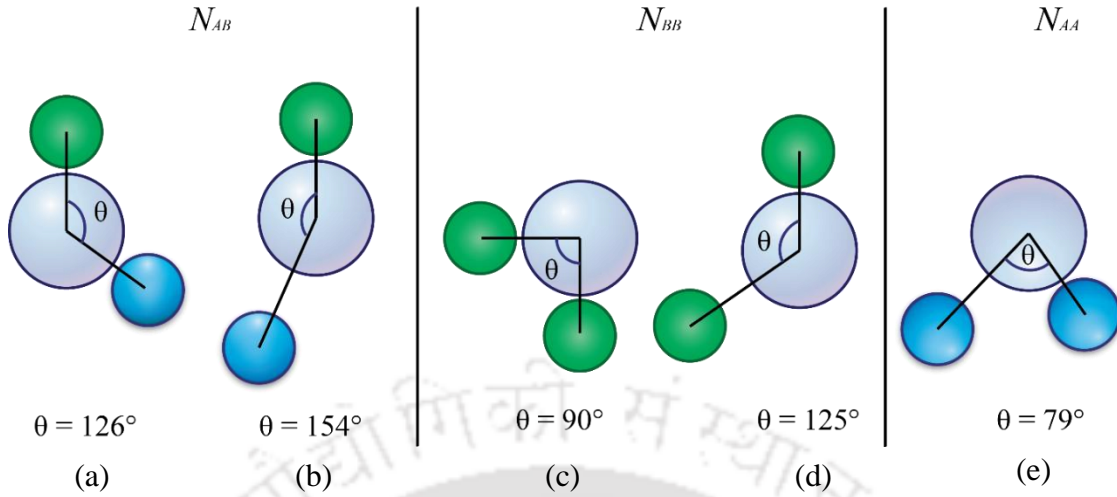
$$H_{mA} = -N_{AA}M_A - N_{AB}M_B \dots (1.1)$$

where  $M_A$  and  $M_B$  are the magnetizations corresponding to the 'A' and 'B' sublattices, respectively, whereas  $N_{AB}$  and  $N_{AA}$  are the molecular field constant for the nearest neighbor and next nearest neighbor interaction, respectively. Similarly, for the atom sitting on the 'B' site the molecular field ( $H_{mB}$ ) can be written as

$$H_{mB} = -N_{BA}M_A - N_{BB}M_B \dots (1.2)$$

Since, similar kind of atoms occupies the 'A' and 'B' sublattices, we can conclude that  $N_{AA} = N_{BB} = N_{ii}$  and  $N_{AB} = N_{BA}$ . Then, if an external magnetic field  $H$  is also applied, the field associated to the 'A' and 'B' sublattices, can be written as

$$H_A = H - N_{ii}M_A - N_{AB}M_B \dots 1.3(a)$$



**Figure 1.6:** Ion pair configuration of super-exchange interaction. Large spheres represents oxygen ions, cations in ‘A’ sites represent by small blue color sphere and small green color sphere are the cations in B sites [18].

and

$$H_B = H - N_{AB}M_A - N_{ii}M_B \dots 1.3(b)$$

The molecular field constant  $N_{AB}$  must be positive as the nearest neighbor interaction between the atoms in the A and B sublattices is antiferromagnetic. On the other hand, the next nearest neighbor interactions may be positive, negative or zero depending on the particular material.

At thermal equilibrium the magnetizations of the sublattices can be written as

$$M_A = \frac{1}{2} N g \mu_B S B_S(x_A) \dots (1.4)$$

where

$$x_A = \left( \frac{S g \mu_B}{kT} \right) H_A \dots (1.5)$$

and the Brillouin function

$$B_S(x_A) = \left[ \frac{2S+1}{2S} \right] \coth \left[ \frac{2S+1}{2S} \right] x_A - \left( \frac{1}{2S} \right) \coth \left( \frac{x_A}{2S} \right)$$

and

$$M_B = \frac{1}{2} N g \mu_B S B_S(x_B) \dots (1.6)$$

where

$$x_B = \left( \frac{S g \mu_B}{kT} \right) H_B$$

and

$$B_S(x_B) = \left[ \frac{2S+1}{2S} \right] \coth \left[ \frac{2S+1}{2S} \right] x_B - \left( \frac{1}{2S} \right) \left( \frac{x_B}{2S} \right)$$

In the above equations ‘N’ represents the total number of atoms or ions per unit volume having a permanent dipole moment, and ‘J’ has been set equal to ‘S’.

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Although there is no antiferromagnetic ordering above the  $T_N$ , a small magnetization is induced in the system in the presence of applied magnetic field. For the minimal applied fields, saturation effects are negligible and the Brillouin function can be substituted by the first term in the above equations, after the expansion of the series with respect to  $x$ , namely,  $B_S(x) = [(S+1)/3S]x$ . The revised equations become

$$M_A = \frac{Ng^2\mu_B^2S(S+1)}{6kT} H_A \dots (1.7)$$

and

$$M_B = \frac{Ng^2\mu_B^2S(S+1)}{6kT} H_B \dots (1.8)$$

now

$$\begin{aligned} H_A &= |H - N_{ii}M_A - N_{AB}M_B| \\ &= H - N_{ii}M_A - N_{AB}M_B \end{aligned}$$

Since  $H$ ,  $M_A$ , and  $M_B$  are parallel in the paramagnetic region. Similarly,

$$H_B = H - N_{AB}M_A - N_{ii}M_B$$

Substitution of these values of  $H_A$  and  $H_B$  into the foregoing equations for  $M_A$  and  $M_B$  gives,

$$M_A = \frac{Ng^2\mu_B^2S(S+1)}{6kT} (H - N_{ii}M_A - N_{AB}M_B) \dots (1.9)$$

and

$$M_B = \frac{Ng^2\mu_B^2S(S+1)}{6kT} (H - N_{AB}M_A - N_{ii}M_B) \dots (1.10)$$

Adding of the equations (1.9) and (1.10) results,

$$M = M_A + M_B = \frac{Ng^2\mu_B^2S(S+1)}{6kT} [2H - (N_{ii} + N_{AB})M] \dots (1.11)$$

Hence the susceptibility  $\chi = M/H$  is given by

$$\chi = \frac{c}{T+\theta} \dots (1.12)$$

where,

$$c = \frac{Ng^2\mu_B^2S(S+1)}{3k}$$

and

$$\theta = \frac{1}{2} C(N_{ii} + N_{AB})$$

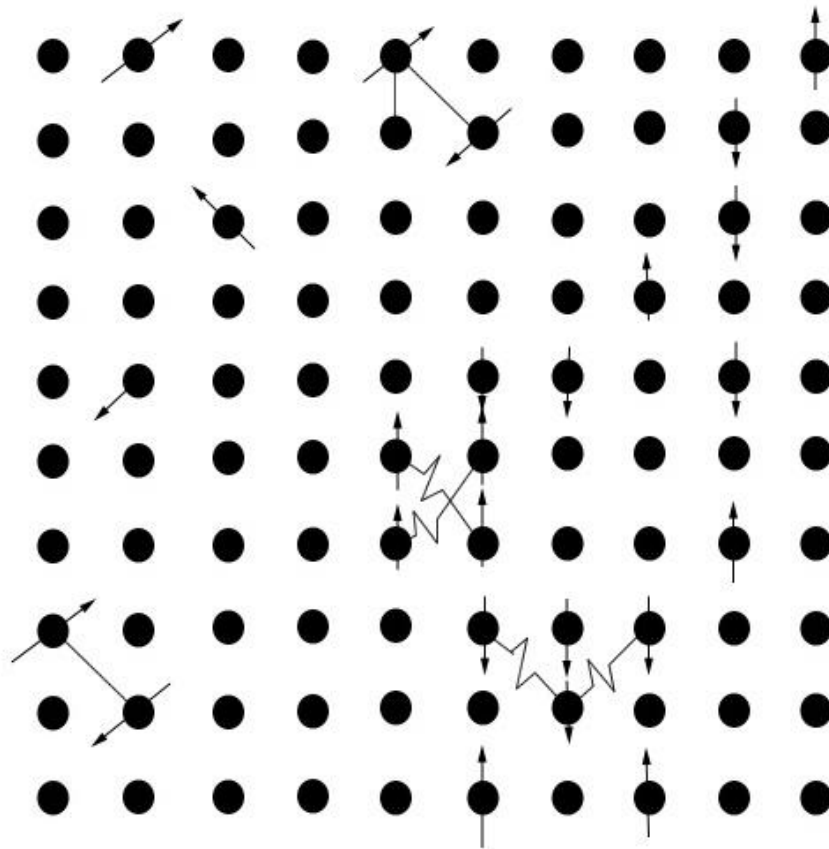
Since, generally,  $N_{AB} > N_{ii}$ ,  $\theta$  is positive. It is interesting to compare the equation  $\chi = C/(T+\theta)$  With equation  $\chi = C/(T - \theta)$ , the Curie-Weiss law so that one can easily evaluate the molecular field constant discussed above [18].

#### **1.4 Dilution Effects and Reentrant Spin-glass State:**

Magnetic frustration resulting from either the competing exchange interactions or dilution of magnetic elements can disrupt the long-range magnetic ordering of any magnetic-material and may lead to spin-glass (SG) state [31-36]. Such disorder driven SG state preceded by a long-range magnetic ordering at higher temperatures are often termed as re-entrant SG systems, which is the subject of this paper [33-36]. Among many such diverse disordered magnetic materials which show re-entrant SG state, cobalt (Co) based inverse-spinel oxides (e.g.  $\text{Co}_2\text{SnO}_4$  and  $\text{Co}_2\text{TiO}_4$ ) are considered as unique systems mainly because of their interesting magnetic properties resulting from octahedrally coordinated divalent 'Co' ions [37, 38]. Usually, frozen-spin behavior can be seen in dilute metallic alloys and nonmetallic systems [39]. At the point of transition the alignment of the canting-spin freeze due to a high degree of randomness and strong competing interaction among the crystal sub-lattice of the systems without developing long-range order [40]. Recently, spin-glass behavior has also been observed in magnetic-spinel due to the presence nonmagnetic cations in the two sub-lattices lead to geometric frustration [31-36]. The following sections describe the origin of disorderness in standard spin-glass systems.

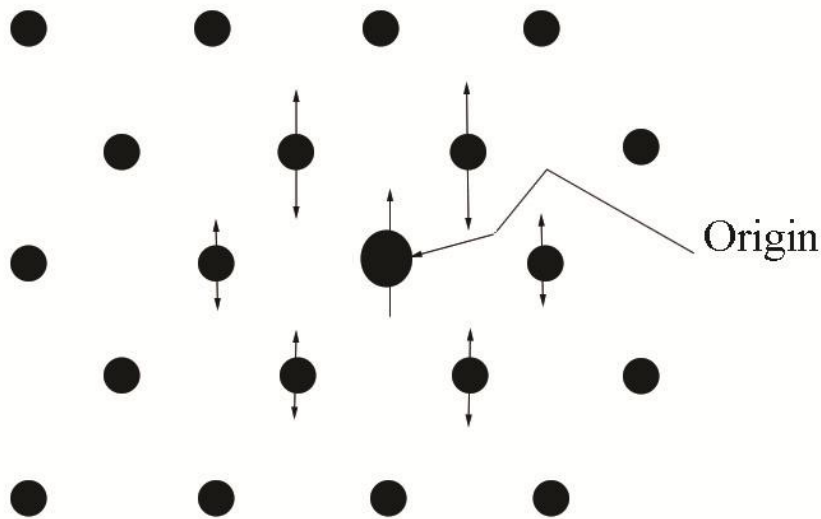
Figure 1.7 represents the square lattice whose sites are denoted by the dots. A certain fraction 'x' is occupied by the magnetic moment or spin which are distributed randomly all over the lattice sites and are indicated by the arrows. In order to avoid too many nearest-neighbor occupancies we keep the 'x' small ( $\sim 1/4$ ). Now the magnetic moments interacts ferromagnetically (parallel) between the nearest neighbor and antiferromagnetically (antiparallel) between the next nearest neighbors. Such a situation is illustrated in figure 1.7 where we have removed any thermal disorder by reducing the temperature to a negligible value. In the figure we choose arbitrarily the alignment of the top right moment to upwards. Though there are spins or arrows are completely decoupled from the large clusters, but almost all of them connected in the lattice environment strongly and also able to propagate from top to bottom. A perfect balancing of the up and down spins (exhibits zero net moment) also observed. However, a certain number of spins or moments still unable to satisfy their second neighbor bond due to the creation of frustrations. The frustration comes when first neighbor ferromagnetic coupling strength ( $J_1 > 0$ ) exhibits equal values of two second neighbor's antiferromagnetic coupling strength ( $J_2 < 0$ ) i.e,  $|J_1| = |2J_2|$ , then the spin will not know which way to point and disconnects to the two spins below itself.

The most salient example of an entirely frustrated spin-lattice is triangular one, where all the interactions are antiferromagnetic and the surroundings spins are in a totally confused state once the direction of the center spin is chosen (as shown in figure 1.8). In terms of energy consideration, the frustrated spins unable to make any difference as they are not capable to change the rotation of the magnetization vector. Such situation is popularly known as 'frozen state', an identical state in 3D lattice at  $T = 0$  K. The basic ingredients of the frozen state of a spin-glass are (i) randomness (ii) mixed interaction and (iii) frustration, such conditions lead to many possible ground state configurations. Now in order to know much about the SG state, we have to understand the formation of the random mixing of the spins at high temperature. The randomness in SG systems and compounds with mixed



**Figure 1.7:** Schematic representation of frozen spin glass with  $J_1 > 0$  (ferromagnetic) and  $J_2 < 0$  (antiferromagnetic). The zig-zag links indicate a broken bond [67].

interacting spin configuration follows a co-operative freezing of spins at a definite temperature often called as “Freezing temperature ( $T_f$ )”. Below  $T_f$  a highly irreversible, metastable frozen state occurs which is short range spatial magnetic order in nature [33-36]. In a single word spin-glass represents the ‘frozen state’ of the compound. The two most key requirements of spin-glass are the randomness in positions of the spins, or the signs of the neighboring couplings: ferro ( $\uparrow\uparrow$ ) or antiferromagnetic ( $\uparrow\downarrow$ ) or in both. There must be disorder, as the site or bond disorder creates spin-glass state, otherwise the magnetic transition will be normal long range ordering transitions (ferromagnetic or antiferromagnetic) [41, 42]. The combine effects of the randomness and the competing or mixed interactions is the source of frustration, as illustrated in figure 1.7. This second requirement of frustration is the sole characteristic of the spin-glass ground state, which is disordered, but still exhibits many exciting properties associated to its co-operative nature. For example, a macroscopic anisotropy is created and peculiar metastabilities (time and aging dependence) occur especially in reaction to an applied magnetic field. Observation of exchange-bias phenomena below  $T_f$  is one of the recent observations noticed in re-entrant SG system which will be discussed in more detailed way in the coming chapters. It is sufficient to say that, there must be disorder in the constitution



**Figure 1.8:** Schematic diagram of frustrated triangular (hexagonal) lattice with all antiferromagnetic interactions ( $J_1 < 0$ ) [67].

of a spin glass: either site randomness with various distances between the magnetic spins, or bond randomness where the nearest neighbor interaction varies between parallel and antiparallel coupling  $+J$  and  $-J$ .

The spin-glass problem is the interactions between the spins and these exchange interactions creates a randomness through which a unique type of ground state is formed. According to quantum mechanics magnetic exchange interaction in the form of spin Hamiltonian can be written as  $H_{ij} = -J_{ij} S_i \cdot S_j$ , which couples the spins at lattice sites ' $i$ ' and ' $j$ '. The energy difference between the parallel and antiparallel configurations should be equivalent to the magnitude of exchange energy. In 1979, theoretical studies by Villian (Scholl and Binder) predicted that increasing of dilution in mixed ferrimagnetic spinels (like  $Mg_{1-t}Fe_{2-2t}Ti_tO_4$  with  $J_{AB} \gg J_{BB} > J_{AA}$ ) may increase the unsatisfied bonds causes competition between percolation and frustration finally results to a new mixed state called (reentrant) spin-glass-like state [40]. Thus  $J_{AB}$  renders the undiluted spinel ferrimagnet, with all A-site moments oriented antiparallel to all B-site moments, but with BB and AA bonds remaining unsatisfied. However, frustration of certain moments occurs due to the dilution of any of the two sublattices and the collinearity of ferrimagnetic phase will collapse well below the percolation threshold for AB bonds [43].

### 1.5 Negative Magnetization in Spinel:

Negative magnetization or magnetization reversal is an exciting phenomenon of the magnetically ordered system, where the dc magnetization verge from a positive value to a negative value as a function of temperature. Such an interesting behaviour is observed in magnetic spinels below their  $T_C$  or  $T_N$  including some perovskite systems, molecular magnets, garnets, intermetallic alloys, and multilayers [44 - 51]. In 1948, Néel gave the first phenomenological theory for the explanation of negative magnetization under the framework of molecular field

theory [52]. Later in 1950, this magnetic reversal phenomenon first observed experimentally in ferrites [53 - 55]. In ferrites, the magnetic moment at the tetrahedral ‘A’ and ‘B’ sublattices are coupled antiferromagnetically with each other. According to the Néel theory, the local molecular fields at the ‘A’ and ‘B’ sublattices can be expressed as

$$H_A = \gamma(\alpha M_A - M_B) \dots (1.13)$$

$$H_B = \gamma(M_A - \beta M_B) \dots (1.14)$$

where,  $M_i$  is the  $i^{\text{th}}$  sublattice magnetization and  $\gamma$  represents molecular field coefficients corresponding to the A-B magnetic exchange interaction. In this equation ‘ $\alpha$ ’ and ‘ $\beta$ ’ are the molecular field coefficient for intra-sublattices interactions (A-A, and B-B) normalized by ‘ $\gamma$ ’. The sublattices Brillouin function  $B_J(x)$  can be given by,

$$B_J(x) = \left[ \frac{2J+1}{2J} \right] \coth \left[ \frac{(2J+1)x}{2J} \right] - \left( \frac{1}{2J} \right) \coth \left[ \left( \frac{1}{2J} \right) x \right] \dots (1.15)$$

and  $x = gJ\mu_B H/k_B T$

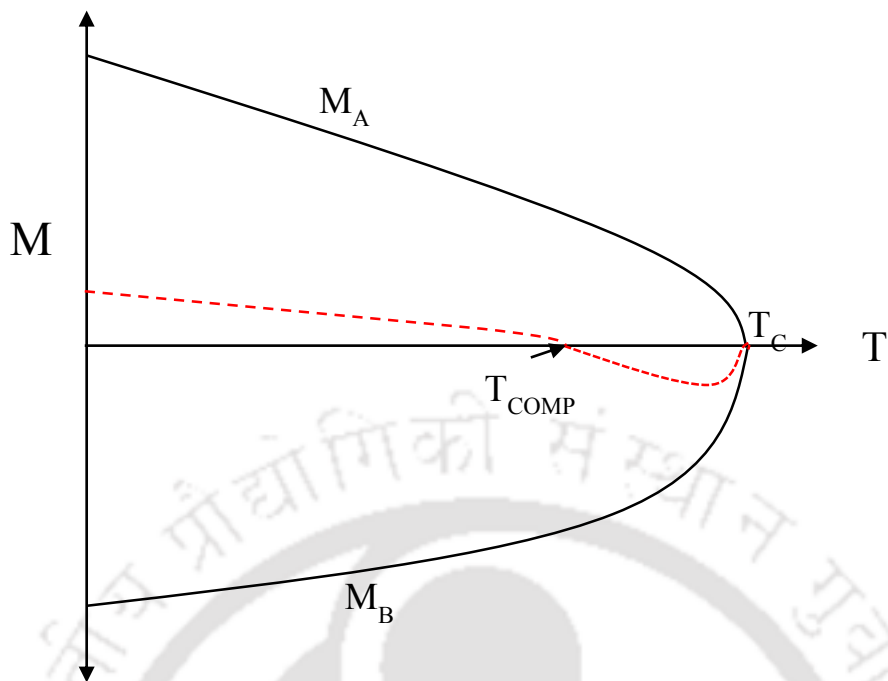
In the above equation ‘J’ is the total angular momentum, ‘g’ is the Lande g-factor,  $\mu_B$  is the Bohr magneton,  $k_B$  is the Boltzmann constant, and ‘N’ is the total number of magnetic atoms/ions per unit volume. The Brillouin function dependence of the ‘A’ and ‘B’ site magnetizations with respect to temperature (T) and external magnetic field (H) are given by

$$M_A = \lambda N g \mu_B S_A B_{S(A)} \left[ \frac{g \mu_B S_A (H + H_A)}{k_B T} \right] \dots (1.16)$$

and

$$M_B = \delta N g \mu_B S_B B_{S(B)} \left[ \frac{g \mu_B S_B (H + H_B)}{k_B T} \right] \dots (1.17)$$

where ‘N’ is the total number magnetic ion per unit volume and  $S_A$  and  $S_B$  are the spin angular momenta for the ‘A’ and ‘B’ sites, respectively. The parameters ‘ $\lambda$ ’ and ‘ $\delta$ ’ are the molar fractions of the magnetic ions at the A and B sites so that  $\lambda + \delta = 1$ . Equations 1.13 to 1.17 can be solved numerically to obtain the temperature as well as external field variations of the ‘A’ and ‘B’ sublattice magnetizations ( $M_A$  and  $M_B$ ) and also the net magnetization ( $\Delta M$ ). In his theory, Néel’s pointed out all prospects of ferrimagnetism i.e, Q-type, P-type, R-type, and N-type ferrimagnetism based on the values of  $\alpha$ ,  $\beta$ ,  $\lambda$ ,  $\delta$ ,  $S_A$  and  $S_B$  [52, 53]. Out of the above mentioned ferrimagnetism, N-type is the most interesting ferrimagnetism with the compensation temperature ( $T_{\text{COMP}}$ )  $0 < T < T_N$ . This situation arises when  $\alpha > \beta$ , and  $0 > \beta > -1$ . Under this condition,  $M_A$  and  $M_B$  exactly balancing each other and for  $\lambda S_A < \lambda S_B$  and the net magnetization is parallel to B sublattice magnetization with a possibility of a negative magnetization below  $T_N$ . Figure 1.9 shows temperature dependence of  $M_A$  and  $M_B$  along with the net magnetization. According to molecular field theory, it is evident that the sublattice magnetization respond



**Figure 1.9:** Temperature variation of magnetization  $M(T)$  for the N-type ferrimagnetism as per the Néel's theory. The net magnetization is represented as the dotted red color line [62].

differently with temperature resulting the magnetization reversal. Néel's theory (by considering two/three magnetic sublattices) successfully explained the observed magnetization reversal in a large varieties of spinel compounds, e.g,  $\text{NiFe}_{2-x}\text{V}_x\text{O}_4$  [56],  $\text{Fe}_2\text{MoO}_4$  [57],  $\text{CoCr}_{2-x}\text{Fe}_x\text{O}_4$  [58, 59],  $\text{Li}_{0.5}\text{Fe}_{1.7}\text{Al}_{0.8}\text{O}_4$  [60]. However, Néel's theory, unable to predict the nature of net-magnetization once it becomes negative and opposite to the field direction. If the system exhibits finite value of anisotropy, then in presence of low magnetic field the Zeeman energy is suppressed by the anisotropy energy as a result, the net magnetization reversed to the applied field direction and hence negative magnetization appears. Later Belov *et al.* explained the negative magnetization in some other ferrites and garnets using the concept of weak magnetic sublattice [61]. According to this theory, the ferrimagnetic systems contain (i) a weak magnetic sublattice having anomalous temperature dependence of magnetization, and (ii) strong magnetic sublattice with normal 'Weiss-type' temperature dependence of magnetization. At  $T < T_{\text{COMP}}$ , magnetization of the weak magnetic sublattices behaves like that of a strong magnetic sublattice, whereas above  $T_{\text{COMP}}$  it behaves like an 'exchanged-enhanced' paramagnetic sublattice [61]. Belov *et al.* further predicted that weak magnetic sublattice exists due to the presence of the unidirectional magnetic anisotropy in ferrites [61]. This anisotropy arises because of the presence of the effective exchange field of the 'strong' sublattices, ordered at a high temperature. Ferrimagnetic systems like  $\text{Zn}_x\text{Mg}_{0.75-x}\text{Cu}_{0.25}\text{Fe}_2\text{O}_4$ ,  $\text{Zn}_x\text{Cu}_{1-x}\text{FeCrO}_4$ ,  $\text{Zn}_x\text{Ni}_{1-x}\text{FeCrO}_4$ , and  $\text{Zn}_{0.4}\text{Co}_{0.6}\text{Al}_x\text{Fe}_{2-x}\text{O}_4$  shows sign reversal of a net magnetization as a consequence of either different ordering temperatures of 'A' and 'B' sublattices or a non-Weiss type ordering of A or B sublattice moment, which support Belov hypothesis [62-66].

### 1.6. Description of the Problem and the Approach:

Besides their potential technological applications, number of exciting magnetic properties exhibited by the spinel oxides poses many challenges to researchers in understanding their exact origin. In particular, phenomena like the low temperature spin-liquid state, exchange-bias under zero-field-cooled condition and reentrant spin-glass ordering in spinel oxides drawn immense attention recently [67-76]. In the present thesis, we first attempt to study the role of dilution on the low-temperature magnetic ordering of ferrimagnetic spinel cobalt orthostannate ( $\text{Co}_2\text{SnO}_4$ ) and cobalt orthotitanate ( $\text{Co}_2\text{TiO}_4$ ). Although few reports are available in the literature dealing with the dc-magnetization of both these oxides with ordering temperature 41 K and 55 K for  $\text{Co}_2\text{SnO}_4$  and  $\text{Co}_2\text{TiO}_4$ , respectively, but a clear understanding of the low-temperature ac-magnetization studies at different frequencies was lacking in the literature when we endeavored this problem. It was believed that non-magnetic  $\text{Sn}^{4+}$  or  $\text{Ti}^{4+}$  randomize the cationic distribution in the octahedral site, which may break the symmetry of octahedral crystal field [77 - 83]. As a result, the system possess frustration in the magnetic ordering, and may result spin-glass-like ordering, negative magnetization and compensation effect below  $T_N$ , which are the main objectives of the current thesis [62-65, 77, 82, 83]. Our approach to understand the role of dilution is two-fold: first to perform a detailed temperature, frequency and dc-magnetic field dependence of ac-magnetic susceptibility, and secondly to perform the heat-capacity measurements under various dc-fields, and probe the nature of magnetic transitions in both the systems. Though there are few reports available in the literature showing the signatures of (i) asymmetry in hysteresis loops, (ii) two-peak behavior in the temperature dependence of magnetization, and (iii) random-anisotropy in both  $\text{Co}_2\text{SnO}_4$  and  $\text{Co}_2\text{TiO}_4$ . However, a detailed work involving the low-temperature Raman active modes, Arrott plots ( $H/M$  versus  $M^2$ ) analysis, dynamic-scaling studies (e.g. Vogel-Fulcher law and Power-law of critical slowing down), and magnetic field dependence of specific heat was missing in the literature. Such issues are addressed in this thesis. We have also made attempts to understand the high-temperature ac-electrical resistivity, vibrational excitations using Raman spectroscopy and other characteristics of both  $\text{Co}_2\text{SnO}_4$ ,  $\text{Co}_2\text{TiO}_4$  and the two-phase composites of  $\text{Co}_3\text{O}_4$  and  $\text{Co}_2\text{TiO}_4$ .

Field induced magneto-structural quantum phases reported in tetragonally distorted ferrimagnetic normal-spinel Hausmannite ( $\text{Mn}_3\text{O}_4 = (\text{Mn}^{2+})[\text{Mn}^{3+}]_2\text{O}_4$ ) is another topic motivated us to reinvestigate [84 - 90]. In 2010, Kim *et al.* reported the complex magnetic structure of  $\text{Mn}_3\text{O}_4$  below  $T_N$  (= 43 K) using the temperature and magnetic field dependent X-ray diffraction and vibrational spectra of single-crystal  $\text{Mn}_3\text{O}_4$  [91]. These authors observed a significant shift in the Raman active  $T_{2g}$  mode frequency between 33 K and 39 K, where, the system exhibits incommensurate magnetic phase regime. Below 33 K, the  $T_{2g}$  mode abruptly splits into two modes near  $290\text{ cm}^{-1}$  and  $300\text{ cm}^{-1}$ . Such splitting was consistent with the tetragonal to monoclinic structural phase transitions taking place below 33 K, which lift the degeneracy of  $T_{2g}$  mode by expanding the  $\text{Mn}^{2+}\text{-O}^{2-}$  bond length along the easy axis direction and contracting the  $\text{Mn}^{2+}\text{-O}^{2-}$  bond length along the hard axis direction (such stretching is linked with the giant atomic displacement of  $\sim 0.25\text{ \AA}$  without breaking inversion symmetry and colossal magnetic anisotropy below  $T_N$ ). Nonetheless, the magnetization dynamics below the long-range ordering at varying ac-

## ***Chapter 1: Introduction to Spinel and their Complex Magnetic Structure***

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magnetic field frequencies was lacking in the literature. Hence, an attempt has been made to understand the ac-magnetic response of all the phase transitions occurring below  $T_N$  under the superimposition of various dc-bias fields. We also studied the magnetic-field dependence of dielectric permittivity  $\{\epsilon_r(H,T)\}$  under both cooling and heating cycles with special emphasis to probe the newly observed lock-in transition at 38 K below the Yafet-Kittle type and spiral incommensurate transitions.



#### **2.1 Synthesis of the Oxide Spinel:**

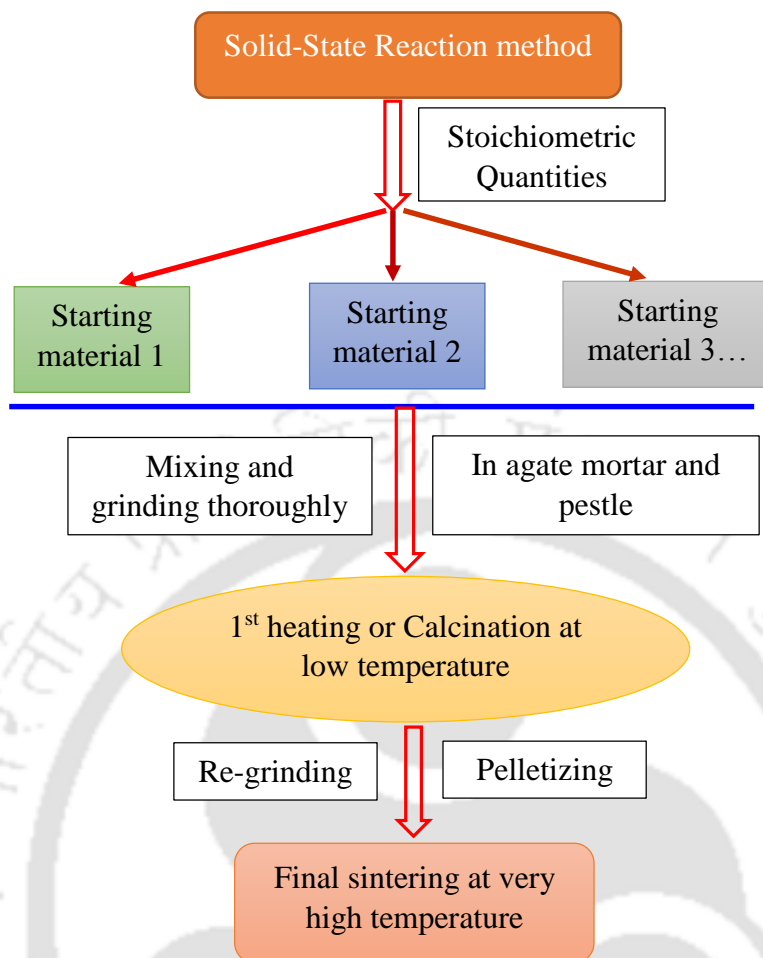
This chapter describes the synthesis procedure of the investigated compounds and the characterization techniques implemented for studying the structural, magnetic, morphological and optical properties. All the high quality precursors were procured from Alfa Aesar GmbH and Sigma-Aldrich Chemicals. Several methods are available to synthesize polycrystalline samples in bulk grain forms, such as, solid-state-reaction, sol-gel processing, co-precipitation method, vapor phase transport etc. In this thesis, we employed both solid-state-reaction technique and sol-gel process for the preparation of  $\text{Co}_2\text{SnO}_4$ ,  $\text{Co}_2\text{TiO}_4$  and  $\text{Mn}_3\text{O}_4$  polycrystals.

##### **2.1.1 Solid State Reaction:**

Solid-state-reaction method is the most versatile technique, thermodynamically stable and environment friendly process for the synthesis of polycrystalline bulk cobalt and manganese oxides. The main advantage of the solid state reaction method is that it provides a wide range of selection of precursors like oxides, carbonates etc. As the starting materials do not react with each other at room temperature, prominent temperature with proper heating and cooling rates are needed for the appropriate reaction. Thus, the thermodynamic as well as the kinetic factors are important for the solid state reaction method in which raw materials react in the absence of any solvent at very high temperature. Therefore, after the heat-treatment process the final product obtained from this method is in form of solid with big grain sizes. Figure 2.1 shows the flowchart of the synthesis procedure. High purity binary transition metal oxides of fine grain size were taken in stoichiometric amounts and grind them together in an agate mortar using a pestle for 4 h so that the mixed powders attain a high degree of homogeneity and better contact is achieved between surfaces of the reactants. This product was calcined in air for 4 h between 500-600°C to remove the volatile substances present in the mixture. This mixture was regrind for 1 h and pelletized using a 13 mm KBr die and hydraulic press (5 tons/cm<sup>2</sup>) to form compact cylindrical pellets. These pellets are sintered at high temperature 1200°C-1350°C for 8 - 12 h in air with cooling and heating rates 4°C/minute to form dense ceramic compound of desired composition. The final sintering temperature and pre-sintering conditions are varied depending on the nature of the sample for required properties. For the preparation of polycrystalline  $\text{Co}_2\text{SnO}_4$ ,  $\text{Co}_2\text{TiO}_4$  and the  $\text{Co}_3\text{O}_4$  -  $\text{Co}_2\text{TiO}_4$  two-phase composites we followed the above mentioned procedure. However,  $\text{Mn}_3\text{O}_4$  was synthesized using the sol-gel process described below.

##### **2.1.2 Sol-gel Method:**

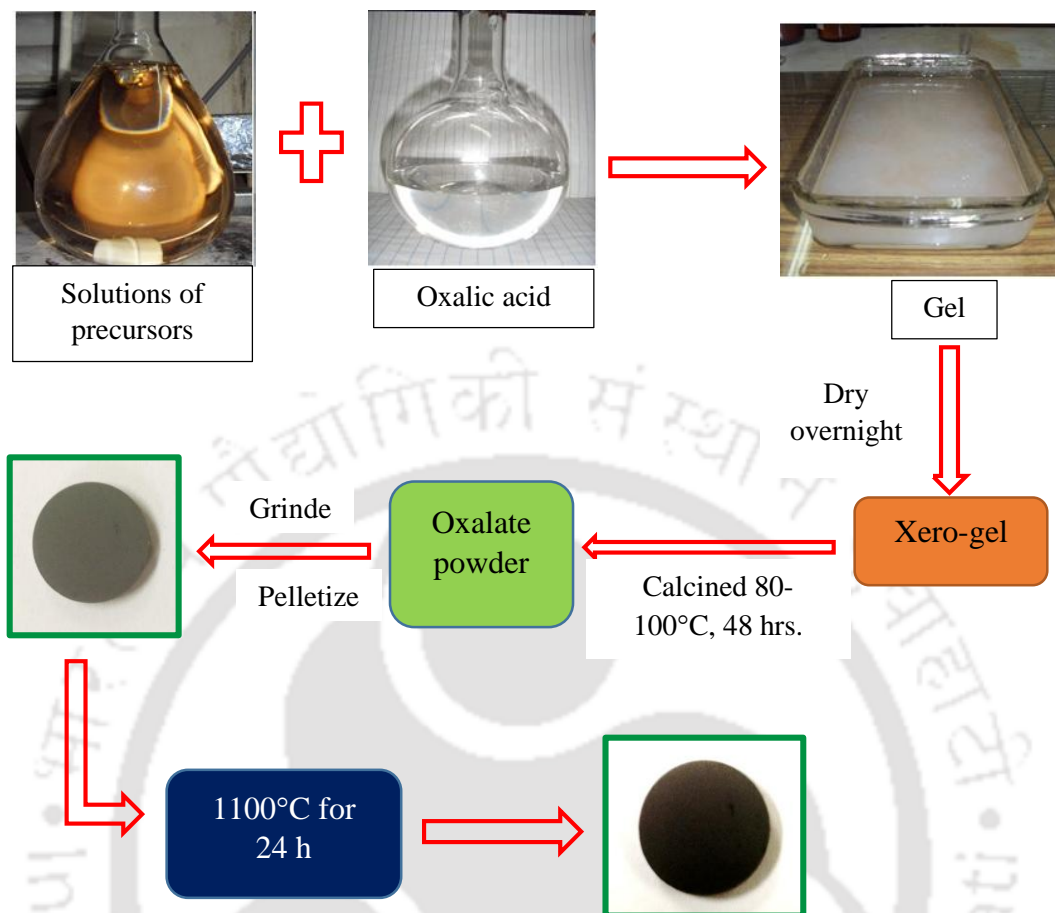
Sol-gel process involves conversion of monomers into a colloidal solution (commonly known as sol) that acts as the precursor for an integrated network (or gel) of either discrete particles or polymer networks. In this method wide variety of precursors can be selected as starting materials to prepare magnetic and non-magnetic ceramic



**Figure 2.1:** Schematic diagram of standard solid state reaction method employed in the present work.

oxides. Sol-gel process has many advantages like simple, cost effective, requires low temperature for processing, allows high degree of solubility, provides homogenous dispersion of dopants, and controls the composition accurately [92]. The precise size control of the particle is the main strength of the sol-gel process. Due to this oxides nanoparticles obtained from alkoxide are preferred to prepare by sol-gel technique. It also provides better control of the microstructure and density.

Figure 2.2 depicts various steps of sol-gel method involves in the synthesis of crystalline oxides. Initially, the starting materials were dissolved in the solvent (distilled water, ethanol or acid) and then mixed together thoroughly. The resultant mixture was kept under stirring for 1-2 h at 50°C to ensure the homogeneity of the solution. Proper amount of citric acid or oxalic acid solution added to the mixture. Here citric acid/oxalic acid act as a gulating agent and carboxylate group in it act as ligands to form linked-complex network with the cations. The obtained gel kept at 80-100°C in a hot air oven for several hours till the water/ethanol/acids evaporate. The oven dried product obtained after this process is called metal xerogel. This xerogel was calcined at temperatures between 500-800°C to remove the volatile substances such as crystallizing water, CO and CO<sub>2</sub> to form the final



**Figure 2.2:** Various stages of the sol-gel method used to synthesize single phase ceramics.

product. In the present case polycrystalline  $Mn_3O_4$  sample was synthesized by sol-gel process using manganese acetate tetrahydrate  $[Mn(CH_3COO)_2 \cdot 4H_2O]$  and oxalic acid  $[C_2H_2O_4 \cdot 2H_2O]$  as precursors and ethanol as solvent. Initially, manganese acetate tetrahydrate was dissolved in ethanol under constant stirring and moderate heating to obtain transparent wine color solution (called sol) [93]. The oxalic acid solution was added drop-wise to the transparent sol yielding a thick wet-gel network called aerogel. This aerogel was then dried in a hot air oven at  $80-100^\circ C$  for 48 h to obtain the manganese oxalate dihydrate  $[MnC_2O_4 \cdot 2H_2O]$ , which further heated at  $500^\circ C$  for 2 h in air to obtain mainly  $Mn_2O_3$  as major product which was further heat treated at  $1100^\circ C$  for 4 h [93]. This product was ground in an agate mortar, then pressed into pellets and finally sintered at  $1200^\circ C$  for 48 h and quenched from  $1200^\circ C$  to liquid nitrogen temperature. Such quenching is necessary to avoid the formation of other stable manganese oxides e.g.  $MnO_2$ ,  $Mn_2O_3$ , and  $Mn_5O_8$ .

**2.2 Characterization Techniques:**

**2.2.1 Structural Characterization:**

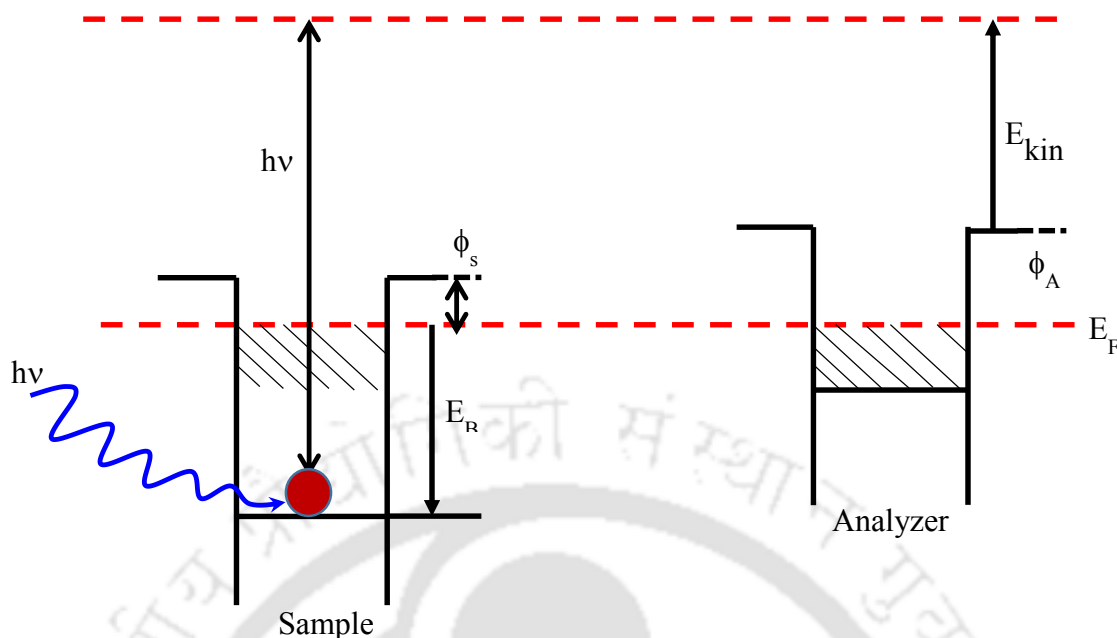
We employed X-ray diffraction technique to determine the crystal structure of the synthesized spinel oxides because this technique is a powerful and non-destructive structural characterization tool. In the present work we used two different X-ray sources; the first one is Co- $K_{\alpha}$  radiation of wavelength  $\lambda = 1.7889 \text{ \AA}$  and the second source is Cu-  $K_{\alpha}$  radiation with  $\lambda = 1.5406 \text{ \AA}$  from PHILIPS (Model: PW-1050) X-ray powder diffractometer and from Rigaku (Model: TTRAX-III) X-ray diffractometer in  $\theta - 2\theta$  geometry. These diffractometers consist of scintillation detectors on the circumference of the vertical circle. Few micron thick Ni foil is placed in the form of the source window to filter out the  $K_{\beta}$  lines from  $K_{\alpha}$  radiation. The sample stage is fixed and positioned at the center of the circle while the goniometer assembly provides uniform rotation of both the source and detector. We also used the software called FullProf programme to perform the Rietveld refinement of the experimentally extracted X-ray diffraction pattern.

**2.2.2 Surface Morphology and Microstructure:**

To probe the surface morphology and microstructure of the samples investigated in the present work we employed a scanning electron microscope (SEM, M/s LEO, 1430vp) and a field-emission-scanning electron microscope (FESEM, from m/s Zeiss, Sigma). Both these electron microscopes were used under secondary-electron (SE) mode to probe the microstructure of the bulk samples studied in this work. SEM is also equipped with energy dispersive X-ray spectrometer (EDS/EDAX) which is used to trace the elements present in the samples.

**2.2.3 X-ray Photoelectron Spectroscopy:**

In this thesis, we extensively used the X-ray photoelectron spectroscopy (XPS) for the determination of the electronic structure of the samples. It is well known that the XPS is a surface-sensitive quantitative spectroscopic technique involving photon and electrons that mainly use for the quantification of the elemental composition. XPS spectra are obtained by exposing a material from the top-surface to few nanometers depth (typically from 0 to 10 nm) with a beam of X-rays while simultaneously measuring the kinetic energy and number of electrons (similar to Photoelectric effect). It requires high vacuum ( $P \sim 10^{-8}$  millibar) or ultra-high vacuum (UHV;  $P < 10^{-9}$  millibar) to analyze the samples at pressures of a few tens of millibar. XPS mainly involves the interaction of X-ray photons with electrons in the energy range 1-5 keV (for soft X-rays), and 5 - 8 keV (for hard X-rays) and is widely used to study the chemical composition and/or speciation of the outer 1-2 nm of solid surface. XPS is also a sensitive probe of the chemical environment and/or oxidation state of surface species. Core level XPS is highly sensitive to the chemical environment (the binding energy may be strongly dependent on the oxidation state of the investigated ion, as well as on the neighboring atoms). Photoelectric effect can be understood by means of the following three



**Figure 2.3:** Schematic diagram of Photoemission process.

steps: (a) Probability of creation of photoelectron by photo-excitation of the solid, (b) Transport of photoelectron to sample surface, and (c) Emission of photoemission into vacuum and then to the energy analyzer. Photoelectrons generated by the incident photon energy  $h\nu$  are transported to the continuum where they are detected by electron energy analyzer. This is possible only if the incident photon energy is greater than or equal to the sum of binding energy ( $E_B$  or BE) of the electron with respect to energy of Fermi level ( $E_F$ ), and the work function ( $\Phi_s$ ) of the sample. So that, one can write

$$h\nu = E_B + \Phi_s + E_{kin} \dots (2.1)$$

Where  $E_{kin}$  is the kinetic energy of the photoelectron. Since the electron has to overcome work function in order to be detected by the analyzer. Thus, the modified equation becomes

$$h\nu = E_B + \Phi_s + (\Phi_A - \Phi_s) + E_{kin} \dots (2.2)$$

From the above equation we can obtain the binding energy of the emitted electron

$$BE = E_B = h\nu - \Phi_A - E_{kin} \dots (2.3)$$

The intensity of XPS spectra is recorded as a function of binding energy and it has contributed from a background signal. The resonance peaks above the background are the characteristic of the bound states of the electrons in the surface atoms. Since  $\Phi_s$  cancels in the equation (2.2), the photoelectron energy is known and the  $\Phi_A$  is constant, the  $E_{kin}$  determines the  $E_B$  and vice versa. For calculating  $\Phi_A$  the energy scale is set to zero at the Fermi edge of the reference samples like Ag, or Ni or Au [94, 95]. This calibration results in  $\Phi_A$  equal to zero, and relate  $E_B$  and  $E_{kin}$  directly by the equation:  $E_{kin} = h\nu - E_B$ . Note that the above analysis is only valid for conducting samples where the energy of the Fermi level of the sample and analyzer is almost equal as depicted in

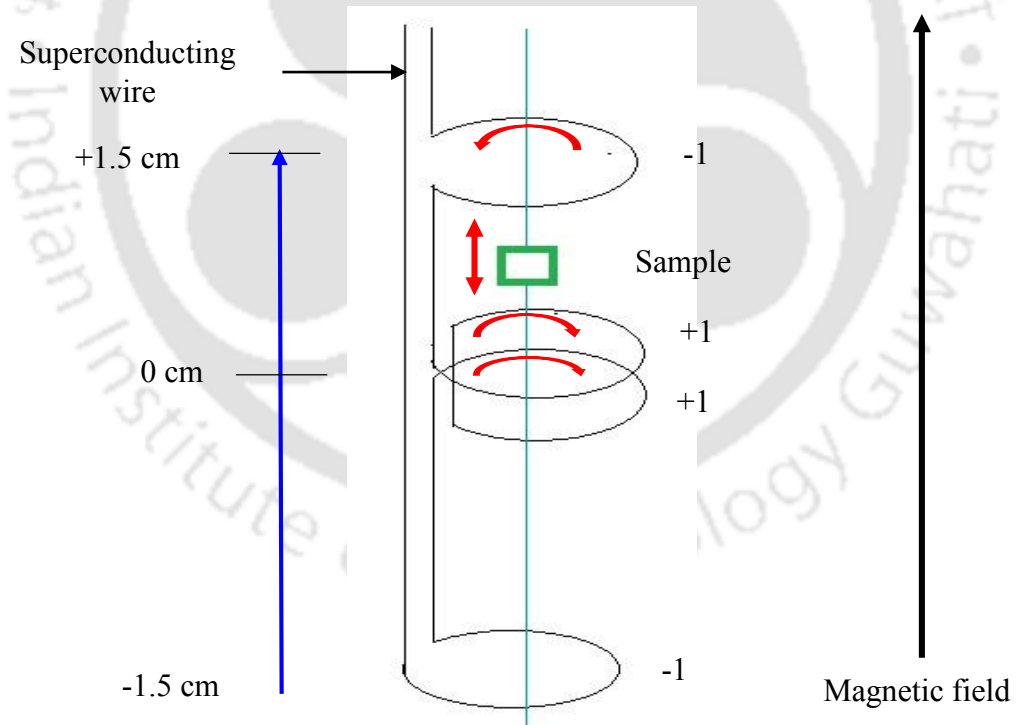
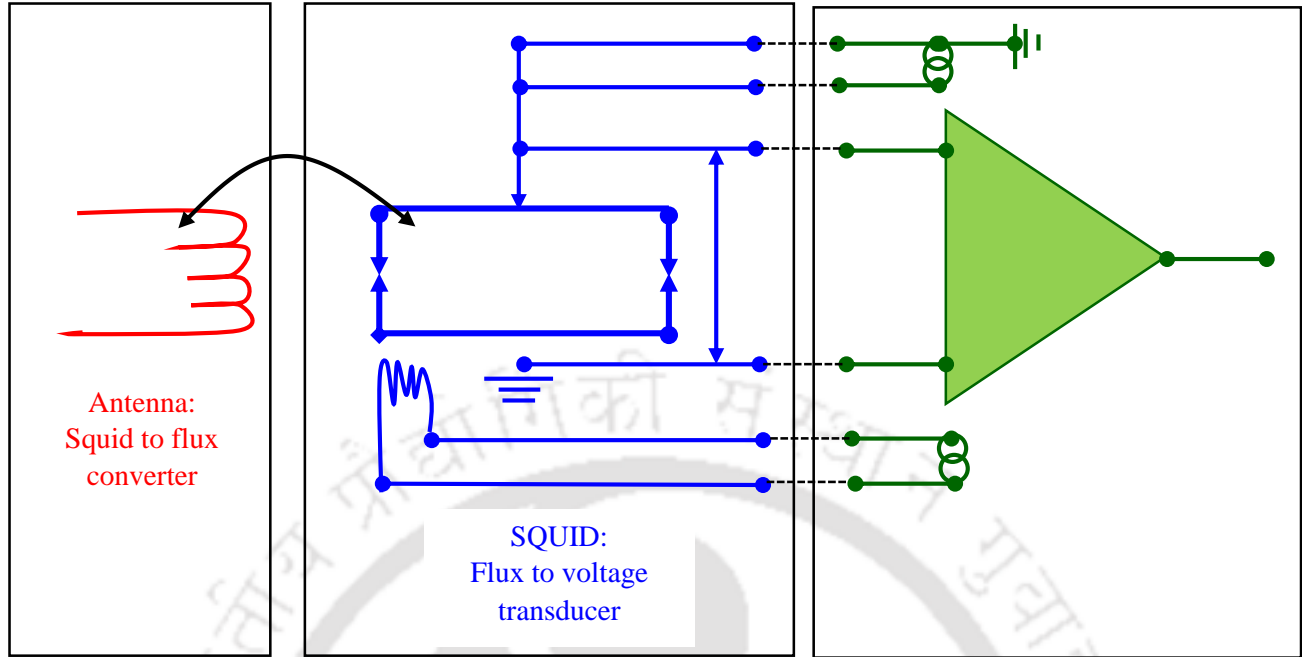
figure 2.3. In the case of insulators, the Fermi-level is not well defined due to charging effect and consequently a shift in the binding energy observed. In general, the following six features are observed in any XPS spectra [94].

- (a) *Sharp peaks*: due to photoelectrons created within the first few atomic layers (elastically scattered). These peaks constitute the main spectral feature which correspond to the particular element of interest.
- (b) *Multiplet splitting*: occurs when unfilled shells in atoms contain unpaired electrons.
- (c) *Satellites*: (shake-off and shake-up) are due to a sudden change in Coulombic potential as the photo-ejected electron passes through the valence band.
- (d) *Plasmons*: which are created by collective excitations of the valence band.
- (e) *Auger peaks*: produced by X-rays (transitions from L to K shell).
- (f) *Background*: A broad structure due to electrons from deeper in the solid which are inelastically scattered (reduced KE) forms the background.

In the present thesis, all the spectra were recorded by a dual source X-ray photoelectron spectroscope (Al-K $\alpha$  @ 1486.8 eV, Mg-K $\alpha$  @ 1253.6 eV) from VG-Microtech equipped with an ultrahigh vacuum ( $8 \times 10^{-8}$  Torr) chamber with pass energy of 100 eV was employed. The data were recorded from 0 to 1100 eV of binding and calibrated against the C-1s peak 284.5 eV.

### 2.2.4 DC & AC-Magnetization Measurements:

All the temperature (2 - 320 K) and magnetic field ( $\pm 7$ -9 Tesla) dependence of DC and AC magnetization measurements are performed using the superconducting quantum interference device (SQUID) based magnetometer from Quantum design. In particular, Magneto property Measurement system (MPMS) (7XL SQUID) was used [96]. The device may be configured as a magnetometer to detect extremely small magnetic fields small enough to measure the magnetic fields in living organisms using the Josephson junctions. The basic phenomena governing the operation of SQUID devices are flux quantization in superconducting loops and the Josephson-effect [97]. In 1962, B. D. Josephson showed that the electrical current density through a weak electric contact between two superconductors depends on the phase difference  $\Delta\phi$  of the two superconducting wave functions [98, 99]. Moreover, the voltage across the weak contact is interrelated with the time derivative of  $\Delta\phi$ . In a typical superconducting ring with one (known as RF-SQUID) or two (DC-SQUID figure 2.4) weak contacts,  $\Delta\phi$  is additionally influenced by the magnetic flux  $\Phi$  through this ring. Hence, such a structure can be used to convert magnetic flux into an electrical voltage which is the basic working principle of a SQUID magnetometer. When a sample moves up and down it produces an alternating magnetic flux in the pick-up coils. These coils together with a SQUID antenna transferring the magnetic flux from the sample to an RF-SQUID with high degree of accuracy of measuring the magnetic moment  $\sim 10^{-8}$  emu. The RF-SQUID act as a magnetic-flux to voltage converter. The variation in the voltage is proportional to the change in magnetic flux of the sample. The voltage is then magnified and read out by the magnetometer's electronics (figure 2.4). The principal components of this measurement system comprise the following aspects:



**Figure 2.4:** (a) Schematic diagram of the superconducting quantum interference device (SQUID) flux to voltage converter and (b) pick-up coil.

- (i) *Temperature control system:* Precision control of the temperature in the range 2 K to 400 K.
- (ii) *Magnet control system:* Current from a power supply is set to provide magnetic fields from zero to  $\pm 7$  Tesla.
- (iii) *Superconducting SQUID amplifier system:* The RF-SQUID detector is the heart of the magnetic moment detection system. It provides reset circuitry, auto-ranging capability, a highly balanced second-derivative sample coil array.
- (iv) *Sample handling system:* The ability to step and rotate the sample through the detection coils without transmitting undue mechanical vibration to the SQUID is of primary importance.
- (v) *Computer operating system:* All operating features of the MPMS are automated, computer control. The user interface at the PC console provides the option of working under standard sequence control, or diagnostic control which will invoke individual functions.

### 2.2.5 Physical Property Measurement System (PPMS):

The temperature and magnetic field dependence of specific-heat ( $C_P(T,H)$ ) of the bulk samples  $\text{Co}_2\text{SnO}_4$  and  $\text{Co}_2\text{TiO}_4$  were performed by means of a physical property measurement system (PPMS) from Quantum Design (Model 6000 PPMS). Furthermore, temperature dependence of pyroelectric current measurements and the high-field ( $\pm 14$  Tesla) magneto-dielectric measurements of  $\text{Mn}_3\text{O}_4$  system are also performed by the PPMS. Heat capacity is a very useful quantity and play a major role in many fields of physics and chemistry. From the heat capacity measurement of solid sample, one can get substantial information about the lattice properties, phase transitions, electronic, and even magnetic properties of the materials. Generally, the heat capacity measurements of any compound can be performed well below the Debye temperature, because it directly probes the electronic and magnetic energy levels of that material and hence allow comparison between theory and experiment. A very small piece of sample (usually  $\leq 10$  mg) is mounted on this platform for precise and fast measurements using a standard cryogenic grease or adhesive such as Apiezon N or H Grease (addenda). The heat capacity of the sample is determined by subtracting the addenda from the total heat capacity. Typically, heat capacity measurement involves some separate stages: first, the sample platform and puck (PPMS 12 pin format electronic connection) temperatures are stabilized at some initial temperature, after this the sample platform is elevated to a certain temperature. Next the temperature of the sample platform relaxes towards the puck temperature. The sample platform temperature is monitored during both heating and cooling cycles, providing the raw data of the heat capacity calculation. The sophisticated two-tau model is used to analyze the heat capacity of the sample [100, 101]. The two-tau model simulates the effect of heat flowing between the sample platform and sample, and also between the sample platform and puck. By optimizing the agreement between the experimental data and the two-tau model the heat capacity values along with other physical parameters are determined. In the two-tau model, the first time constant ( $\tau_1$ ) represents the relaxation time between the sample platform and the puck, and the second time constant ( $\tau_2$ ) represents the relaxation time between the sample platform and the sample itself. On the other

hand, magneto-dielectric measurements were performed using the impedance and gain phase analyzer from Agilent technologies (Model No- 4284 A) which was assembled with the low-temperature accessory of the PPMS.

### **2.2.6 AC-resistivity and Dielectric Permittivity Measurements:**

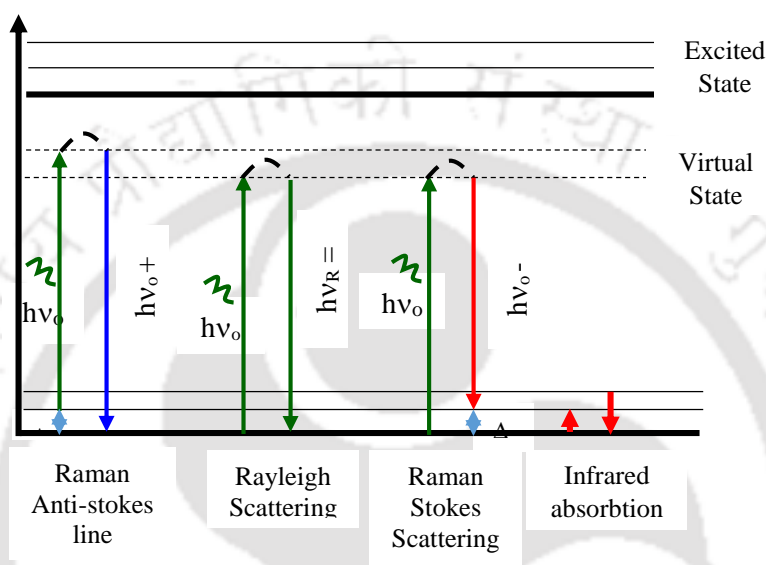
High frequency ( $100 \text{ Hz} \leq f \leq 20 \text{ MHz}$ ) ac-electrical resistivity and dielectric permittivity studies of  $\text{Co}_2\text{SnO}_4$  and  $\text{Co}_2\text{TiO}_4$  were performed between the temperatures 120 K and 570 K using the impedance and gain-phase analyzer from Novocontrol Alpha AN impedance analyzer with Quatro cryosystem. A pour-fill liquid nitrogen cryostat was assembled with the impedance analyzer to achieve the low-temperatures ( $-160^\circ\text{C}$ ), where as a home-made heater was designed to realize high temperatures. Sample holder from Novocontrol BDS 1200 based passive parallel plate ZG4 4-wire was used. The dielectric properties of the insulating spinels  $\text{Co}_2\text{SnO}_4$  and  $\text{Co}_2\text{TiO}_4$  are unknown in the literature until now, this aspect motivated us to study the ac-conductivity and dielectric behavior of these samples. Magnetic ceramic materials are of usual interest for practical applications such as thermistors, memristor and magneto-dielectric devices [102, 103].

### **2.2.7 Vibrational Excitations and Raman spectroscopy:**

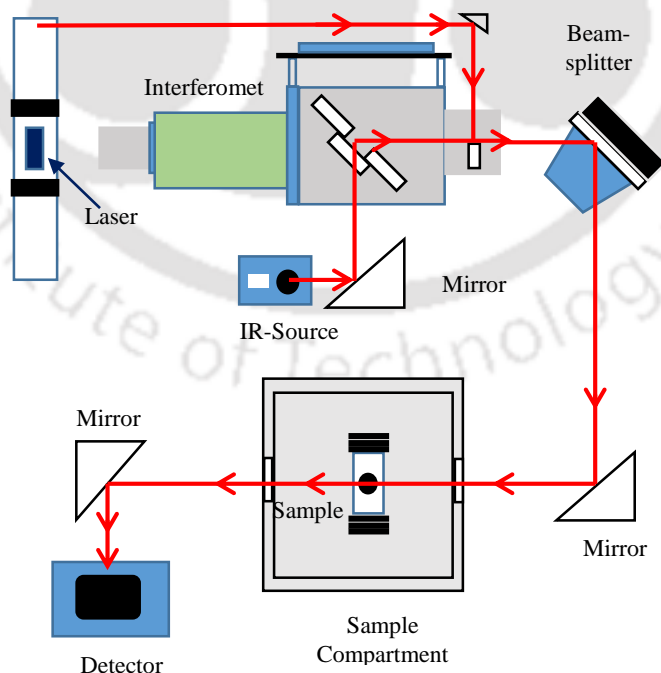
Raman spectroscopy probes molecular vibration of the sample and is a versatile technique for analysis of a wide range of samples. Qualitative analysis can be performed by measuring the frequency and intensity of scattered radiations [104, 105]. Raman spectroscopy is sensitive to the crystal structure, bonding, and chemical composition of the material and does not require any sample preparation [106]. In Raman spectroscopy, the monochromatic laser beam falls and interact with the molecule of the sample and scattered light is generated. Due to the inelastic scattering of monochromatic incident light with the atoms/molecules of the compound a shift in the frequency of output spectrum (scattered light) can be observed, based on such difference in the frequency Raman spectra can be classified either Stokes or Anti-stokes (figure 2.5). In case of Stokes: the frequency of incident radiation is higher than the frequency of the scattered radiation. If the frequency of incident radiation is lower than the frequency of the scattered radiation then such spectrum is known as Anti-stokes. However, if the scattered radiation frequency is equal to the frequency of incident radiation then such scattering is known as Rayleigh scattering (shown in figure 2.5). Stokes lines are more intense than anti-stokes lines. Hence stokes are used to measure the conventional Raman spectroscopy while anti-stokes bands are measured with fluorescing samples because fluorescence causes interference with Stokes bands. The magnitude of the Raman shift is independent of the wavelength of the incident radiation. Since Raman scattering due to water is low, water is used as an ideal solvent for dissolving liquid samples. Solid samples can directly mount on a glass substrate and perform the measurements by mean of the optical components (mirror, lens, sample cell) in Raman spectrophotometer [104, 105, 107]. In the present thesis, two different Raman spectrophotometers are used. The room temperature measurements are performed using LABRAM HR800 Raman spectrometric analyzer with an excitation wavelength of 488 nm of an Ar-ion laser. For low temperature Raman measurements (down to 25 K) a different

## Chapter 2: Experimental Techniques

Raman spectrophotometer (Jobin Yvon T64000) with wavelength 514 nm was used. This instrument is equipped with a dedicated heating/cooling sample stage (Linkam, THMS600). All the spectra were recorded in a backscattered geometry furnished with a 50× objective, an appropriate edge filter, and a Peltier-cooled charge-coupled device detector. An Ar<sup>+</sup> ion excitation laser source in a high-resolution dispersive geometry was used for these low-temperature micro-Raman measurements with  $\lambda = 514 \text{ nm}$  and an  $1800 \text{ mm}^{-1}$  grating. The spectral resolution of the system is  $1 \text{ cm}^{-1}$ . For high degree of positional accuracy, the grating was fixed during the entire temperature scan.



**Figure 2.5:** Energy level diagram of the Rayleigh and Raman Scattering.



**Figure 2.6:** Schematic diagram of the Fourier transform infrared spectrometer.

### 2.2.8 Fourier Transform Infrared Spectroscopy:

In past few years Fourier transform infrared spectroscopy (FTIR) is used as an important technique for material analysis. The term Fourier-transform infrared spectroscopy originates from the fact that a Fourier transform (a mathematical process) is required to convert the raw data into the actual spectrum. Basically, FTIR is the study of interaction of infrared radiation with matter as a function of photon frequency. It provides many valuable scientific information about the vibration and rotation of the chemical bonds and molecular structures, which are useful for analyzing and also identifying the materials. An infrared spectrum represents a finger-print of a compound with absorption peaks of certain vibrational frequencies of chemical bonds. In addition, the size of the peaks in the spectrum is a direct measure of the quantity of the material. With the invention of modern software algorithms, this infrared characterization technique becomes an excellent tool for quantitative analysis of the chemicals. Infrared spectroscopy generally measured in the wavenumber range  $4000\text{--}400\text{ cm}^{-1}$ . When a material is exposed to the infrared radiation, atoms/molecules absorbed the radiation at frequencies equivalent to their vibrational modes. The corresponding radiation absorbed by the atoms is recorded as a function of frequency of the electromagnetic radiation which further analyze to identify the functional group and/or stretching of the chemical bonds of the investigated compounds. Figure 2.6 represents the schematic diagram of a FTIR spectrometer. The basic ingredients of the instruments are:

- (a) *Source*: Infrared energy is emitted from a glowing black-body source. The beam allowed to pass through an aperture to control the amount of energy falling on the sample.
- (b) *Interferometer*: After passing through the aperture the beam enters into the interferometer. The interferometer guides the beam via a beam-splitter and mirror to incident exactly on the sample.
- (c) *Sample*: A small amount of sample was first diluted with 150 mg of vacuum-dried IR-grade potassium bromide (KBr) powder and subjected to a pressure of 39.2 bar. After that the sample placed in the sample-holder and it is exposed by the incident beam. In this process, specific frequencies of energy are absorbed which are characteristic of the sample.
- (d) *Detector*: The beams scattered from the sample finally passes to the detector for final measurement. These detectors are specially designed to measure the special interferogram signal.
- (e) *Computer*: The measured signal is digitized and sent to the computer where the Fourier transformation takes place. The final infrared spectrum is then presented to the user for further interpretation.

In the present thesis work, FTIR spectra of all the compounds were recorded using a Perkin-Elmer 180 Spectrometer in the wavenumber range  $4000\text{ cm}^{-1}$  (far-IR) -  $400\text{ cm}^{-1}$  (IR) with the spectral resolution of  $\pm 2\text{ cm}^{-1}$ .

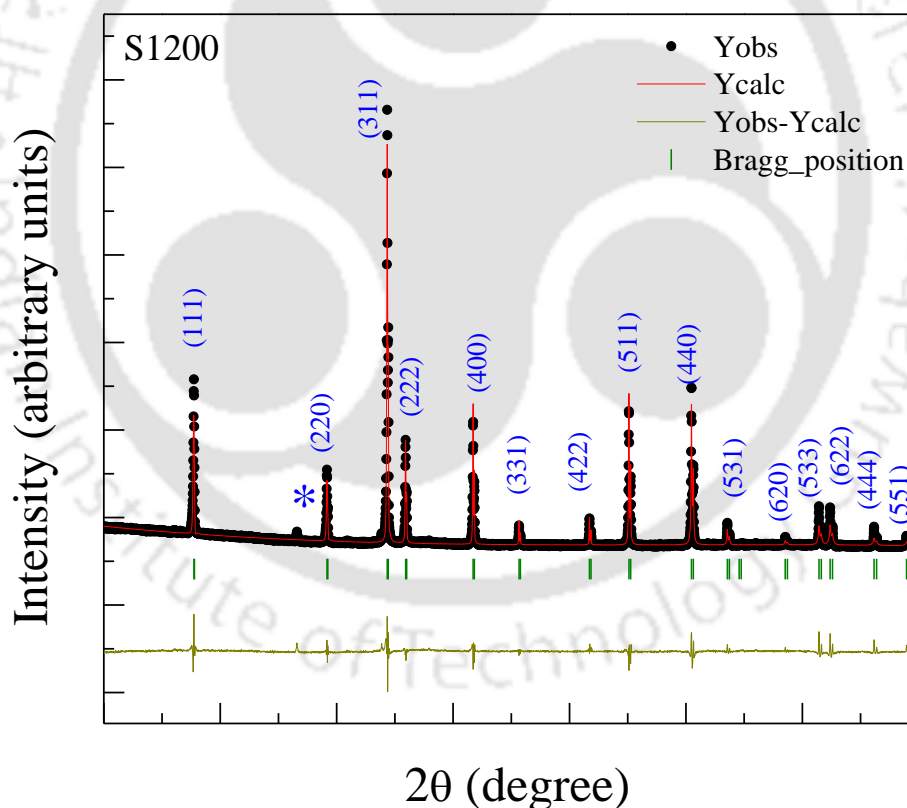
Nature of Magnetic Ordering in  $\text{Co}_2\text{SnO}_4$ **3.1 Introduction:**

This chapter deals with the synthesis and characterization of the Cobalt-Orthostannate, ( $\text{Co}_2\text{SnO}_4$ ) polycrystalline system with special emphasis on the role of magnetic dilution on the long-range ordering.  $\text{Co}_2\text{SnO}_4$  possess inverted cubic spinel crystal structure ( $[\text{Co}^{2+}]_A[\text{Co}^{2+}\text{Sn}^{4+}]_B\text{O}_4$ ) with two divalent cobalt ions  $[\text{Co}^{2+}(3d^7)]$  occupied in two-different sublattice (tetrahedral A and octahedral B sites) [81, 108, 109]. Earlier studies reveal that  $\text{Co}_2\text{SnO}_4$  exhibits ferrimagnetic properties due to the unequal magnetic moments of  $\text{Co}^{2+}$  ions in A- and B-sublattices  $[\uparrow M_A \neq M_B \downarrow]$  [57]. In 1976, Hermon *et al.* first reported that,  $\text{Co}_2\text{SnO}_4$  undergoes a long-range ferrimagnetic to paramagnetic transitions at Néel temperature  $T_N \sim 44 \pm 2$  K [81]. These authors also reported that in the limit  $T \rightarrow 0$  K, the nearest neighbor molecular field constant  $N_{AB}$  is antiferromagnetic, whereas, the next-nearest neighbor molecular field constant  $N_{AA}$  and  $N_{BB}$  is ferrimagnetic in nature [81]. On the other hand, later studies by Strooper *et al.* reported that all the three exchange constant are antiferromagnetic in nature with different magnitude of magnetic moments of  $\text{Co}^{2+}$  in the A and B-sublattices [82]. In single crystal  $\text{Co}_2\text{SnO}_4$ , Sagerdo *et al.* observed a strong irreversibility below  $T_N$  in both zero-field cooled (ZFC) and field-cooled (FC) magnetization curves [83]. The non-magnetic  $\text{Sn}^{4+}$  ions essentially randomize the cationic distribution in the B-site which may break the octahedral crystal field symmetry. As a result, the system possesses frustrated magnetic behavior along with short range spin-glass ordering and magnetic training effect [83]. Srivastava *et al.* observed two peak behavior in the ac-susceptibility measurements ( $\chi_{ac}$  versus T) of  $\text{Co}_2\text{SnO}_4$  polycrystals [108]. It was believed that the second peak in  $\chi_{ac}$  versus T curve indicated a separate freezing of spins located at A and B-sites [108]. As discussed earlier in the introduction chapter, such kind of peak-splitting in  $\chi_{ac}$ -T is associated with the semi-spin-glass behavior predicted by Villian [40]. Such interesting behavior along with enthralling physics, originated from the different magnetic moments at A and B sites ( $\mu_A \neq \mu_B$ ) motivated us to work on this compound. Not only from the fundamental physics perspective, but from the applications point-of-view  $\text{Co}_2\text{SnO}_4$  has attracted immense attention recently due to its excellent catalytical properties and its positive temperature coefficient of resistance which make it a useful material for thermistor devices [81, 108, 109]. Therefore, we extensively investigated its physical properties like crystal structure, magnetic, electrical, specific heat which gives insights into its local atomic environment. Such properties are discussed extensively in this chapter along with a detailed synthesis procedure.

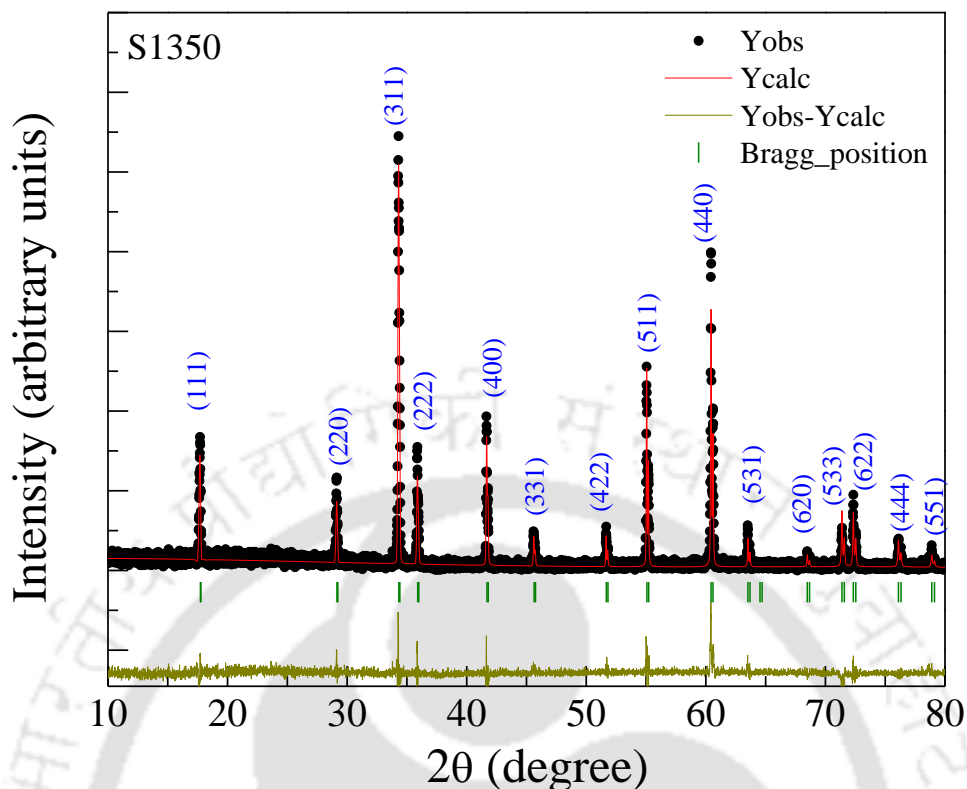
**3.2 Experimental Details:**

The polycrystalline bulk-grain size  $\text{Co}_2\text{SnO}_4$  was prepared by standard solid-state reaction method using stoichiometric amounts of  $\text{Co}_3\text{O}_4$  (Alfa Aesar, purity 99.99%) and  $\text{SnO}_2$  (Alfa Aesar, purity 99.99%) as the starting

materials. Appropriate amount of these two oxides was grounded in an agate mortar for 4 h with the help of a pestle. This mixed powder was first calcined at  $800^\circ\text{C}$  for 24 h in air and then pressed into 13 mm pellets using a hydraulic press with maximum load of 5 tons per  $\text{cm}^2$ . These pellets were then heat-treated at high temperatures ( $1200^\circ\text{C}$ ) for long time duration 48 h in air (sintering) with precise heating and cooling rate ( $3^\circ\text{C}/\text{min}$ ). Inter-diffusion of the chemical species occurs at these higher temperatures which creates an environment for grain growth and finally leads to the formation of strong solid material. This sample sintered at  $1200^\circ\text{C}$  is given a code: S1200. A second method was also implemented to prepare the  $\text{Co}_2\text{SnO}_4$  by ball-milling method. In this case the precursors  $\text{Co}_3\text{O}_4$  and  $\text{SnO}_2$  were first ball-milled using Retsch (PM-100 from FRITSCH GmbH) at 100 revolutions per minute for 2 h using zirconia jar and balls with ethanol as the milling media. After drying the resulting powder at  $120^\circ\text{C}$  for 24 h in air, this sample, was hydraulically pressed at pressure of 110 MPa in a stainless-steel die to form of cylindrical pellet of size 13 mm followed by sintering at  $1350^\circ\text{C}$  for 8 h in air using slower heating and cooling rates. This sample was named as S1350.



**Figure 3.1:** The X-ray diffraction pattern (dotted symbols) together with the Rietveld refined data (red line) of  $\text{Co}_2\text{SnO}_4$  bulk samples sintered at  $1200^\circ\text{C}$  (S1200) in air. The asterisk mark shows the position of the  $\text{SnO}_2$  secondary peak. Vertical lines represent the Bragg positions and the bottom line represents the difference between the intensities of the observed (Yobs) and calculated (Ycalc) pattern.



**Figure 3.2:** The X-ray diffraction pattern (scattered circular symbols) together with the Rietveld refined data (red line) of  $\text{Co}_2\text{SnO}_4$  bulk samples sintered at  $1350^\circ\text{C}$  (S1350) in air. Vertical lines represent the Bragg positions and the bottom line represents the difference between the intensities of the observed (Yobs) and calculated (Ycalc) pattern.

### 3.3 Results and Discussion:

#### 3.3.1 Structural Characterization:

The X-ray diffractogram recorded at room temperature using  $\text{Cu-K}\alpha$  ( $\lambda = 1.5406 \text{ \AA}$ ) along with the Rietveld refinement data (performed by FullProf program) of both S1200 and S1350 samples are shown in figures 3.1 and 3.2. The Miller-Indices of planes of these patterns belongs to the cubic spinel family with and space group  $Fd-3m$  (227) and lattice parameter  $a = 8.637(3) \text{ \AA}$  for S1200. The asterisk mark shown in the figure 3.1 is corresponding to the peak due to unreacted non-magnetic  $\text{SnO}_2$ . The weight % of this secondary phase present in the major phase of  $\text{Co}_2\text{SnO}_4$  was quantified using the following expression [110].

$$W_{\text{SnO}_2} = \left[ \frac{1}{\left\{ 1 + 1.265 \left( \frac{I_{\text{Co}_2\text{SnO}_4}}{I_{\text{SnO}_2}} \right) \right\}} \right] \times 100 \dots (3.1)$$

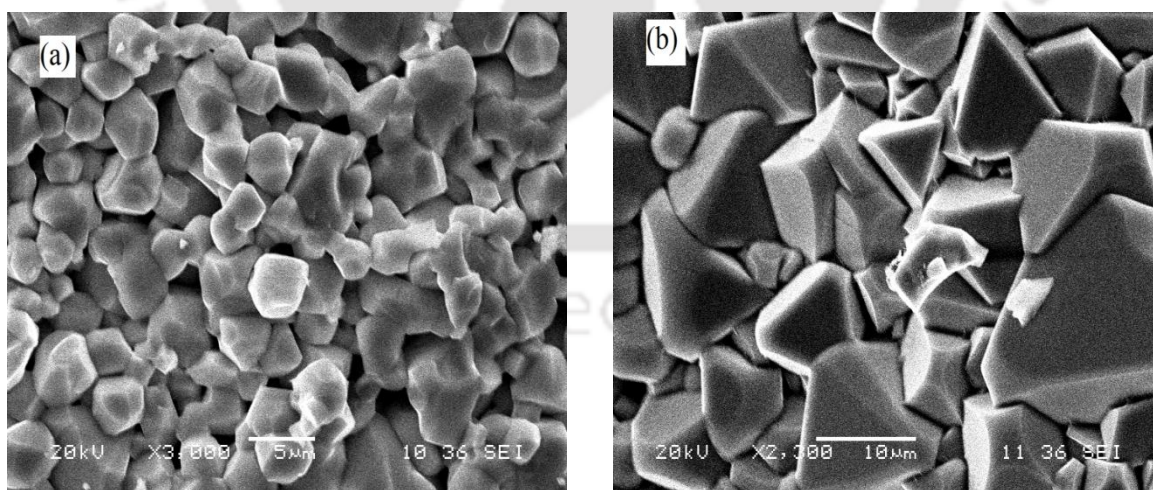
where  $W_{\text{SnO}_2}$  indicates the weight fraction of the  $\text{SnO}_2$  phase, and  $I_{\text{SnO}_2}$  and  $I_{\text{Co}_2\text{SnO}_4}$  represents the strongest X-ray diffraction line intensities of the  $\text{SnO}_2$  and  $\text{Co}_2\text{SnO}_4$ , respectively. The intensity ratio  $I_{\text{Co}_2\text{SnO}_4}/I_{\text{SnO}_2}$  is independent of variations in diffractometer. In the present case, intensities of (311) peak for  $\text{Co}_2\text{SnO}_4$  phase and (110) peak for

**Table 3.1:** The list of lattice parameters ( $a = b = c$ ), bond lengths and bond angles of S1200 and S1350 samples. (The interaxial angles  $\alpha = \beta = \gamma = 90^\circ$ ).

System ( $\text{Co}_2\text{SnO}_4$ )	Lattice Parameter	Bond Length		Bond Angle	
		A-O	B-O	A-O-B	B-O-B
S1200	$8.45 \pm 0.01 \text{ \AA}$	$1.92 \pm 0.011 \text{ \AA}$	$2.09 \pm 0.017 \text{ \AA}$	$123.68^\circ \pm 0.62^\circ$	$91.95^\circ \pm 0.48^\circ$
S1350	$8.66 \pm 0.02 \text{ \AA}$	$1.88 \pm 0.02 \text{ \AA}$	$2.16 \pm 0.021 \text{ \AA}$	$125.01^\circ \pm 0.65^\circ$	$90.37^\circ \pm 0.45^\circ$

$\text{SnO}_2$  were the maximum intense peaks. Using the above equation, we found that  $\sim 1.47 \text{ wt\%}$  of  $\text{SnO}_2$  present in the 98.53% of  $\text{Co}_2\text{SnO}_4$  matrix.

In order to avoid the formation of  $\text{SnO}_2$  phase we sintered the sample at higher temperature  $\sim 1350^\circ\text{C}$ . The diffraction pattern shown in figure 3.2 is also consistent with the standard cubic spinel phase with space group  $Fd-3m$  (227) without any signature of  $\text{SnO}_2$ . However, the lattice parameter obtained for S1350 is  $a = 8.657(3) \text{ \AA}$  which is slightly higher than that of S1200. Such variation in the lattice parameter is generally associated with the variation in the bond lengths and angles caused by the higher sintering temperature. Table-3.1 clearly summarizes the bond lengths and bond angles of both S1200 and S1350 obtained from the refinement process. It is evident that the average bond length (B-O) between the oxygen ion and elements present in the octahedral sites (B-O) of S1350 is higher than that in S1200 while the reverse is true for the tetrahedral sites (A-O). Whereas an opposite trend was observed in the case of bond-angles (A-O-B and B-O-B).



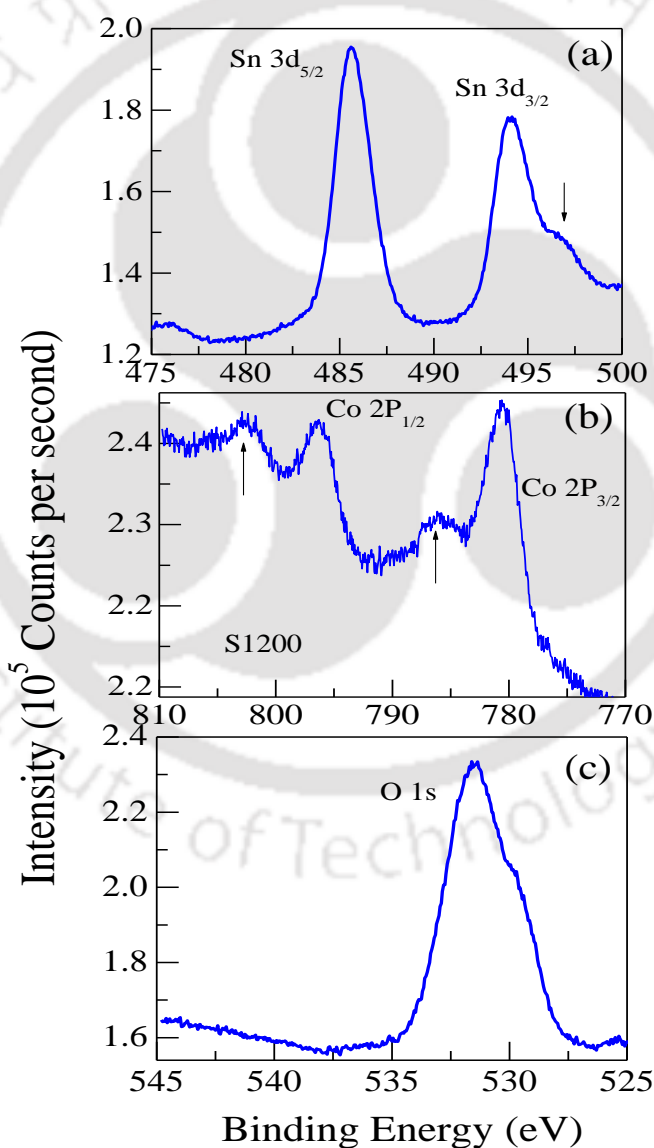
**Figure 3.3:** Field Emission Scanning Electron (FESEM) Micrograph of  $\text{Co}_2\text{SnO}_4$  bulk samples sintered at (a)  $1200^\circ\text{C}$  (S1200) and  $1350^\circ\text{C}$  (S1350) in air.

### 3.3.2 Morphology and Microstructure Analysis:

Figure 3.3 shows the micrographs of both S1200 (a) and S1350 (b) recorded using a field emission scanning electron microscope (FESEM) under secondary electron mode. These FESEM images show the formation of polygonal shape of micro-grains. The average grain sizes for S1200 and S1350 samples are coming out to be  $\sim 3.73 \mu\text{m}$  and  $\sim 6.47 \mu\text{m}$ , respectively.

### 3.3.3 X-ray Photoelectron Spectroscopy (XPS):

For a detailed understanding of the electronic state of the elements present in  $\text{Co}_2\text{SnO}_4$ , XPS measurements were performed using  $\text{Al-K}\alpha$  X-rays as source. Figure 3.4 shows the photoelectron intensity versus binding energy of the Sn-3d, Co-2p and O-1s spectra. The sharp peaks at 485.65 and 494.8 eV and a weak shoulder at 496.75 eV



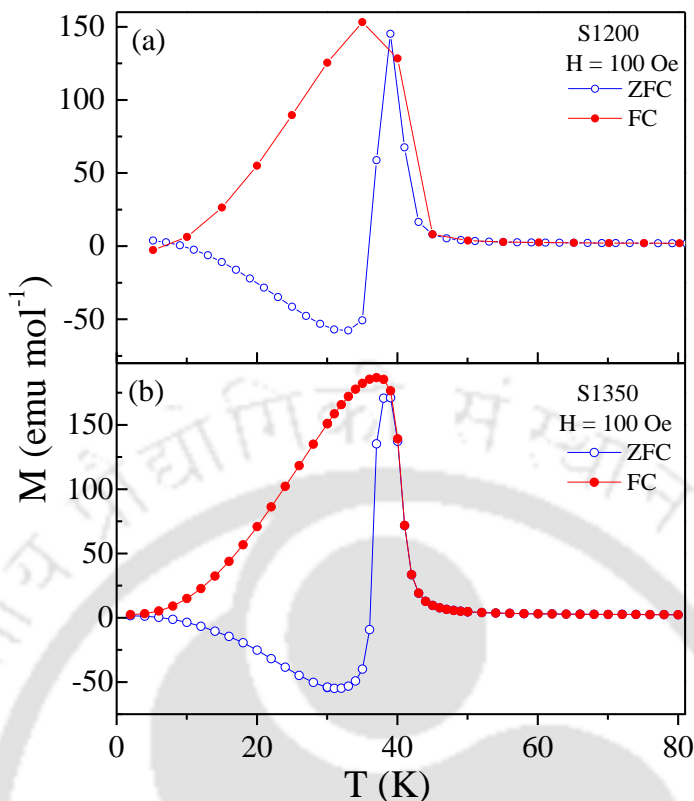
**Figure 3.4:** The X-ray-photoemission spectra of (a) Sn-3d, (b) Co-2p and (c) O-1s peaks in the S1200 sample.

in figure 3.4(a) are characteristics of the  $\text{Sn}^{4+}$  state [111, 112]. The XPS spectra of 'Co' shows two major peaks centered at 780.6 and 796.3 eV with satellite peaks at 786.15 and 802.4 eV. It is known that both divalent and trivalent cobalt cations ( $\text{Co}^{2+}$  and  $\text{Co}^{3+}$ ) exhibit similar binding energy peaks in XPS with the peak near 780 eV identified with the  $2p_{3/2}$  level and peak near 796 eV identified with the  $2p_{1/2}$  level. However, the energy splitting  $\Delta E$  of the two levels due to spin-orbit coupling is different for the  $\text{Co}^{2+}$  and  $\text{Co}^{3+}$  configurations with  $\Delta E = 15.0$  eV for  $\text{Co}^{3+}$  and  $\Delta E = 15.7$  eV for  $\text{Co}^{2+}$  [112 - 114]. From the data in figure 3.4(b), we get  $\Delta E = 15.7$  eV, characteristic of  $\text{Co}^{2+}$ . In addition, the two weaker satellite peaks observed here are usually absent in systems with a  $\text{Co}^{3+}$  electronic state. Therefore, the above XPS studies confirmed the presence of  $\text{Co}^{2+}$  and  $\text{Sn}^{4+}$  states in  $\text{Co}_2\text{SnO}_4$ . Finally, figure 3.4(c) shows an intense peak at 531.5 eV due to bonded lattice oxygen with the weak shoulder at 529.35 eV due to the surface oxygen [112 - 116].

### **3.3.4 Magnetization Studies:**

#### **(a) Temperature Dependence DC-Magnetization and AC-Susceptibility:**

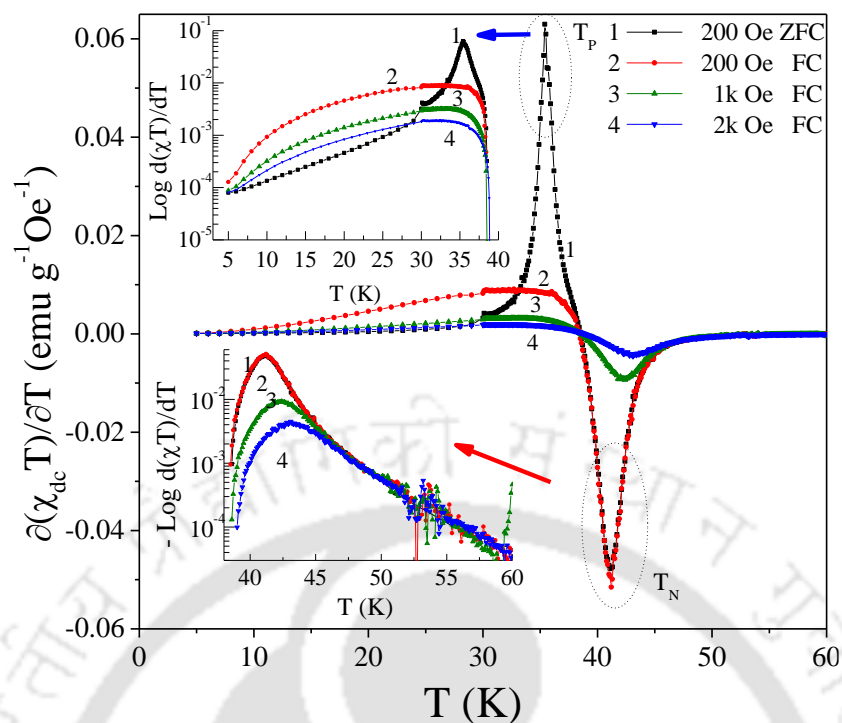
Figure 3.5 depicted the temperature dependence of the magnetization  $M(T)$  of both S1200 and S1350 sample measured under zero-field cooled (ZFC) and field-cooled (FC) conditions at an external magnetic field  $H_{dc}$  of 100 Oe for  $T < 80$  K. In ZFC mode, first the sample was cooled to 2 K in absence of magnetic field from a temperature ( $T$ ) much above its ferrimagnetic Néel temperature  $T_N$  and the magnetic-field is applied at 2 K and then the data is measured during warming. In FC condition, the sample was cooled to 2 K in presence of a static magnetic-field from a temperature much above its  $T_N$  and the magnetization is measured again while warming the sample by keeping the same magnetic-field. Both the magnetization curves  $M_{ZFC}$  and  $M_{FC}$  display a characteristic cusp across 38.1 K with strong irreversibility below this cusp. In order to probe the exact magnetic ordering temperatures, we calculated the derivative of the product of  $T$  and magnetic susceptibility ( $\chi_{dc} = M/H_{dc}$ ), i.e.  $(\partial(\chi_{dc}T)/\partial T)$  and plotted as a function of  $T$ . Figure 3.6 depicts temperature variation of  $\partial(\chi_{dc}T)/\partial T$  for S1200 sample. It is well known that, the temperature variation of  $\partial(\chi_{dc}T)/\partial T$  is analogous to the temperature variation of the specific-heat  $C_p(T)$  in the systems which shows antiferromagnetic variations [117, 118]. From the Curie-Weiss law one can write  $\partial(\chi T)/\partial T = -C\theta/(T-\theta)^2$ , which will give a negative minimum at  $T = \theta$  and for negative values of ' $\theta$ ' the equation  $\partial(\chi T)/\partial T$  gives a positive maximum as observed in figure 3.6 [77]. This exercise leads to the determination of the  $T_N \sim 41$  K and the second transitions  $T_P \sim 35.4$  K. Similar type of analysis provide the existence of two transitions for S1350 sample i.e.,  $T_N = 41$  K and  $T_P = 37.1$  K ( as depicted in figure 3.7). In general, the second transition  $T_P$  signify the presence of either blocking phenomenon or spin-glass state in the  $\text{Co}_2\text{SnO}_4$  system. Since the average grain sizes observed from the FESEM micrograph are in the  $\mu\text{m}$  range,  $T_P$  cannot be attributed to the blocking phenomena as the grain size in this case should be of the order of nm ( $< 30$  nm). The data in the inset of figure 3.6 shows that with increase in  $H_{dc}$  from 200 Oe to 2 kOe,  $T_N$  shifts towards the higher value whereas  $T_P$  shifts towards the lower value, which is a typical signature of spin-glass transitions. Similar behavior observed in S1350 also (as shown in the inset figure 3.7). The decrease of magnetization with decrease in temperature as seen in



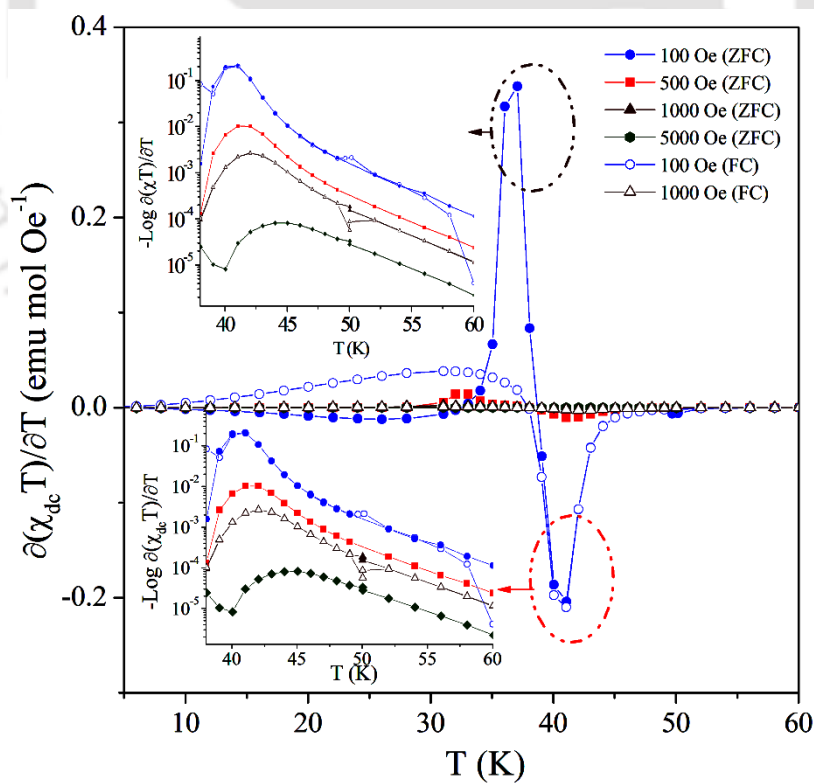
**Figure 3.5:** Temperature dependence of dc-magnetization  $M(T)$  measured under ZFC and FC ( $H@100$  Oe) conditions for both  $\text{Co}_2\text{SnO}_4$  bulk samples (a) sintered at  $1200^\circ\text{C}$  (S1200) and (b)  $1350^\circ\text{C}$  (S1350).

figure 3.5 suggests that the temperature dependence of A-sublattice magnetization  $M(A)$  is different from that of B-sublattice magnetization  $M(B)$  since the measured magnetization for a collinear ferrimagnet is proportional to the magnitude of the difference between  $M(A)$  and  $M(B)$ . The observed variation of  $M$  versus  $T$  below  $T_N$  in figure 3.5 is quite consistent with the expected variations in ferrimagnets with different temperature dependences of  $M(A)$  and  $M(B)$ .

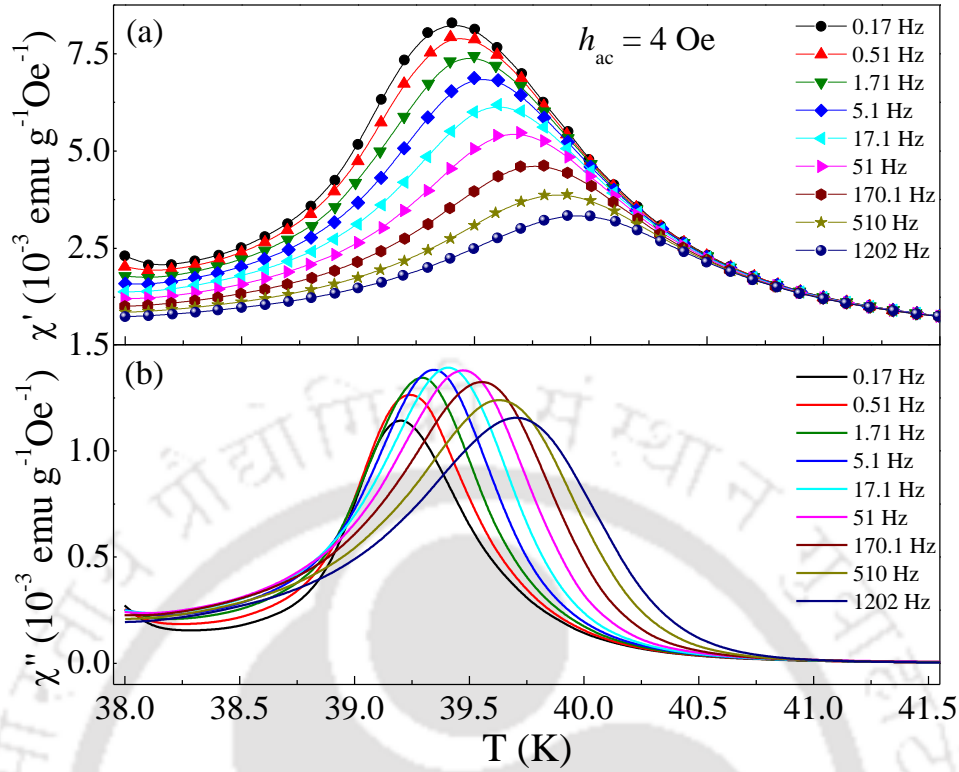
Figures 3.8 and 3.9 show the temperature dependence of the real-component  $\chi'(T)$  and imaginary component  $\chi''(T)$  of ac-magnetic susceptibility  $\chi_{ac}(T)$  recorded using different measuring frequencies ( $f$ ) ranging from 0.17 to 1202 Hz and under zero dc-bias field for the samples S1200 and S1350, respectively. It is well known that the dynamic susceptibility is an important phenomenon to understand the nature of magnetism in diluted systems such as  $\text{Co}_2\text{SnO}_4$  below  $T_N$  where the short-range ordering arises again due to the competing interactions. In both the samples S1200 and S1350 the data was recorded from 30 K to 50 K with very close interval  $\Delta T = 0.1$  K in presence of dynamic ac-magnetic field amplitude  $h_{ac} \sim 4$  Oe. One can clearly notice the frequency dispersion of cusp in both  $\chi'(T)$  and  $\chi''(T)$  for both S1200 and S1350. Such shift of peak position towards higher temperatures in both  $\chi'(T)$  and  $\chi''(T)$  clearly signify the existence of the glassy behavior in the investigated systems [42, 67, 119]. In



**Figure 3.6:** The differential susceptibility plots ( $\partial(\chi_{dc}T)/\partial T$ ) versus  $T$  of S1200 sample at various external fields  $H = 200$  Oe, 1 kOe, and 2 kOe. The insets depict  $\partial(\chi_{dc}T)/\partial T$  plotted with a logarithmic scale to show the variation in the peak clearly.

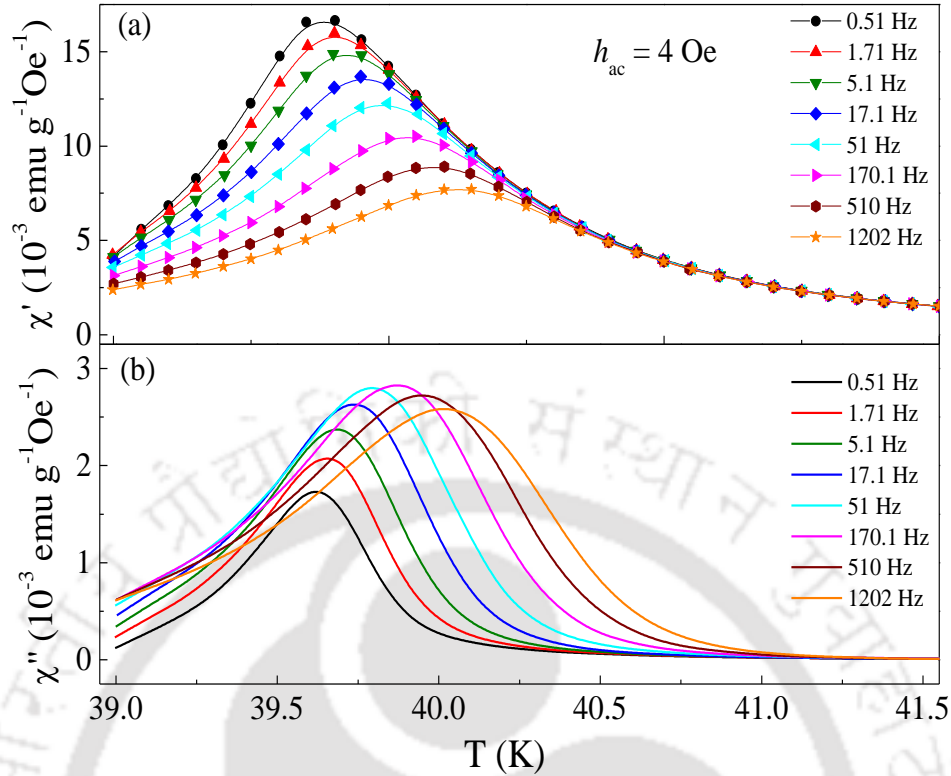


**Figure 3.7:** Plots of  $\partial(\chi_{dc}T)/\partial T$  versus  $T$  plots of S1350 sample at various external fields  $H = 100, 500, 1000$  and  $5000$  Oe. The insets show the  $\partial(\chi_{dc}T)/\partial T$  in logarithmic scale to show the variation in the peak clearly.



**Figure 3.8:** Temperature dependence of the (a) real-component  $\chi'(T)$  and (b) imaginary-components  $\chi''(T)$  of ac-magnetic susceptibility for S1200 recorded using different measuring frequencies under zero-dc bias field with the amplitude of dynamic magnetic-field  $h_{ac} = 4$  Oe.

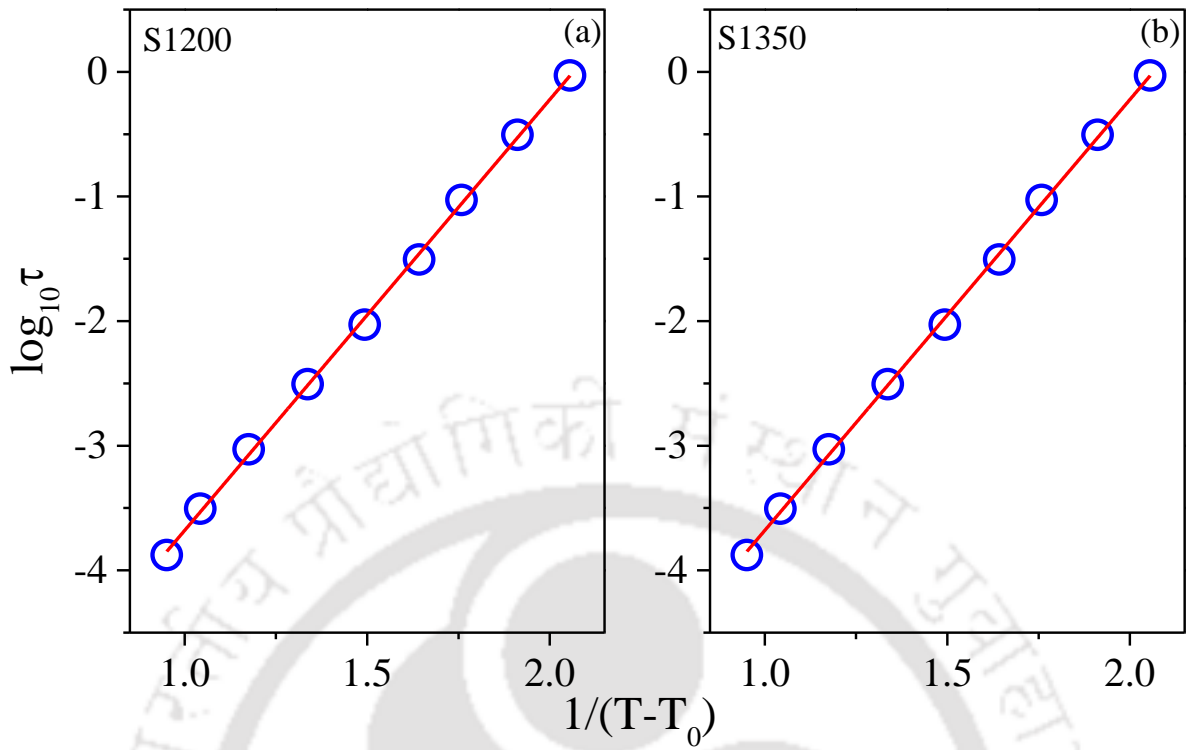
order to examine such spin-glass behavior in detail, we analyzed the data using two dynamic scaling laws – (i) Vogel-Fulcher law for interacting particle system and (ii) Power law describing the critical slowing down in phase transition [67]. Vogel-Fulcher law can be expressed as:  $\tau = \tau_0 \exp(E_a/k_B(T - T_0))$ , where  $\tau = 1/2\pi f$ ,  $\tau_0$  is the relaxation time constant,  $T_0$  is a measure of the interparticle interaction strength,  $k_B$  is the Boltzmann constant, and  $E_a$  is an activation energy parameter. The best fits using the Vogel-Fulcher law (shown in figure 3.10) yields the value  $\tau_0 = 6.3 \times 10^{-14}$  s ( $7.3 \times 10^{-8}$  s) and  $T_0 = 38$  K (39.3 K) for S1200 (S1350) samples, respectively. In the above fitting analysis we obtained a very large value of  $\tau_0$  for S1350 sample. Such large value of  $\tau_0$  has been observed in other system as well, such as CuMn,  $\text{Y}_{0.7}\text{Ca}_{0.3}\text{MnO}_3$  which indicates the presence of interacting magnetic spin clusters of significant sizes in the system [120, 121]. We, believe that the spin clusters arise from a short range order which occurs due to the competition between ferrimagnetism and magnetic frustration in the system. On the other hand, the Power-law can be represented as:  $\tau = \tau_0 ((T/T_g) - 1)^{-z\nu}$ , where  $T_g$  is the freezing temperature,  $\tau_0$  is related to the relaxation of the individual cluster magnetic moment and  $z\nu$  is a critical exponent. Figure 3.11 shows the least square fit of the data using Power-law relation. An equally good fit as the Vogel-Fulcher law was obtained with  $T_g = 39.1$  K (39.6 K),  $\tau_0 = 1.7 \times 10^{-22}$  s ( $1.4 \times 10^{-15}$  s) and  $z\nu = 12.6$  (6.4) for



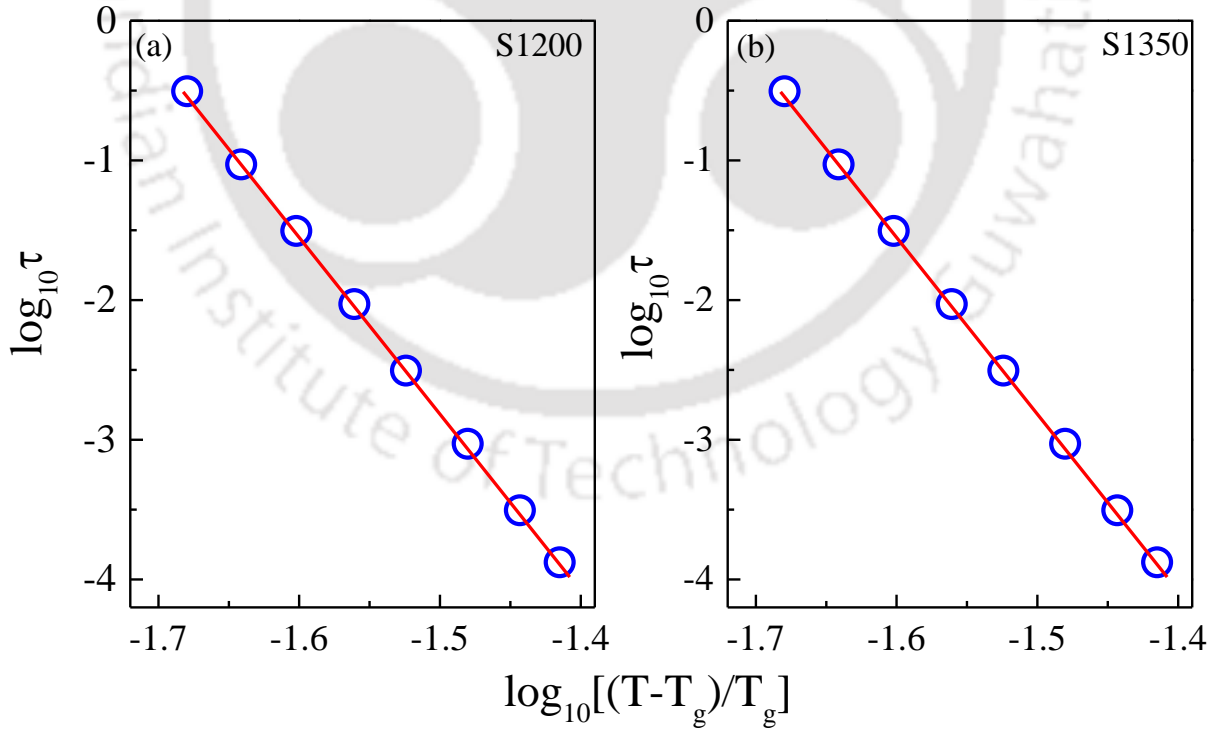
**Figure 3.9:** Temperature dependence of the (a) real-component  $\chi'(T)$  and (b) imaginary-components  $\chi''(T)$  of ac-magnetic susceptibility for S1350 recorded using different measuring frequencies under zero-dc bias field with the amplitude of dynamic magnetic-field  $h_{ac} = 4 \text{ Oe}$ .

S1200 (S1350) samples, respectively. For an ideal spin-glass system the  $zv$  value should lie between 4 and 12 [67]. However, we obtained a little high value for S1200 system which is quite unphysical for spin-glass system, but very small difference between  $T_o$  and  $T_g$  suggest the system is close to a spin-glass transition. It is important to mention that while fitting the data for the sample S1200 to the power law, we could obtain more than one set of parameters giving almost equally good fits (the value of goodness of fit  $R^2$  changing after the 5<sup>th</sup> decimal place). However, for the pure sample (S1350 without any  $\text{SnO}_2$  impurity), the data could be fitted using a set of parameters which gave an unambiguous best fit.

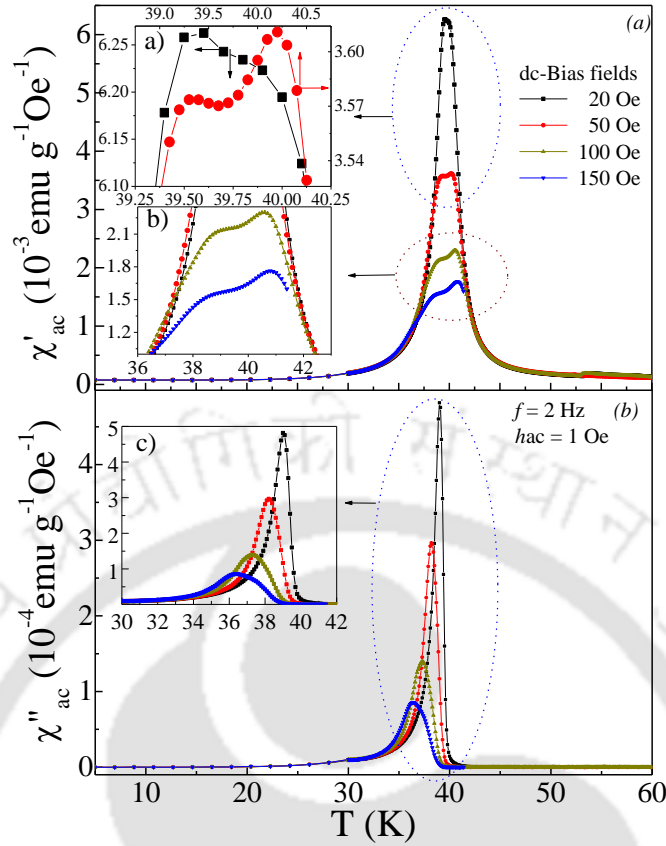
For further understanding the nature of magnetism below  $T_N$ , we measured the ac-magnetic susceptibility superimposed with various dc-bias fields ( $H_{dc}$ ). Figure 3.12(a) and 3.12(b) represent the temperature dependence of  $\chi'$  and  $\chi''$  measured at a constant driving frequency ( $f = 2 \text{ Hz}$ ) and the ac-field-amplitude  $h_{ac} = 1 \text{ Oe}$  superimposed with external dc-bias field ( $0 \text{ Oe} \leq H_{dc} \leq 200 \text{ Oe}$ ) for S1200 system. The in-phase ac-susceptibility ( $\chi'$ ) shows two-peak behavior with their splitting increases with increasing  $H_{dc}$ . On the other hand,  $\chi''$  versus  $T$  curves show a single peak with decreasing intensity and shift towards lower temperatures with increase in  $H_{dc}$ . Since, the out of phase susceptibility is related to the transverse spin component. These observations reveal the co-existence of ferrimagnetism of longitudinal spin component along with the freezing of transverse spin



**Figure 3.10:** The best fit of the relaxation times to the Vogel–Fulcher law for (a) S1200 and (b) S1350 sample.

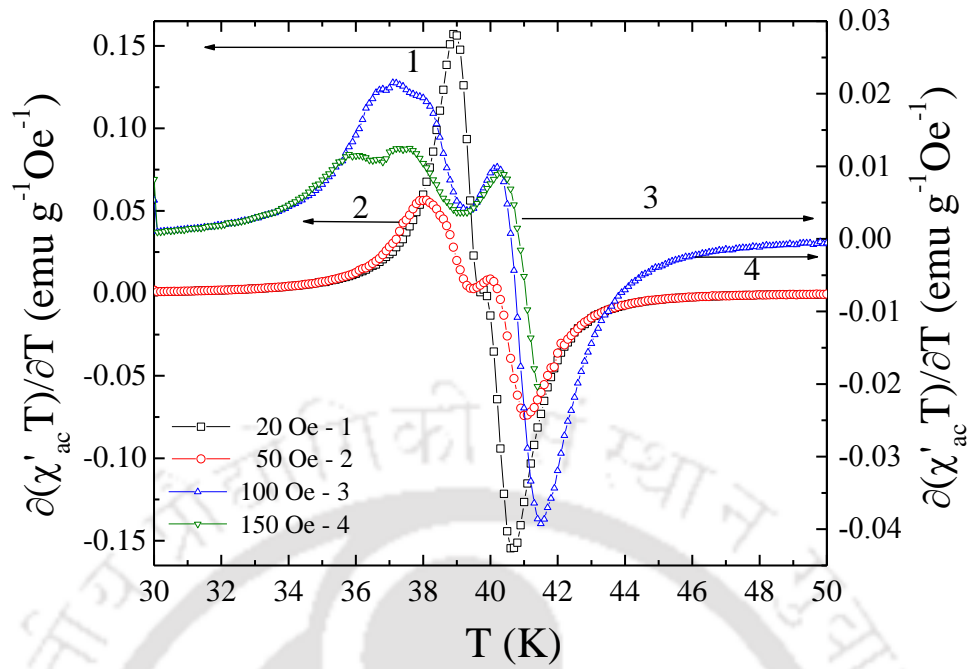


**Figure 3.11:** The best fit of the relaxation times to the Power–law for (a) S1200 and (b) S1350 sample.

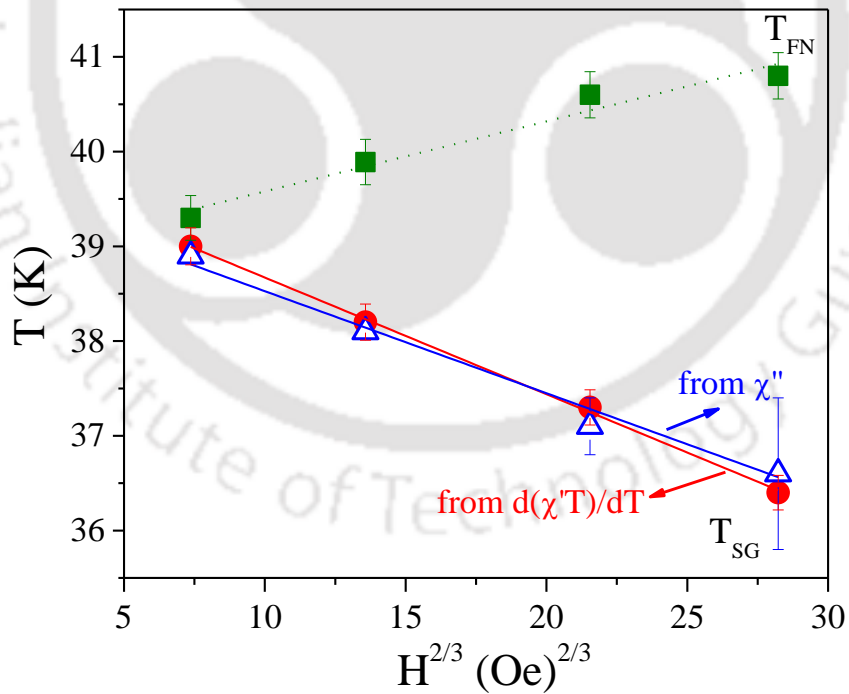


**Figure 3.12:** Temperature dependence of ac-magnetic susceptibilities: (a) real part ( $\chi'$ ) and (b) imaginary part ( $\chi''$ ) component of S1200 recorded at various dc-bias fields  $H_{dc} = 20, 50, 100$  and  $150$  Oe with constant frequency  $f = 2$  Hz and amplitude  $h_{ac} = 1$  Oe. The insets (a)-(c) depict the zoom view of the same curves at various temperature regimes to show the transition better.

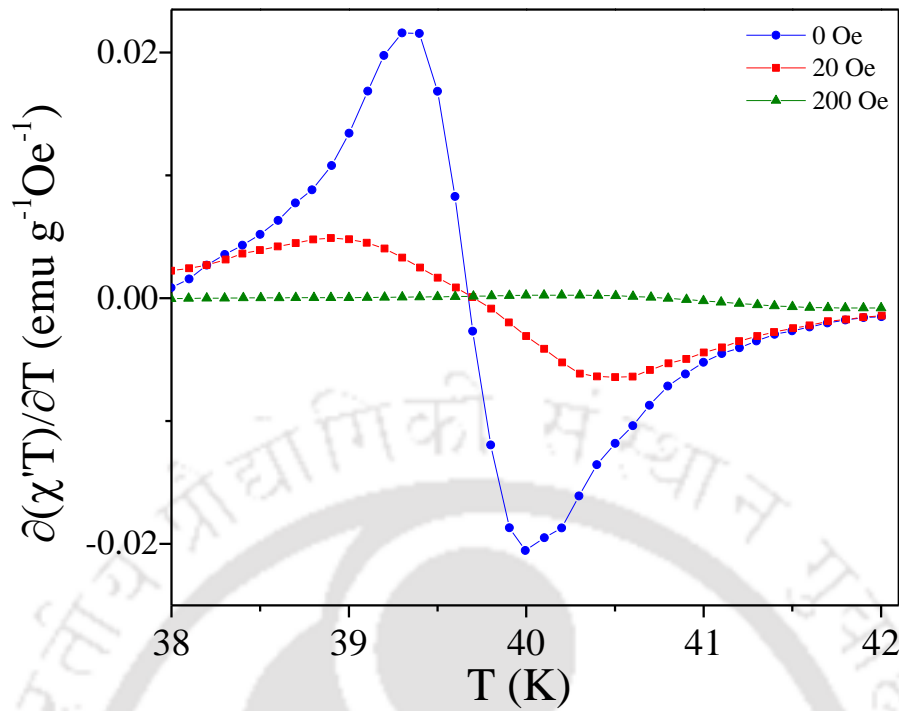
component in  $\text{Co}_2\text{SnO}_4$  system. Such type of semi-spin-glass state was first predicted by Villian in magnetically diluted systems and later established theoretically by Gabay and Thoulose [40, 122]. Figure 3.13 shows temperature dependence of  $\partial(\chi'T)/\partial T$  for S1200 sample. Since, the temperature dependence of  $\partial(\chi'T)/\partial T$  and  $\chi''$  versus T are found to be comparable in many systems and has a strong theoretical basis [123 - 125], similar type of peaks should be observed in  $\partial(\chi'T)/\partial T$  (T) and  $\chi''(T)$ . In S1200, the peaks in the  $\partial(\chi'T)/\partial T$  versus T curve and in  $\chi''$  versus T curve occur at different temperatures. Besides that, we observe that there is a single peak in  $\chi''$  versus T but two peaks in  $\partial(\chi'T)/\partial T$  versus T (associated with  $T_N$  and  $T_{SG}$ ) which suggest a more complicated magnetic ordering of bulk  $\text{Co}_2\text{SnO}_4$  system. The position of two peaks in  $\partial(\chi'T)/\partial T(T)$  and the location of single peak in  $\chi''(T)$  are plotted as function of  $H_{dc}^{2/3}$  (figure 3.14). It is clear from the figure that the peak associated with the  $T_N$  shifts towards higher temperature with increase in the magnetic-field. Such type of behavior justifies the ferrimagnetic character of  $\text{Co}_2\text{SnO}_4$  in which the direct coupling occurs between the order parameter and the applied field. Conversely, the linear behavior of the second peak in  $\partial(\chi'T)/\partial T(T)$  and the single peak in  $\chi''(T)$



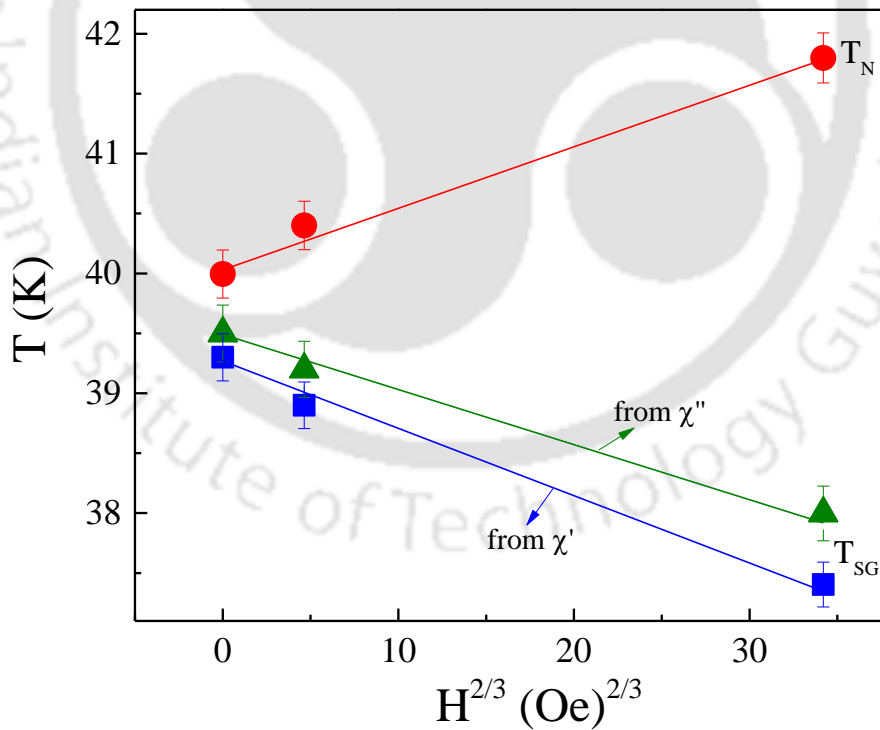
**Figure 3.13:** Temperature variation of  $\partial(\chi'_{ac}T)/\partial T$  plots at different bias fields  $20 \text{ Oe} \leq H_{dc} \leq 150 \text{ Oe}$  for S1200 sample.



**Figure 3.14:** Variation of ferrimagnetic Néel temperature  $T_N$  and spin-glass transition temperature  $T_{SG}$  with respect to  $H^{2/3}$  for S1200 sample. The solid lines show the linear fit to the data (often called the de Almeida-Thouless AT line) whereas the dotted line for  $T_{SG}$  is for visual aid.



**Figure 3.15:** Temperature variation of  $\partial(\chi'_{ac}T)/\partial T$  plots at different bias fields  $0 \text{ Oe} \leq H_{dc} \leq 200 \text{ Oe}$  for S1350 sample.

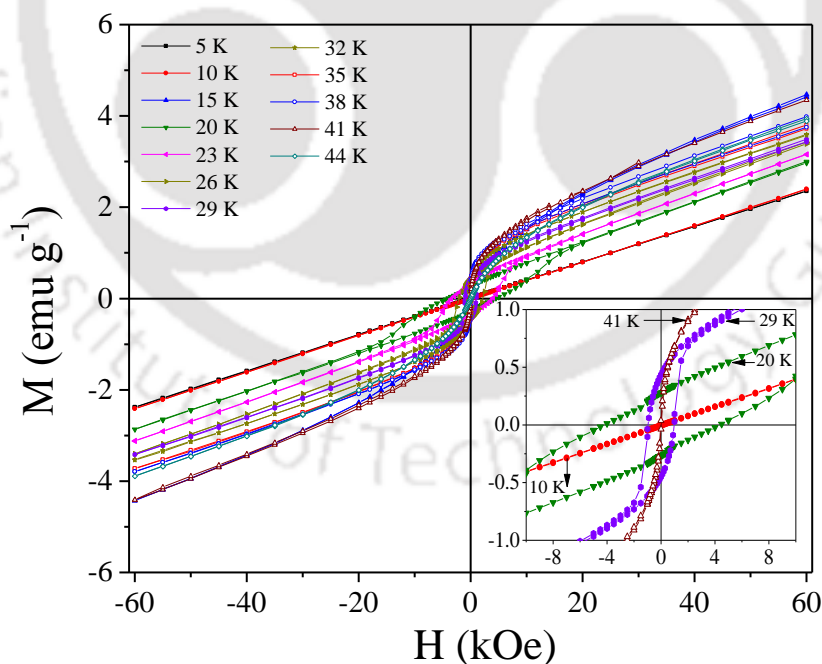


**Figure 3.16:** Variation of ferrimagnetic Néel temperature  $T_N$  and spin-glass transition temperature  $T_{SG}$  with respect to  $H^{2/3}$  for S1350 sample. The solid lines show the linear fit to the data (often called the *de Almeida-Thouless* AT line) whereas the dotted line for  $T_{SG}$  is for visual guide.

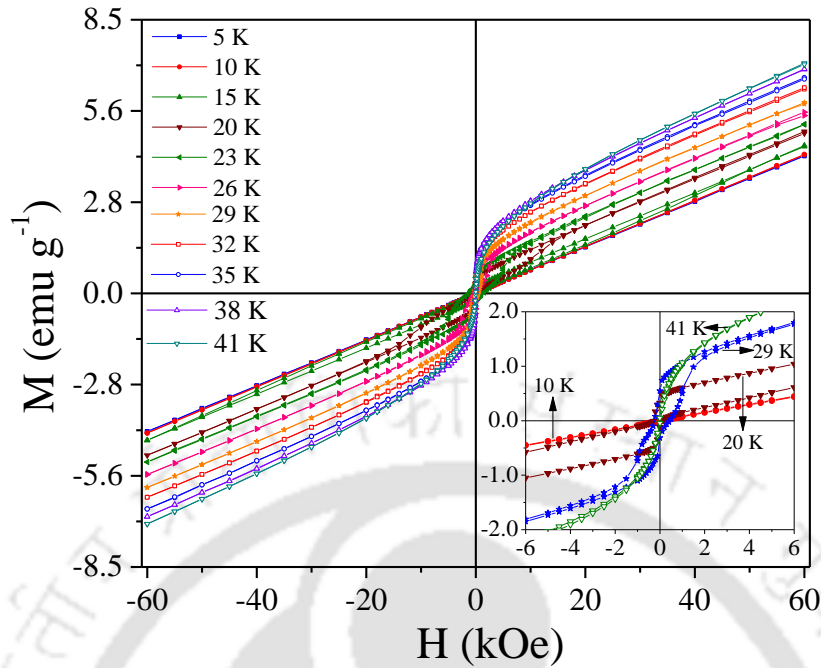
shift identically with  $H_{dc}^{2/3}$ . Such  $H_{dc}^{2/3}$  variation of the peak is characteristic of the de Almeida-Thouless line (popularly known as AT-line) for a spin-glass state and such variation is often used as one of the tests for the presence of spin-glass like short range ordering in a variety of disordered systems [126 - 129]. In  $\text{Co}_2\text{SnO}_4$ , the semi-spin-glass state arises due to magnetic frustration and dilution (i.e. non-magnetic  $\text{Sn}^{4+}$  substituted at octahedral B-sites). The indiscriminate distribution of  $\text{Sn}^{4+}$  on the B-sites weaken the A-B exchange interaction, which randomize the canting of  $\text{Co}^{2+}$  below  $T_N$ . Application of the external dc-magnetic field reduces this random canting and shifts  $T_{SG}$  towards a lower temperature value. Figure 3.15 shows the ac-susceptibility of S1350 for  $f = 51$  Hz, and  $h_{ac} = 4$  Oe with different dc bias fields. No field induced transition to long range order seems to be observed. The magnitude of ac-susceptibility is strongly suppressed in the presence of dc-magnetic field suggests the existence of glassy behavior. The AT-line analysis of S1350 sample (shown in figure 3.16) supports the above spin-glass behavior similar to that of S1200 sample discussed above.

**(b) Temperature Dependence of the Hysteresis Loop Measurements:**

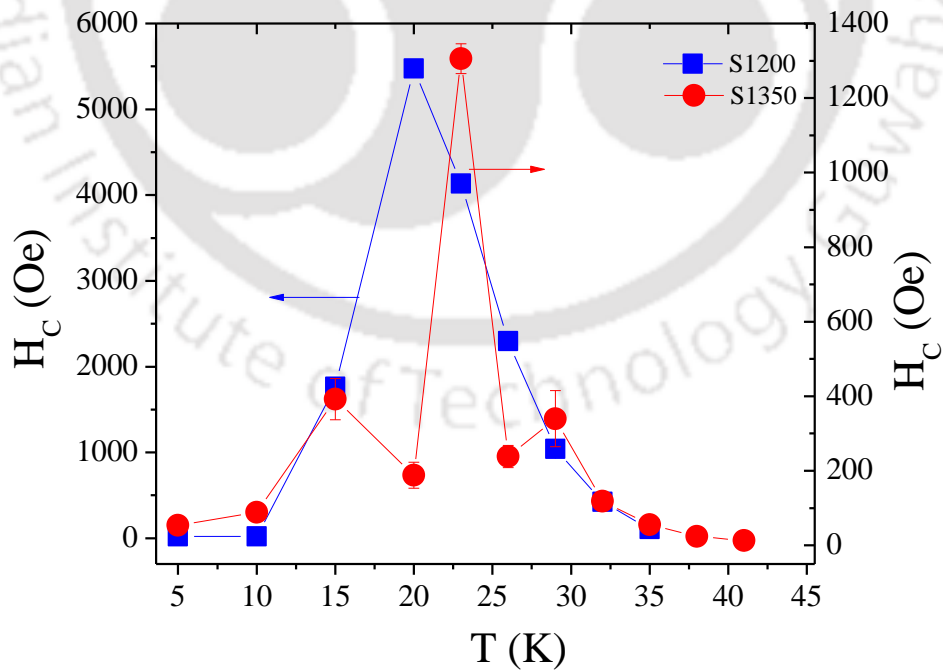
The hysteresis loops measured at various temperatures in the magnetic field range -60 kOe to +60 kOe are shown in the figure 3.17 and 3.18 for S1200 and S1350, respectively. The inset shows a zoomed view of magnetization versus field i.e, M-H curves at selected temperatures 10 K, 20 K, 29 K and 41 K to avoid overcrowding for both the samples. These measurements were done for samples cooled in ‘zero-field’ from room



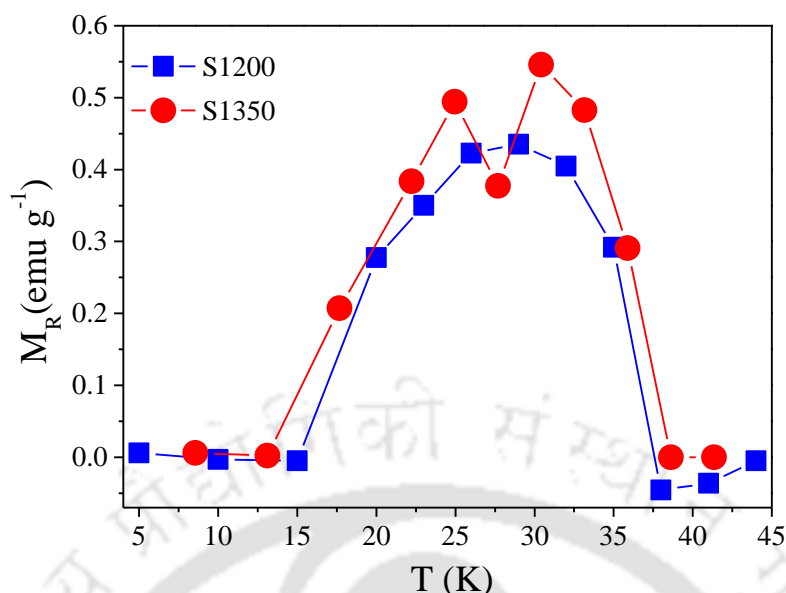
**Figure 3.17:** Magnetization (M) versus magnetic field (H) hysteresis loops recorded at various temperatures in the range  $5 \text{ K} \leq T \leq 45 \text{ K}$  under zero-field conditions for S1200 samples. Inset shows the zoomed view at selected temperature



**Figure 3.18:** Magnetization ( $M$ ) versus magnetic field ( $H$ ) hysteresis loops recorded at various temperatures in the range  $5 \text{ K} \leq T \leq 41 \text{ K}$  under zero-field conditions for S1350 samples. Inset shows the zoomed view at selected temperature.



**Figure 3.19:** Temperature dependent coercivity ( $H_c$ ) for both S1200 and S1350 sample.

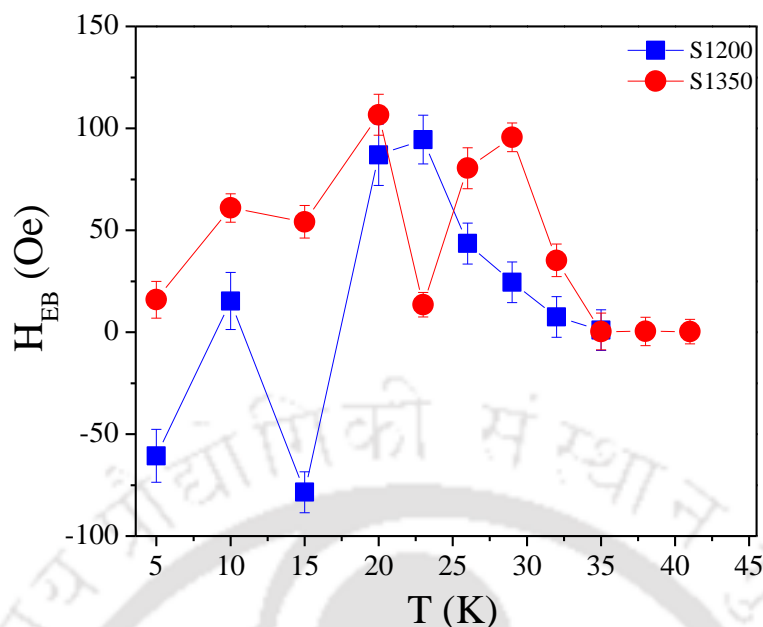


**Figure 3.20:** Temperature dependent remanence ( $M_R$ ) for both S1200 and S1350 sample.

temperature to the measuring temperature. The coercive field  $H_C$ , remanence  $M_R$  and the loops asymmetry  $H_{EB}$  (EB = exchange-bias) were measured from the above loops. The temperature variation of  $H_C$  and  $M_R$  are plotted in figure 3.19 and 3.20. One can clearly notice that  $H_C$  and  $M_R$  are practically zero outside the temperature range of  $15 \text{ K} < T < 39 \text{ K}$  with their peak magnitudes occurring near 25 K. Also the magnitudes of  $M_R$  ( $\sim 0.45 \text{ emu}\cdot\text{g}^{-1}$ ) and their temperature dependences in the two samples (S1200 and S1350) are nearly identical. The magnitudes of the loop asymmetry parameter  $H_{EB}$  for the ZFC samples were also determined from the measured hysteresis loops (figure 3.21). However, their magnitudes at different temperatures were found to be quite small (zero to 100 Oe) as compared to the magnitudes of  $H_C$ , and, their temperature dependence did not show any systematic pattern. Such small values of  $H_{EB}$  might be due to the residual field present in the zero-field cooling process as mentioned above, it is inappropriate at present to attach a great deal of significance to this small asymmetry observed in the hysteresis loops. Generally,  $H_{EB}$  has been observed only in samples cooled in presence of a magnetic field containing ferromagnetic (FM)–antiferromagnetic (AFM) [130], FM-spin glass (SG) [131], FM-ferrimagnetic [132], AFM-ferrimagnetic [133] and AFM-SG [134, 135] interfaces from above the Néel temperature or spin-glass temperature. Recently, few papers have reported significant  $H_{EB}$  in ZFC samples in bulk Ni–Mn–In alloys [136] and in bulk  $\text{Mn}_2\text{PtGa}$  [137]. They predicted that the source of this unusual  $H_{EB}$  in the ZFC sample can be attributed to the presence of complex magnetic ordering containing ferrimagnetic, spin–glass and AFM phases [136, 137].

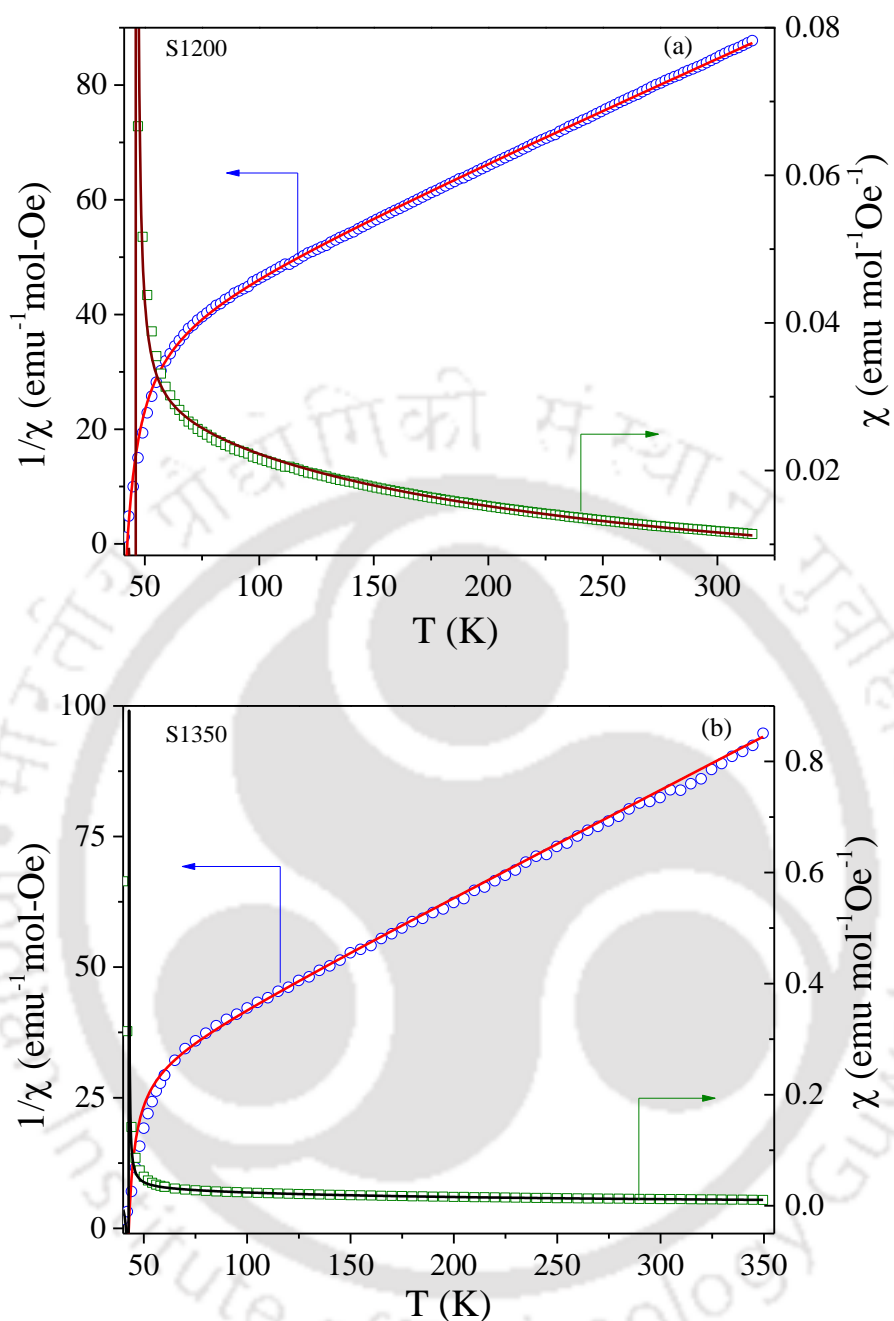
### (c) Temperature Dependence of the Paramagnetic Susceptibility:

Figure 3.22(a) and 3.22(b) shows the temperature dependence of dc-magnetic susceptibility  $\chi(T)$  and its inverse  $\chi^{-1}(T)$  of both the samples S1200 and S1350 above the Néel temperature. One can clearly notice higher values of



**Figure 3.21:** Temperature dependence of exchange-bias ( $H_{EB}$ ) for both the S1200 and S1350 samples.

susceptibility in S1350 sample as compared to S1200 which contains few percent of unreacted  $\text{SnO}_2$ . The solid lines shows least square fits to the Néel expression for ferrimagnets [18].  $(1/\chi) = (T/C) + (1/\chi_0) - [\sigma_0/(T - \theta)]$ . The ratio  $C/\chi_0 = T_a = 130.99 \text{ K}$  ( $112.13 \text{ K}$ ) for S1200 (S1350) represents the strength of the antiferromagnetic exchange coupling between the spins on the ‘A’ and ‘B’ sites and is often termed as asymptotic Curie temperature ‘ $T_a$ ’. Using the Curie constant ‘C’ value ( $=N\mu_{\text{eff}}^2/3k_B$ ) we have evaluated the total effective magnetic moment  $\mu_{\text{eff}} = 6.31 \mu_B$  ( $6.25 \mu_B$ ) for S1200 (S1350) which is equivalent to  $\mu_{\text{eff}} = [\mu(A)^2 + \mu(B)^2]^{0.5}$ . Assuming spin only moment of  $\text{Co}^{2+}$  ion in A –sites i.e.,  $\mu(A) = 3.87 \mu_B$  ( $3.87 \mu_B$ ) for S1200 (S1350) with  $S = 3/2$  and  $g = 2$ , we obtained the ‘B’ site magnetic moment  $\mu(B) = 4.98 \mu_B$  ( $4.91 \mu_B$ ) for S1200 (S1350) samples respectively. Table 3.2 summarizes the magnetic moments of A and B-sites along with the other parameters obtained from the fitting analysis. Using the fitted parameters of the Néel’s expression we have evaluated the molecular field constants ( $N_{AA}$ ,  $N_{BB}$  and  $N_{AB}$ ) between nearest neighbor and next nearest neighbors, and the corresponding exchange constants ( $J_{AA}$ ,  $J_{BB}$  and  $J_{AB}$ ) for both S1200 and S1350 systems. Among all the theoretical and experimental techniques, temperature dependent paramagnetic susceptibility is the most constructive and useful method to determine the magnitude of such exchange parameters. The obtained molecular field constants and the exchange constants are listed in table 3.2. From the table one can clearly observe that molecular field constants follows the trend  $N_{AB} > N_{AA} > N_{BB}$ . However, the antiferromagnetic exchange coupling constants  $J_{BB} = 6.14 \text{ k}_B$  ( $4.28 \text{ k}_B$ ) and  $J_{AB} = 5.97 \text{ k}_B$  ( $5.26 \text{ k}_B$ ) are greater than  $J_{AA} = 4.07 \text{ k}_B$  ( $4.05 \text{ k}_B$ ) for S1200 and S1350 systems, respectively. Such trend of exchange constants was observed earlier in other spinels also [138-140]. From the above analysis, we can conclude that the difference in  $\mu_{\text{eff}}$  for  $\text{Co}^{2+}$  on A and B-sites along with the antiferromagnetic coupling constants is responsible for the ferrimagnetism in  $\text{Co}_2\text{SnO}_4$ .



**Figure 3.22:** Temperature dependence of susceptibility ( $\chi$  versus  $T$ ) (R.H.S) and inverse susceptibility (L.H.S) ( $\chi^{-1}$  versus  $T$ ) for the samples (a) S1200 (b) S1350 are shown. The solid lines are fits to the Néel's expression for ferrimagnets as discussed in this chapter.

We now compare the magnetic properties of  $\text{Co}_2\text{SnO}_4$  with those reported in literature for some other relevant spinels. In 1956, Anderson predicted that in normal spinels such as  $\text{ZnFe}_2\text{O}_4$  in which the magnetic ions  $\text{Fe}^{3+}$  all occupy the B-sites and the geometrical frustration will lead to lack of long range magnetic order [141]. This has been confirmed recently in  $\text{ZnFe}_2\text{O}_4$  in that although the system orders antiferromagnetically at  $T_N \sim 10.5$  K, short

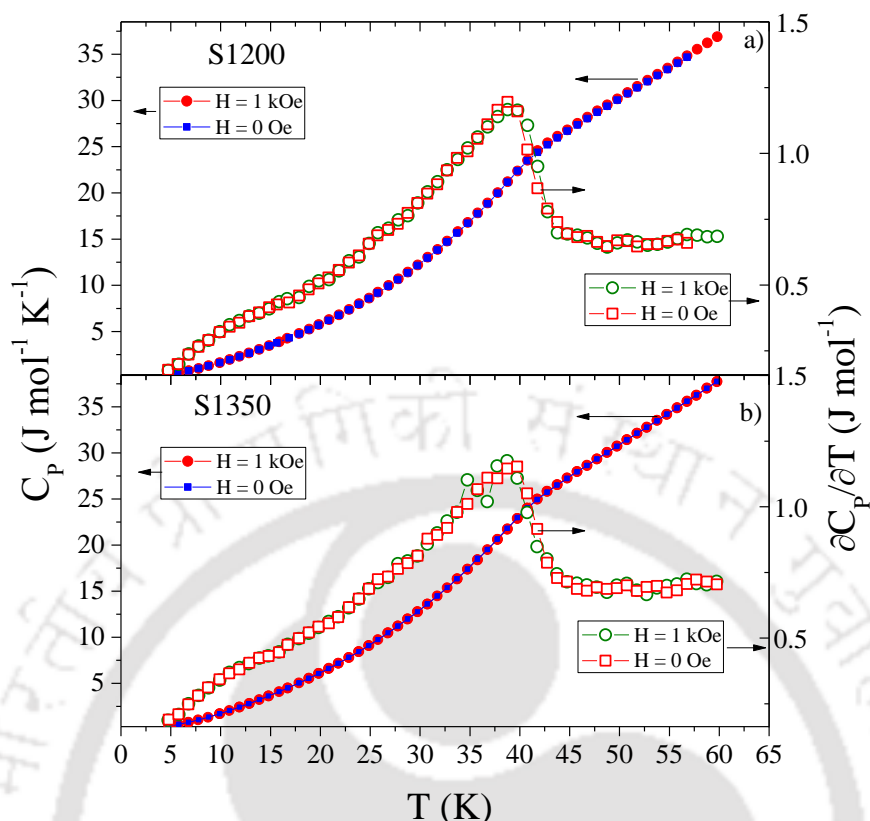
**Table 3.2:** The list of various parameters obtained from the Néel fits of  $\chi^{-1}$  versus T curve recorded under zero-field condition.

System	C (emu K mol <sup>-1</sup> Oe <sup>-1</sup> )	$\chi_0$ (emu mol <sup>-1</sup> Oe <sup>-1</sup> )	$\sigma_0$ (emu <sup>-1</sup> Oe mol K)	$\theta$ (K)	$\mu_{\text{eff}}$ ( $\mu_B$ )	$\mu$ (A) ( $\mu_B$ )	$\mu$ (B) ( $\mu_B$ )
$\text{Co}_2\text{SnO}_4$ (S1200)	4.987	0.03807	77.001	44.1228	6.313	3.872	4.985
	$g_A = 2$ $g_B = 2.53$	$N_{AA}$ 21.73	$N_{BB}$ 14.82	$N_{AB}$ 37.12	$J_{AA}$ 4.07 $k_B$	$J_{BB}$ 6.14 $k_B$	$J_{AB}$ 5.97 $k_B$
$\text{Co}_2\text{SnO}_4$ (S1350)	4.889	0.0436	102.400	39.5	6.2508	3.8729	4.9064
	$g_A = 2$ $g_B = 2.57$	$N_{AA}$ 21.564	$N_{BB}$ 10.678	$N_{AB}$ 33.201	$J_{AA}$ 4.05 $k_B$	$J_{BB}$ 4.28 $k_B$	$J_{AB}$ 5.26 $k_B$

range order is observed at temperatures as high as  $10 T_N$  and well below  $T_N$  [8]. In the inverse spinel  $\text{CoFe}_2\text{O}_4$  with ionic distribution of  $[\text{Fe}^{3+}][\text{Co}^{2+}\text{Fe}^{3+}]\text{O}_4$ , ferrimagnetism is observed with  $T_N \sim 793$  K [18]. In this case,  $\text{Fe}^{3+}$  moments on the A- and B-sites are antiparallel with  $\text{Co}^{2+}$  provides the ferrimagnetic component. Recently, Bhowmik *et al.* reported the nature of magnetism in magnetically diluted  $\text{Co}_{0.2}\text{Zn}_{0.8}\text{Fe}_2\text{O}_4$  system [142]. The 20% concentration of  $\text{Co}^{2+}$  obtained by 80% dilution of the  $\text{Co}^{2+}$  with  $\text{Zn}^{2+}$  is well below the percolation threshold  $p_c = 33\%$  of  $\text{Co}^{2+}$  needed for long-range magnetic ordering. Interestingly, the reported magnetic studies indicate  $T_N \sim 110$  K and for  $110 \text{ K} \leq T \leq 260 \text{ K}$ , it is inferred that short range ferrimagnetic phase coexists with cluster spin-glass phase [142]. In the  $\text{Co}_{0.2}\text{Zn}_{0.8}\text{Fe}_{1.95}\text{Ho}_{0.05}\text{O}_4$  system, ferrimagnetism with  $T_N \sim 225$  K followed by cluster spin-glass state below 120 K is reported. [143] Since it is well established that for magnetic concentration  $p < p_c$ , the system consists of unconnected magnetic clusters often with spin-glass like ordering, [104, 105] it is highly likely that cluster spin-glass states reported in these systems is due to the magnetic dilution of  $\text{Co}^{2+}$  site well below its  $p_c$ . The  $\text{Co}_2\text{SnO}_4 = [\text{Co}^{2+}][\text{Co}^{2+}\text{Sn}^{4+}]\text{O}_4$  system investigated here differs substantially from the  $\text{Co}_{0.2}\text{Zn}_{0.8}\text{Fe}_2\text{O}_4$  system noted above in that the magnetic dilution of  $\text{Co}^{2+}$  B-site by  $\text{Sn}^{4+}$  is only 50%, well above  $p_c = 33\%$ . Consequently, this system is expected to exhibit long-range magnetic ordering of the longitudinal component followed by the predicted spin-glass freezing of the transverse component in a diluted spinel. The  $H^{2/3}$  dependence of the spin-glass freezing temperature  $T_{\text{SG}}$  provides the confirmatory evidence. These results suggest paramagnetism in  $\text{Co}_2\text{SnO}_4$  for  $T \gg T_N$ , but normal spin correlations develop as T approaches  $T_N$  from above.

### 3.3.5 Temperature Dependence of Specific Heat:

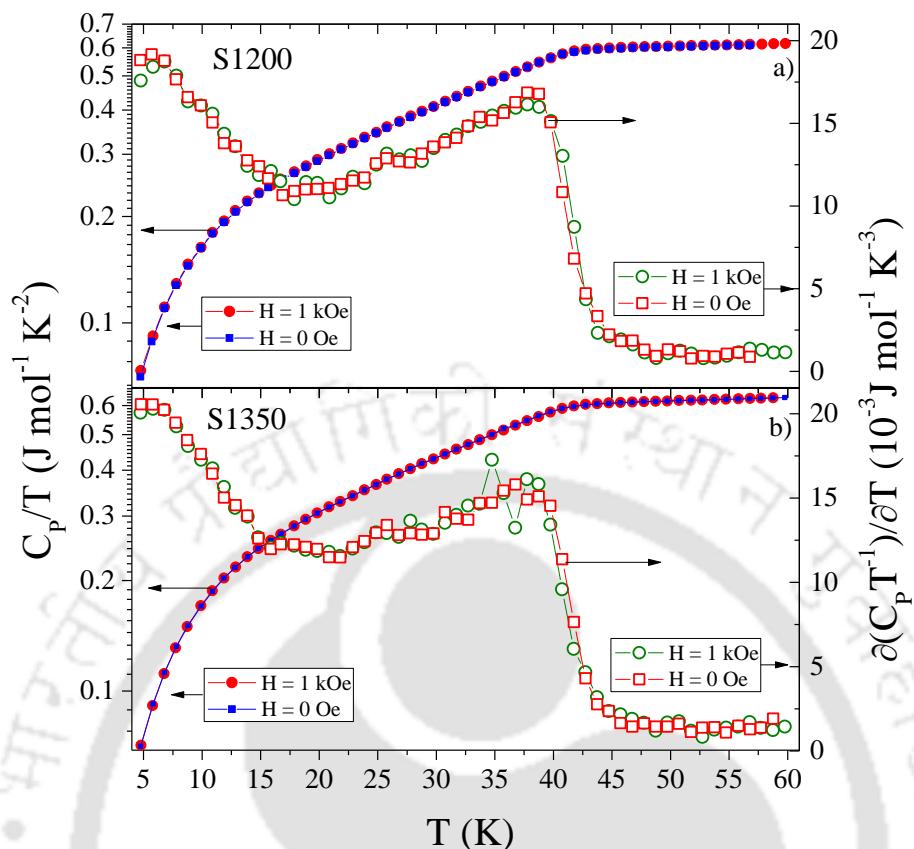
The temperature dependence of the specific-heat  $C_P(T)$  for the S1200 and S1350 samples in  $H = 0$  Oe and  $H = 1$  kOe, measured from 5 K to 60 K in 1 K steps, is shown in figure 3.23 (a) and (b). For both samples, no measurable difference is observed for the data recorded in  $H = 0$  and  $H = 1$  kOe, and, there is no indication of any



**Figure 3.23:** The temperature dependence of specific heat  $C_p(T)$  for the samples; (a) S1200, and (b) S1350 measured under both zero magnetic field and in the presence of magnetic field of  $H = 1$  kOe recorded under warming condition. The corresponding derivative plots  $\partial C_p(T)/\partial T$  versus  $T$  is shown on the right-hand-side scale.

peak in  $C_p(T)$  near 41 K or 39 K expected for a conventional first or second order magnetic phase transition [146, 147]. Instead, there is only an inflection point near 39 K which yields a peak in  $\partial(C_p)/\partial T$  near 39 K as shown in figure 3.23 (right hand scale). Furthermore, there is an indication of another weak anomaly in  $\partial(C_p)/\partial T$  near 15 K below which  $\partial(C_p)/\partial T$  continues to increase. The absence of peak in  $C_p$  is a well-known characteristic of spin-glass ordering near  $T_{SG}$  [146, 147]. Thus the new measurements of  $C_p$  versus  $T$  reported here for both the S1200 and S1350 samples of  $\text{Co}_2\text{SnO}_4$  indicate the presence of a spin-glass transition near 39 K and suggest some changes in magnetic ordering taking place below 15 K. A detailed study related to this low-temperature anomalous magnetic ordering will be discussed in the coming chapter where we compare the low-temperature magnetic properties of  $\text{Co}_2\text{SnO}_4$  with its sister compound  $\text{Co}_2\text{TiO}_4$ .

Furthermore, we have plotted the  $C_p/T$  and its temperature derivative  $\partial(C_p T^{-1})/\partial T$  versus  $T$  in figure 3.24 to look for any anomalous changes. There is a clear change in  $C_p/T$  versus  $T$  data at 39 K suggesting the entropy loss due to spin-glass ordering beginning near 39 K. There is another rapid decrease in  $C_p/T$  with decreasing  $T$  beginning near 15 K, indicating further changes in the magnetic ordering of the system. These anomalies are clearly evident in the computed plots of  $\partial(C_p T^{-1})/\partial T$  versus  $T$  in figure 3.24. Further support for these results comes from the temperature dependence of the magnetic hysteresis loop parameters discussed in section (b).



**Figure 3.24:** The temperature variation of the  $C_p/T$  and its first derivative  $\partial(C_p T^{-1})/\partial T$  for the two samples (a) S1200 and (b) S1350 in  $H = 0$  Oe and  $H = 1$  kOe.

Comparison of the experimental results of  $\text{Co}_2\text{SnO}_4$  with its sister compound  $\text{Co}_2\text{TiO}_4$  should particularly illuminating because of the similarity of the two systems since non-magnetic  $\text{Ti}^{4+}$  on the B-sites in the former is replaced by non-magnetic  $\text{Sn}^{4+}$  in the later. In  $\text{Co}_2\text{TiO}_4$ ,  $T_N$  at 55 K was followed by  $T_{SG}$  at 46 K [77] compared to  $T_N = 41$  K and  $T_{SG} = 39$  K in  $\text{Co}_2\text{SnO}_4$  reported here. The temperature dependence of coercivity  $H_C$  in  $\text{Co}_2\text{TiO}_4$  showed a compensation point near 28 K followed by a peak in  $H_C$  near 20 K and then dropping to very low values at 1.5 K, the lowest temperature attained in these experiments [77]. The results reported here for  $\text{Co}_2\text{SnO}_4$  do not show a compensation point in either  $H_C$  or  $M_R$  but do show their peak values near 25 K as in  $\text{Co}_2\text{TiO}_4$  followed by rapid drops to negligible magnitudes as the temperature is lowered below 15 K.

A quantitative explanation of the temperature dependence of  $H_C$ , and  $M_R$  in  $\text{Co}_2\text{SnO}_4$  shown in figure 3.19 and 3.20 is not yet possible. However, following the observation of a compensation point in the sister compound  $\text{Co}_2\text{TiO}_4$  [77], it is likely that the different magnitudes and different temperature dependences of the moments on the  $\text{Co}^{2+}$  ions on the ‘A’ and ‘B’ sites in  $\text{Co}_2\text{SnO}_4$  are responsible for the peaks in  $H_C$  and  $M_R$  observed near 25 K. Below about 15 K, the data suggest that there is near complete effective balance of the antiferromagnetically coupled  $\text{Co}^{2+}$  moments at the ‘A’ and ‘B’ sites leading to negligible values of  $H_C$  and  $M_R$ . Earlier results from neutron diffraction in  $\text{Co}_2\text{TiO}_4$  suggested the presence of canted-spins, likely resulting from magnetic frustration

caused by the presence of non-magnetic  $\text{Ti}^{4+}$  ions on the 'B'-sites. A similar canting of the spins might be present in  $\text{Co}_2\text{SnO}_4$  although neutron diffraction studies are needed to verify this suggestion. There are a few subtle differences between the properties of S1200 which contains a few percent of unreacted  $\text{SnO}_2$  and S1350 which does not. Structurally, S1350 was found to be relatively denser material and its lattice constant was slightly larger than that of S1200. Both of these effects were considered to be originated from the high sintering temperature ( $1350^\circ\text{C}$ ) of S1350. In magnetic properties, the major noticeable difference between the two samples is in the magnitudes of the coercivity  $H_C$ . Although the magnitudes of  $H_C$  in both samples peak near 25 K,  $H_C$  in S1200 is nearly 4 times larger than that in S1350. This suggests that in the two samples, the domain structures are somewhat different perhaps due to their different method of preparation although the positions and characteristics of the transitions near 41 and 39 K with peak magnitudes of  $H_C$  and  $M_R$  occurring 25 K and becoming negligible below 15 K are identical in S1200 and S1350. The ac-magnetic susceptibility data and its analysis suggest that the system consists of interacting magnetic clusters close to a spin glass state. These results are reminiscent of those shown in [148], [149] and [150]. In [148], the onset of the cusps in  $\chi'$  (i.e. just above the cusp temperature) were found to be frequency independent, suggesting quasi-long-ranged ferri or antiferromagnetically ordered systems affected by the magnetic frustration. However, in [149] and [150], spin glass phase transitions were observed. In [150],  $\text{La}_{1.1}\text{Sr}_{0.9}\text{MnO}_4$  was found to first order antiferromagnetically, yet the low temperature ac-magnetic susceptibility data indicated that spin glass correlations developed below  $T_N$ .

#### 3.3.6 Summary:

Interpretation of the detailed temperature dependence of the ac- and dc-magnetic susceptibilities of the ferrimagnetic spinel  $\text{Co}_2\text{SnO}_4$ , presented in this chapter, has established the presence of two magnetic transitions in this system visualizing:  $T_N = 41$  K and  $T_{SG} = 39.1$  K. Also, all the molecular field exchange constants  $N_{AA} = 21.73$  (21.56),  $N_{BB} = 14.82$  (10.68) and  $N_{AB} = 37.12$  (33.20) between the magnetic ions on the 'A' and 'B' sites with magnetic moments  $\mu(A) = 3.87 \mu_B$  ( $3.87 \mu_B$ ) and  $\mu(B) = 4.98 \mu_B$  ( $4.98 \mu_B$ ) for S1200 (S1350) respectively, were determined and found to be antiferromagnetic in nature. The ferrimagnetic transition at  $T_N$  is associated with ordering of the longitudinal spin component, whereas,  $T_{SG}$  was attributed to freezing of the transverse spin component. These observations confirm the prediction of Villian [40] in magnetic insulators with non-magnetic impurities, which have been found to be responsible the magnetic frustration and spin-glass like ordering of the transverse spin component.

## Negative Magnetization and Compensation Effect in $\text{Co}_2\text{TiO}_4$

### 4.1 Literature Review:

In the previous chapter we discussed the detailed magnetic structure of  $\text{Co}_2\text{SnO}_4$ ; in this chapter we extend these studies for its sister compound cobalt-orthotitanate ( $\text{Co}_2\text{TiO}_4$ ). Magnetization reversal and negative magnetization has been widely discussed in recent years because of their technological applications in spintronic devices [57, 60, 151 -154]. The magnetization reversal is defined as a crossover of dc magnetization value from a positive to a negative value as the temperature decreases below its long-range ordering. This phenomenon has been debated in literature in a variety of magnetic materials such as spinel ferrites, perovskites, molecular magnets, garnets, intermetallic alloys and multilayers [58]. Several intrinsic properties, e.g. size of the magnetic ions and their exchange interactions, global crystal structure of the compound, magnetic anisotropy, and different temperature dependence of the magnetization of individual cations sitting in the sublattice play a very important role on the magnetization reversal of a compound. Moreover, magnetization reversal and negative magnetization have gained technological importance because of their applications in the field of magneto-electronic switching devices with positive and negative stable states of magnetization under moderate applied fields. During 1950's Néel first observed the phenomenon of magnetization reversal in spinel ferrites. Nevertheless, the theoretical research related to such phenomena was reported a little earlier (in 1948's) than the experimental findings [52]. However, such a fundamental issue in magnetism, has not been paid enough attention in the literature until recent years [155-157]. Therefore, in this chapter, we focus on the magnetization reversal and negative magnetization in  $\text{Co}_2\text{TiO}_4$  whose crystal structure is identical to  $\text{Co}_2\text{SnO}_4$ . In the previous chapter we discussed the nature of magnetic ordering in the spinel  $\text{Co}_2\text{SnO}_4$ , for which, the distributions of the cations on the A- and the B-sites were established to be  $[\text{Co}^{2+}]_A[\text{Co}^{2+}\text{Sn}^{4+}]_B\text{O}_4$ . Analysis of the temperature dependence of both the ac and dc magnetic susceptibilities, and specific heat measurements showed that  $\text{Co}_2\text{SnO}_4$  is a ferrimagnet due to different magnetic moments of  $\text{Co}^{2+}$  sitting at the A- and the B-sites below its ordering temperature  $\sim 41$  K.

$\text{Co}_2\text{TiO}_4$  is isostructural to  $\text{Co}_2\text{SnO}_4$ , in which, non-magnetic 'Sn' plays a similar role of 'Ti'. Although a few are available in the literature dealing with the nature of magnetism in  $\text{Co}_2\text{TiO}_4$ , the results have been controversial. Magnetization studies by Hubsch *et al.* reported ferrimagnetic ordering in  $\text{Co}_2\text{TiO}_4$  with  $T_N \sim 55$  K followed by spin glass transition at  $T_{SG} \sim 46$  K with a magnetic compensation effect near 30 K [77 - 78]. However, later ac-susceptibility studies by Srivastava *et al.* [79] showed no indication of  $T_N \sim 55$  K, rather only a single peak in  $\chi_{ac}$  near 48 K when  $H_{dc} = 0$ . The temperature dependence of specific heat  $C_P(T)$  of  $\text{Co}_2\text{TiO}_4$  by Ogawa and Waki [80] reported only a weak transition near 49 K, which was associated with ferrimagnetic ordering. This indicates the absence of a proper transition near 55 K [80]. In all these reports, it has been assumed that the electronic state of 'Ti' in  $\text{Co}_2\text{TiO}_4$  is  $\text{Ti}^{4+}$ , similar to  $\text{Sn}^{4+}$  in  $\text{Co}_2\text{SnO}_4$  [77, 155 - 157].

In this chapter, we investigated the magnetic properties of  $\text{Co}_2\text{TiO}_4$  in a very detailed way, aiming to address the unsettled issues listed above. We also examined the similarities and differences in the magnetic properties of the isostructural compounds  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$ . Differences such as why the compensation effect observed in  $\text{Co}_2\text{TiO}_4$  near 30 K was not visible in  $\text{Co}_2\text{SnO}_4$  despite of the identical electronic states of Co in both the systems. In these studies, we employed various characterization techniques, such as, X-ray diffraction (XRD), X-ray photoelectron spectroscopy (XPS), temperature and magnetic field dependence of the ac and dc magnetic susceptibilities, and specific-heat measurements to unravel the nature of magnetic ordering in  $\text{Co}_2\text{TiO}_4$ . In the following section we present a comprehensive experimental details including the synthesis procedure.

### 4.2 Experimental Details:

The polycrystalline  $\text{Co}_2\text{TiO}_4$  samples were synthesized by standard solid state reaction method starting with stoichiometric amounts of  $\text{Co}_3\text{O}_4$  (Alfa Aesar, purity 99.99%), and  $\text{TiO}_2$  (Alfa Aesar, purity 99.99%) as precursors. Appropriate amounts of these materials were first ground in an agate mortar and sieved through 240 mesh. The mixed powders were pressed into cylindrical pellets of diameter  $\sim 13$  mm using a hydraulic press with a maximum load of 5 ton per  $\text{cm}^2$ . The pellets of  $\text{Co}_2\text{TiO}_4$  were finally sintered at 1120 - 1200°C for 18 h in air to yield the desired compound without any impurities or unreacted  $\text{TiO}_2$  precursor. The structural characterization was performed using PHILIPS PW 1050 X-ray powder diffractometer with  $\text{Co-K}_\alpha$  radiation of wavelength 1.7889 Å, and a Rigaku X-ray diffractometer (model: TTRAX III) with  $\text{Cu-K}_\alpha$  radiation ( $\lambda = 1.54056$  Å). We also performed the Rietveld refinement of the diffraction patterns using FullProf program which confirmed the phase purity of the samples (Figure 4.1). Both dc-magnetization and frequency dependence (0.17 Hz - 1.2 kHz) of ac-magnetic susceptibility measurements were performed using a superconducting quantum interference device (SQUID) based magnetometer from Quantum Design with temperature capabilities of 2 K – 320 K and magnetic field (H) up to  $\pm 90$  kOe. The low temperature heat capacity data ( $C_p(T)$ ) were recorded by means of a physical property measurement system (PPMS), from Quantum Design. The surface chemical composition of both the bulk samples were analyzed by means of XPS measurements performed with a dual source VG Microtech XPS microprobe system using  $\text{Al-K}_\alpha$  radiation (1486.8 eV) source at a base pressure of  $8 \times 10^{-10}$  Torr. The XPS data was collected from 0 to 1100 eV of binding energy (B.E.) which is acquired with constant pass energy of 100 eV. All the spectra were analyzed using Gaussian-Lorentzian curve fitting.

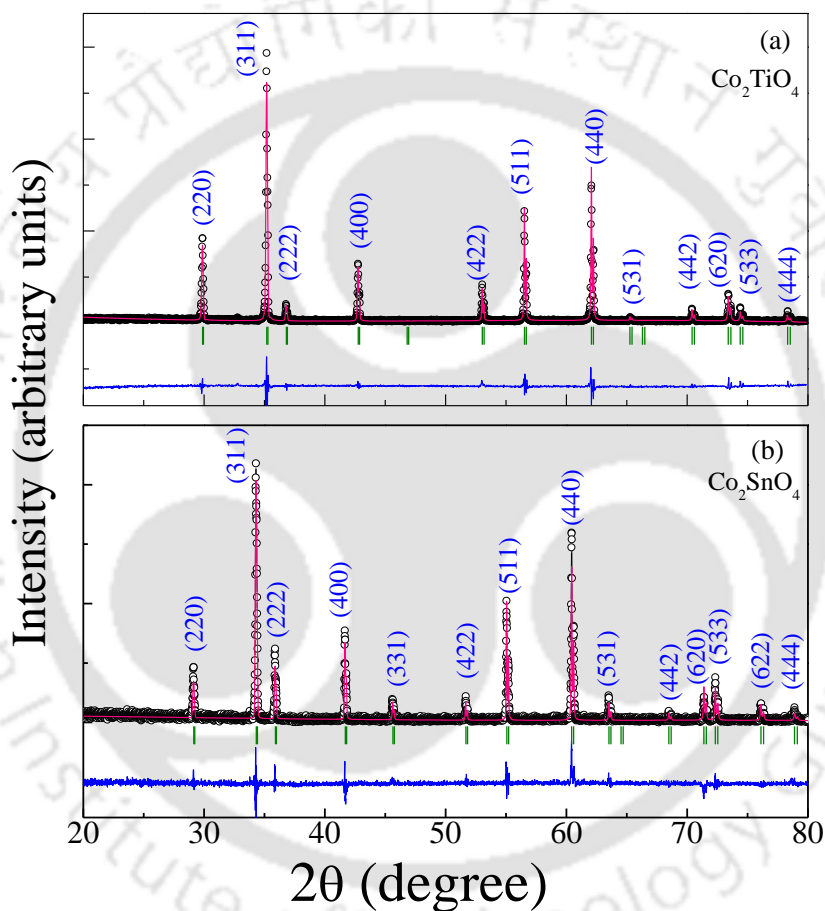
### 4.3 Results and Discussion:

#### 4.3.1 Structural Characterization

Figure 4.1(a) shows the XRD pattern of the  $\text{Co}_2\text{TiO}_4$  polycrystalline sample along with the Rietveld refined data performed using FullProf program, the XRD pattern of  $\text{Co}_2\text{SnO}_4$  also shown in this figure 4.1(b) for the sake of comparison. These patterns are consistent with the standard cubic spinel phase with space group  $Fd-3m$  (227). However, the lattice parameters obtained for  $\text{Co}_2\text{TiO}_4$  ( $a = 8.45$  Å) are slightly less than that of  $\text{Co}_2\text{SnO}_4$  ( $a = 8.66$  Å). Such variation in the lattice parameters is generally associated with the different ionic radii of the constituent

**Table 4.1:** The list of lattice parameters ( $a = b = c$ ), bond lengths and bond angles in  $\text{Co}_2\text{SnO}_4$  and  $\text{Co}_2\text{TiO}_4$ . (The interaxial angles  $\alpha = \beta = \gamma = 90^\circ$ )

System	Lattice Parameter	Bond Length		Bond Angle	
		A-O	B-O	A-O-B	B-O-B
$\text{Co}_2\text{TiO}_4$	$8.45 \pm 0.01 \text{ \AA}$	$1.98 \pm 0.011 \text{ \AA}$	$2.03 \pm 0.017 \text{ \AA}$	$121.68^\circ \pm 0.612^\circ$	$94.95^\circ \pm 0.478^\circ$
$\text{Co}_2\text{SnO}_4$	$8.66 \pm 0.02 \text{ \AA}$	$1.88 \pm 0.02 \text{ \AA}$	$2.16 \pm 0.021 \text{ \AA}$	$125.01^\circ \pm 0.625^\circ$	$90.37^\circ \pm 0.452^\circ$



**Figure 4.1:** X-ray diffraction patterns of (a)  $\text{Co}_2\text{TiO}_4$  and (b)  $\text{Co}_2\text{SnO}_4$ . The scattered symbols represent the experimental data whereas the red lines depict Rietveld refined data. The vertical lines represent the Bragg positions and the bottom blue line shows the difference between the experimental and calculated intensity.

elements. Since the ionic radius of tetravalent stannous ion ( $\text{Sn}^{4+} = 0.69 \text{ \AA}$ ) is slightly greater than that of the titanium ion (either  $\text{Ti}^{4+} = 0.605 \text{ \AA}$  or  $\text{Ti}^{3+} = 0.67 \text{ \AA}$ ), larger unit cell dimensions of  $\text{Co}_2\text{SnO}_4$  as compared to that of  $\text{Co}_2\text{TiO}_4$  is expected. On the other hand, the ionic radius of  $\text{Co}^{2+}$  ions in tetrahedral sites with coordination number four is smaller ( $\text{Co}_{\text{Tetra-A}}^{2+} = 0.58 \text{ \AA}$ ) than that in high spin octahedral sites with six coordination ( $\text{Co}_{\text{Octa}}$

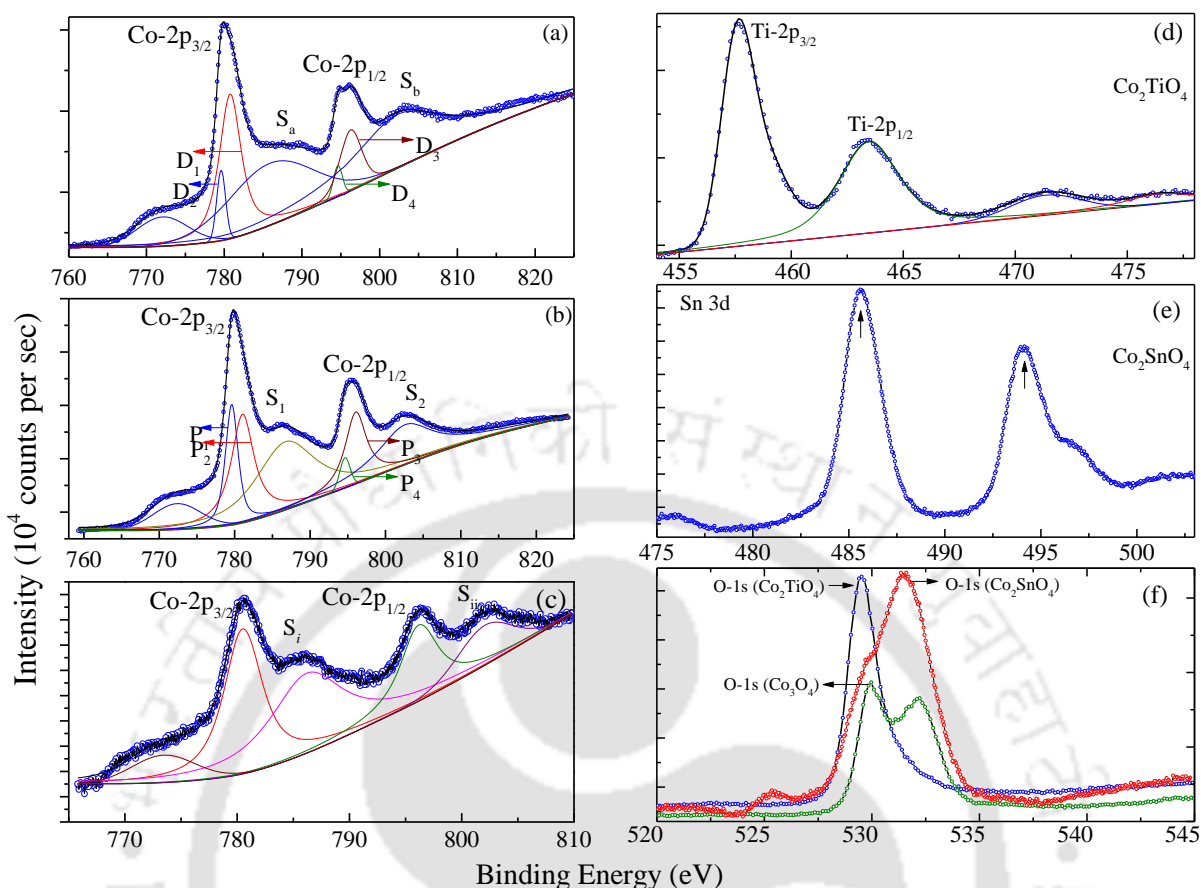
$B^{2+} = 0.745 \text{ \AA}$ ). Table-4.1 summarizes the bond lengths and bond angles in both Co<sub>2</sub>TiO<sub>4</sub> and Co<sub>2</sub>SnO<sub>4</sub> estimated from the refinement process. It is evident that the average bond length (B-O) between the oxygen ion and elements present in the octahedral sites of Co<sub>2</sub>SnO<sub>4</sub> are higher than that in Co<sub>2</sub>TiO<sub>4</sub> while the reverse is true for the tetrahedral sites. Such differences in bond lengths in the octahedral and tetrahedral sites in the two systems result from the difference in the ionic sizes. Since the ‘Sn’ ion is larger than the ‘Ti’ ions, the B-O bond length in Co<sub>2</sub>SnO<sub>4</sub> is greater than that in Co<sub>2</sub>TiO<sub>4</sub>, resulting in larger lattice parameter of Co<sub>2</sub>SnO<sub>4</sub> than that of Co<sub>2</sub>TiO<sub>4</sub> as observed experimentally.

### 4.3.2 X-ray Photoelectron Spectroscopy:

Figure 4.2 (a), (b) and (c) shows the intensity of XPS spectra versus binding energy of the Co-2p core levels for pure Co<sub>3</sub>O<sub>4</sub>, Co<sub>2</sub>TiO<sub>4</sub> and Co<sub>2</sub>SnO<sub>4</sub> systems, respectively. All these spectra exhibit two sharp peaks characteristic of Co-2p<sub>3/2</sub> and Co-2p<sub>1/2</sub> together with the weak intensity satellite peaks shown by arrows at 786.7 eV (S<sub>1</sub>) and 802.91 eV (S<sub>2</sub>). It is well known that both Co<sup>2+</sup> and Co<sup>3+</sup> exhibit similar binding energy peaks in XPS data with a sharp transition near 780 eV identified with 2p<sub>3/2</sub> level and second peak near 796 eV identified with 2p<sub>1/2</sub> level. However, the energy splitting ( $\Delta E$ ) between the two levels due to spin-orbit coupling should be different for the Co<sup>2+</sup> and Co<sup>3+</sup> configurations with  $\Delta E = 15.0 \text{ eV}$  for Co<sup>3+</sup> and  $\Delta E = 15.7 \text{ eV}$  for Co<sup>2+</sup> [112 - 114]. The XPS data in figure 4.2(a) for the spinel Co<sub>3</sub>O<sub>4</sub> which contains both Co<sup>2+</sup> and Co<sup>3+</sup> ions distributed on the A and the B-sites as [Co<sup>2+</sup>]<sub>A</sub>[2Co<sup>3+</sup>]<sub>B</sub>O<sub>4</sub> clearly shows the presence of doublet at D<sub>1</sub> = 779.84 eV and D<sub>2</sub> = 780.34 eV for the Co-2p<sub>3/2</sub> level and a doublet for Co-2p<sub>1/2</sub> level centered at D<sub>3</sub> = 794.84 eV and D<sub>4</sub> = 796.09 eV. The separations between the doublet peaks are  $\Delta E_{D_1-D_3} = 15 \text{ eV}$  and  $\Delta E_{D_2-D_4} = 15.75 \text{ eV}$  which are close to the above mentioned values for Co<sup>3+</sup> and Co<sup>2+</sup> respectively, thus confirming the presence of Co<sup>3+</sup> and Co<sup>2+</sup> in Co<sub>3</sub>O<sub>4</sub>. These results are in good agreement with the previously reported data by Chuang *et al.* [158].

Figure 4.2(b) shows the core level XPS spectra of Co-2p<sub>3/2</sub> and Co-2p<sub>1/2</sub> for the spinel Co<sub>2</sub>TiO<sub>4</sub>. If the distribution of ions in Co<sub>2</sub>TiO<sub>4</sub> is [Co<sup>2+</sup>][Co<sup>2+</sup>Ti<sup>4+</sup>]<sub>2</sub>O<sub>4</sub>, as has been assumed in previous studies, then this system should not exhibit any Co<sup>3+</sup> character. However, our XPS studies in Co<sub>2</sub>TiO<sub>4</sub> (figure 4.2b) show clear signatures of Co<sup>3+</sup> state in addition to the Co<sup>2+</sup> state in terms of doublets discussed above for Co<sub>3</sub>O<sub>4</sub>. For the XPS spectra of Co-2p<sub>3/2</sub> and Co-2p<sub>1/2</sub> levels, the simulated Gaussian-Lorentzian fitting yields two different intensity peaks with narrow separation labeled by P<sub>1</sub> and P<sub>2</sub> for 2p<sub>3/2</sub> and P<sub>3</sub> and P<sub>4</sub> for 2p<sub>1/2</sub> as shown in figure 4.2b. The observed difference between the doublets  $\Delta E_{P_1-P_3} = 14.98 \text{ eV}$  and  $\Delta E_{P_2-P_4} = 15.43 \text{ eV}$  provides the signatures of the Co<sup>3+</sup> and Co<sup>2+</sup> respectively, as compared to the expected values of  $\Delta E = 15.0 \text{ eV}$  for Co<sup>3+</sup> and  $\Delta E = 15.7 \text{ eV}$  for Co<sup>2+</sup>. On the other hand, for Co<sub>2</sub>SnO<sub>4</sub> case the data shown in figure 4.2c gives  $\Delta E = 15.7 \text{ eV}$  characteristic of Co<sup>2+</sup> only and no additional signatures for the Co<sup>3+</sup> state are noticed in Co<sub>2</sub>SnO<sub>4</sub> as discussed in the previous chapter.

Next, we discuss the electronic states of ‘Ti’, ‘Sn’ and ‘O’. For TiO<sub>2</sub> with ‘Ti<sup>4+</sup>’ as the electronic state of titanium, binding energy for the Ti-2p<sub>3/2</sub> state is observed at 459.5 eV [127]. However, in the case of Co<sub>2</sub>TiO<sub>4</sub> the maximum intensity peak for Ti-2p<sub>3/2</sub> appears at 457.65 eV (figure 4.2d), while the second maximum intensity

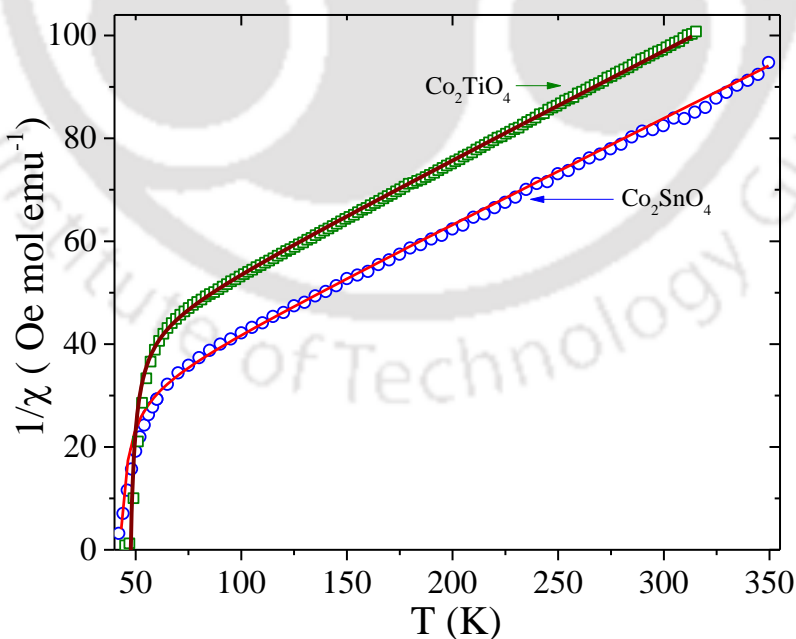


**Figure 4.2:** The left hand side panel shows the X-ray photoelectron spectra (XPS) of Co-2*p* peaks of (a)  $\text{Co}_3\text{O}_4$  (b)  $\text{Co}_2\text{TiO}_4$ , and (c)  $\text{Co}_2\text{SnO}_4$ . Whereas, right hand side panel shows the XPS spectra of (d) Ti-2*p* (e) Sn-3*d*, and (f) O-1*s* peaks of  $\text{Co}_2\text{TiO}_4$ ,  $\text{Co}_2\text{SnO}_4$ ,  $\text{Co}_3\text{O}_4$  bulk systems.

peak corresponding to Ti-2*p*<sub>1/2</sub> is centered at 463.53 eV. This result rules out the presence of Ti<sup>4+</sup> state in  $\text{Co}_2\text{TiO}_4$ . Instead the observed position of the peak at 457.65 eV agrees with the previously reported data of Ti<sup>3+</sup> surface defects at 457.7 eV in TiO<sub>2</sub> system [159]. In addition, these results also rule out the presence of any metallic ‘Ti’ ions in  $\text{Co}_2\text{TiO}_4$  matrix which usually show their signatures in XPS spectra at 454 eV. For  $\text{Co}_2\text{SnO}_4$ , the sharp peaks observed at 485.65 eV and 494.8 eV and a weak shoulder at 496.75 eV in figure 4.2(e) are the characteristic signatures of Sn<sup>4+</sup> state [111, 112]. Finally, figure 4.2(f) shows O-1*s* core level spectra for all the three systems with some signature of weakly bound surface oxygen at binding energy close to 533 eV [112 - 114, 158, 160, 161]. The major conclusions from these comparative XPS studies in  $\text{Co}_3\text{O}_4$ ,  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  are that electronically,  $\text{Co}_2\text{TiO}_4 = [\text{Co}^{2+}][\text{Co}^{3+}\text{Ti}^{3+}]\text{O}_4$  whereas  $\text{Co}_2\text{SnO}_4 = [\text{Co}^{2+}][\text{Co}^{2+}\text{Sn}^{4+}]\text{O}_4$ . This difference in the electronic state of ‘Co’ ions on the B-sites of these two systems has never been reported before, and, as we will show, it leads to major differences in the observed magnetic properties of  $\text{Co}_2\text{TiO}_4$  from those of  $\text{Co}_2\text{SnO}_4$ .

### 4.3.3 Temperature Dependence of the DC-Magnetic Susceptibility:

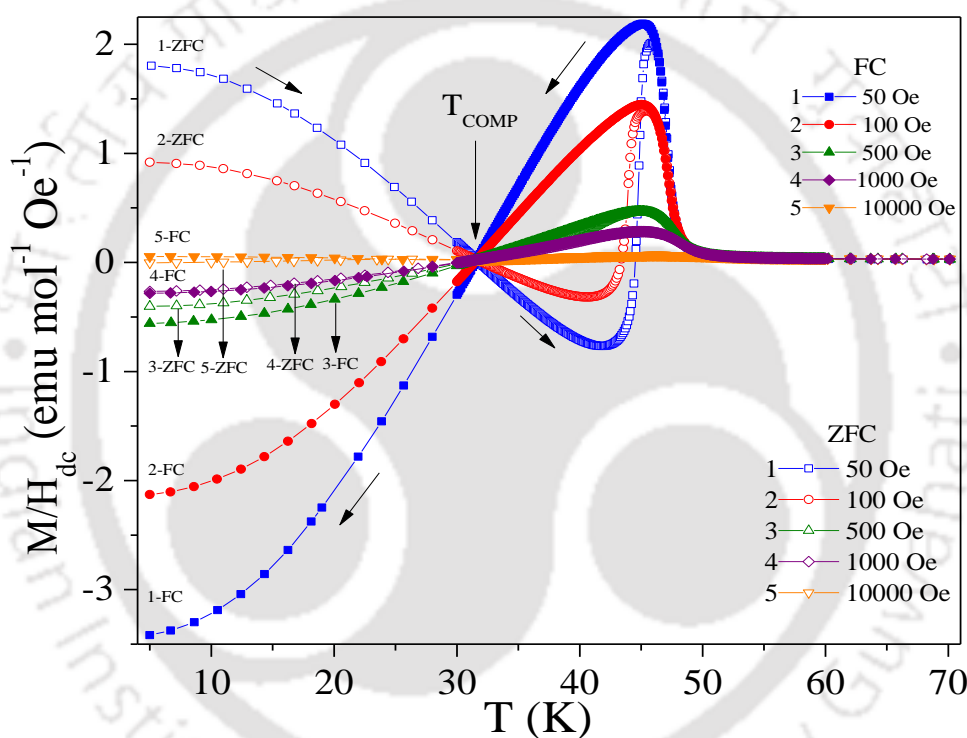
The temperature dependence of inverse paramagnetic susceptibility ( $\chi^{-1}(T)$ ) of both  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  for  $T > 45$  K recorded under zero field cooled (ZFC) conditions is shown in figure 4.3. The blue circles and olive squares represents experimental points and red and brown solid lines as fits to the Néel expression for ferrimagnets viz.  $(1/\chi) = (T/C) + (1/\chi_0) - [\sigma_0/(T - \theta)]$ . The fit for  $\text{Co}_2\text{TiO}_4$  yields the following parameters:  $\chi_0 = 41.92 \times 10^{-3}$  emu/mol-Oe,  $\sigma_0 = 31.55$  mol-Oe-K/emu,  $C = 5.245$  emu-K/mol-Oe,  $\theta = 49.85$  K. The ratio  $C/\chi_0 = T_a = 125.1$  K represents the strength of the antiferromagnetic exchange coupling between the spins on the A and B sites, and is often termed as the asymptotic Curie Temperature  $T_a$ . In Table 4.2, various fitting parameters obtained from the Néel expression for ferrimagnetism of both  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  are summarized. The effective magnetic moment  $\mu_{\text{eff}} = 6.5 \mu_B$  per formula unit (f.u.) of  $\text{Co}_2\text{TiO}_4$  is determined using  $C = N\mu_{\text{eff}}^2/3k_B$ . A similar calculation yielded  $\mu_{\text{eff}} = 6.25 \mu_B$  per f.u. of  $\text{Co}_2\text{SnO}_4 = [\text{Co}^{2+}][\text{Co}^{2+}\text{Sn}^{4+}]\text{O}_4$ . Using  $\mu_{\text{eff}}^2 = [\mu(A)]^2 + [\mu(B)]^2$  with  $\mu(A) = 3.87 \mu_B$  for  $\text{Co}^{2+}$  ions on the A-sites with spin  $S = 3/2$  and  $g = 2$  since its tetrahedral co-ordination does not allow orbital contribution, yields  $\mu(B) = 4.91 \mu_B$  for  $\text{Co}_2\text{SnO}_4$ . This argument for  $\text{Co}_2\text{SnO}_4$  yields ferrimagnetism below ' $T_N$ ' with net small moment of  $1.04 \mu_B$  per f.u. For  $\text{Co}_2\text{TiO}_4$  with the electronic configuration of  $[\text{Co}^{2+}][\text{Co}^{3+}\text{Ti}^{3+}]\text{O}_4$  determined using XPS, the above analysis yields  $\mu_{\text{eff}} = 6.5 \mu_B$  per f.u. Again using  $\mu(A) = 3.87 \mu_B$  for  $\text{Co}^{2+}$  ions on the A-site as in  $\text{Co}_2\text{SnO}_4$ , yields  $\mu(B) = 5.19 \mu_B$  for ions on the B-site. The trivalent titanium ions  $\text{Ti}^{3+}$  with its  $3d^1$  electronic configuration has magnetic moment  $\mu = 1.73 \mu_B$  yielding  $\mu(\text{Co}^{3+}) = 4.89 \mu_B$  as the moment for the  $\text{Co}^{3+}$  ion on the B-site. In the high spin state,  $\text{Co}^{3+}$  ions should have spin only  $\mu = 4.9 \mu_B$  which agrees with the above estimate.



**Figure 4.3.** Temperature variation of the inverse paramagnetic susceptibility  $\chi^{-1}(T)$  of  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  systems. The solid lines are best-fits to the Néel's expression for ferrimagnets discussed in the section 4.3.3.

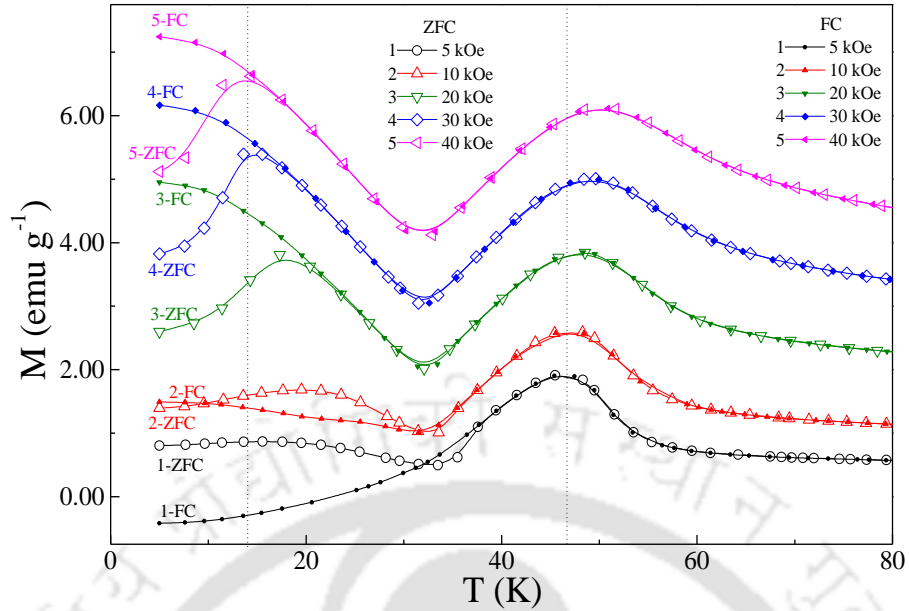
**Table 4.2:** The list of various parameters obtained from the Néel fits of  $\chi^{-1}$  versus T curve recorded under zero-field-cooled condition.

System	C (emu K mol <sup>-1</sup> Oe <sup>-1</sup> )	$\chi_0$ (emu mol <sup>-1</sup> Oe <sup>-1</sup> )	$\sigma_0$ (emu <sup>-1</sup> Oe mol K)	$\theta$ (K)	$\mu_{\text{eff}}$ ( $\mu_B$ )	$\mu$ (A) ( $\mu_B$ )	$\mu$ (B) ( $\mu_B$ )
$\text{Co}_2\text{TiO}_4$	5.245	0.0419	31.55	49.85	6.5	3.87	5.19
		$N_{AA}$	$N_{AB}$	$N_{BB}$	$J_{AA}$	$J_{AB}$	$J_{BB}$
		17.319	35.700	12.720	3.25 k <sub>B</sub>	4.47 k <sub>B</sub>	3.18 k <sub>B</sub>
$\text{Co}_2\text{SnO}_4$	4.889	0.0436	102.370	39.5	6.25	3.87	4.91
		$N_{AA}$	$N_{AB}$	$N_{BB}$	$J_{AA}$	$J_{AB}$	$J_{BB}$
		21.564	33.201	10.678	4.05 k <sub>B</sub>	5.26 k <sub>B</sub>	4.28 k <sub>B</sub>



**Figure 4.4:** Temperature dependence of dc-magnetic susceptibility  $\chi(T)$  ( $= M/H_{\text{dc}}(T)$ ) for  $\text{Co}_2\text{TiO}_4$  measured under both zero-field-cooled (ZFC) and field-cooled (FC) conditions recorded at various magnetic fields in the range 50 Oe  $\leq H_{\text{dc}} \leq 10$  kOe.

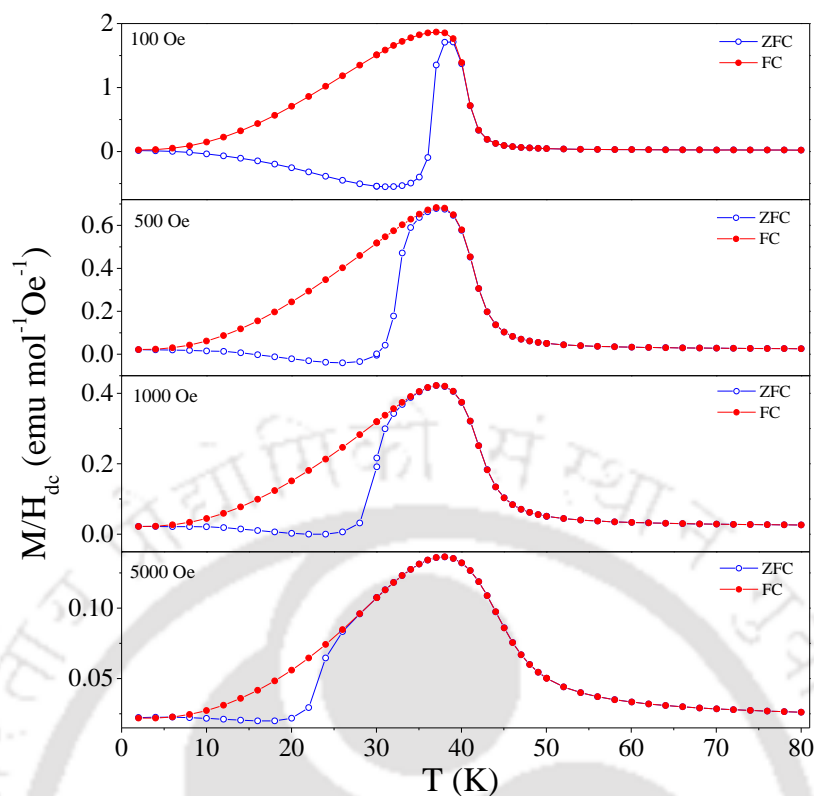
So an important conclusion from this comparative analysis of the paramagnetic susceptibilities is that  $\mu_{\text{eff}} = 6.5 \mu_B$  per f.u. of  $\text{Co}_2\text{TiO}_4$  is higher than that in  $\text{Co}_2\text{SnO}_4$ . This leads to the calculated net ferrimagnetic moment of  $\mu = 1.32 \mu_B$  per f.u. below  $T_N$  which is higher than  $\mu = 1.04 \mu_B$  per f.u. of  $\text{Co}_2\text{SnO}_4$  below its  $T_N$ . This information below is used to explain the observed differences in the measured magnetic properties of  $\text{Co}_2\text{TiO}_4$  against  $\text{Co}_2\text{SnO}_4$  below  $T_N$ . Another important difference between the two systems is that in  $\text{Co}_2\text{TiO}_4$ , the B-site is occupied by  $\text{Co}^{3+}$  and  $\text{Ti}^{3+}$  both of which have magnetic moments unlike the case of  $\text{Co}_2\text{SnO}_4$  in which the  $\text{Sn}^{4+}$  ion on the B-



**Figure 4.5:** High-field ( $5 \text{ kOe} \leq H_{dc} \leq 40 \text{ kOe}$ ) magnetization ( $M$ ) versus temperature ( $T$ ) data for  $\text{Co}_2\text{TiO}_4$  measured under both the ZFC and FC conditions.

site does not have a magnetic moment. Therefore, the effects of magnetic dilution should be less prominent in  $\text{Co}_2\text{TiO}_4$ . Figure 4.4 shows the temperature dependence of  $\chi_{dc}$  ( $= M/H_{dc}$ ) for  $H_{dc} = 50, 100, 500, 1000$  and  $10,000$  Oe of polycrystalline  $\text{Co}_2\text{TiO}_4$  sample. The data are shown for both the traditional ZFC and FC cases. The significant features of the data are: (a)  $\chi$  peaking at a temperature near 46 K suggesting ferrimagnetic ordering, and (b) a crossover in sign for  $\chi(\text{ZFC})$  and  $\chi(\text{FC})$  at a compensation temperature near 32 K where the magnetization of the two sublattices balance each other. These observations are similar to those reported by Hubsch *et al.* in  $\text{Co}_2\text{TiO}_4$  and are discussed in more detail later [77]. The temperature dependence of the magnetization ( $M$ ) for the ZFC and FC cases under applied  $H_{dc} = 5, 10, 20, 30$  and  $40 \text{ kOe}$  is shown in figure 4.5.

Several features of the data are noteworthy: (i) the compensation temperature  $T_{\text{COMP}} \approx 32 \text{ K}$  is independent of applied  $H_{dc}$  and compensation is not complete, in that  $M$  at  $T_{\text{COMP}}$  is not zero but increases with increase in  $H_{dc}$ , (ii) the position of the peak temperature near 46 K shifts slightly to higher temperatures with increase in  $H_{dc}$ , and (iii) the temperature for which  $M(\text{FC})$  bifurcates from  $M(\text{ZFC})$  shifts to lower temperature with increase in  $H_{dc}$ . Very similar features have been recently observed in another spinel Ni-Fe-Sb-O spinel [161]. In order to compare the above observations in  $\text{Co}_2\text{TiO}_4$  with similar measurements in  $\text{Co}_2\text{SnO}_4$ , new  $M/H_{dc}$  data on  $\text{Co}_2\text{SnO}_4$  is shown in figure 4.6 for the ZFC and FC cases in  $H_{dc} = 100, 500, 1000$  and  $5000 \text{ Oe}$ . Although there are some similarities with the data for  $\text{Co}_2\text{TiO}_4$  in figure 4.4, the behavior near the compensation temperature of 32 K in  $\text{Co}_2\text{TiO}_4$  is not observed in  $\text{Co}_2\text{SnO}_4$ . Instead, there is a bifurcation of the FC and ZFC data beginning near 7 K which is field-independent, and a second bifurcation at higher temperatures, the location of which is field-dependent. More information on these differences between the two systems become evident from the behavior of the hysteresis loop parameters in consonance with ac-magnetic susceptibility data which will be discussed in subsequent sections



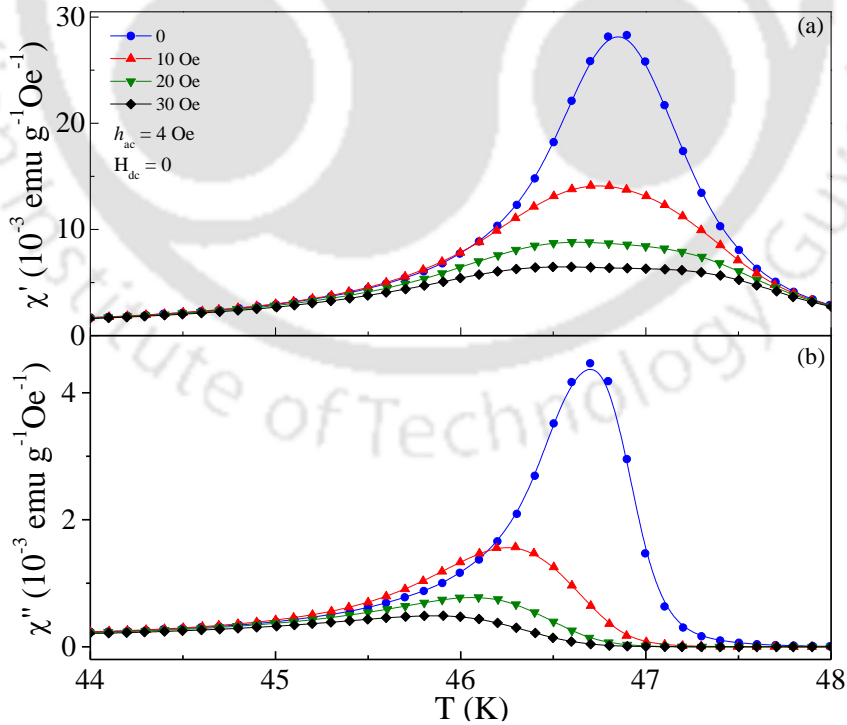
**Figure 4.6.** Temperature dependence of dc-magnetic susceptibility  $\chi(T)$  ( $= M/H_{dc}(T)$ ) for  $\text{Co}_2\text{SnO}_4$  measured under both zero-field-cooled (ZFC) and field-cooled (FC) conditions recorded at various magnetic fields.

The paper by Hubsch *et al.* [77] on the nature of magnetic ordering in  $\text{Co}_2\text{TiO}_4$  reported  $T_N = 55$  K followed by a spin-glass ordering at  $T_{SG} = 46$  K. However, between 55 K and 46 K, the remanence magnetization  $M_R$  was extremely small reaching a peak value of only about 0.05  $\text{emu/g}$  at 50 K, and then becoming zero again at 46 K. Below 46 K, the  $M_R$  increased rapidly, peaking at  $M_R = 0.7$   $\text{emu/g}$  at 40 K before compensation sets in. In the specific-heat  $C_P$  versus  $T$  measurements of Ogawa *et al.* [80] a peak in  $C_P$  is observed only near 48 K, although under non-zero applied  $H_{dc}$ , this feature becomes more diffused and shifts to higher temperatures. The phenomenon of compensation observed near 32 K, in figure 4.4 and figure 4.5, confirms the earlier observation of Hubsch *et al.* [77] However, the compensation in  $\text{Co}_2\text{TiO}_4$  is not complete because the magnetization measured at the minimum is not quite zero, and, it increases with magnetic field. In ferrimagnets with different magnetic moments on the A- and the B-sites, and having different temperature dependence, a complete compensation or at least a minimum in the observed moment  $\mu(T) = \mu(A) - \mu(B)$  could occur at a certain temperature below  $T_N$ . The estimated magnetic moments on the A- and the B-sites of  $\text{Co}_2\text{TiO}_4$  are sufficiently different with  $\mu(A) = 3.87 \mu_B$  and  $\mu(B) = 5.19 \mu_B$  as discussed earlier in Section 4.3.3. For comparison, in  $\text{Co}_2\text{SnO}_4$  with smaller difference in  $\mu(A) = 3.87 \mu_B$  and  $\mu(B) = 4.91 \mu_B$ , compensation is not as evident and clear-cut but below about 7 K, there is effectively no remanence or coercivity implying compensation. Another evidence for the difference in the two systems in this regard is the difference in the measured remanence  $M_R$ . For  $\text{Co}_2\text{SnO}_4$ , maximum in  $M_R = 0.45$

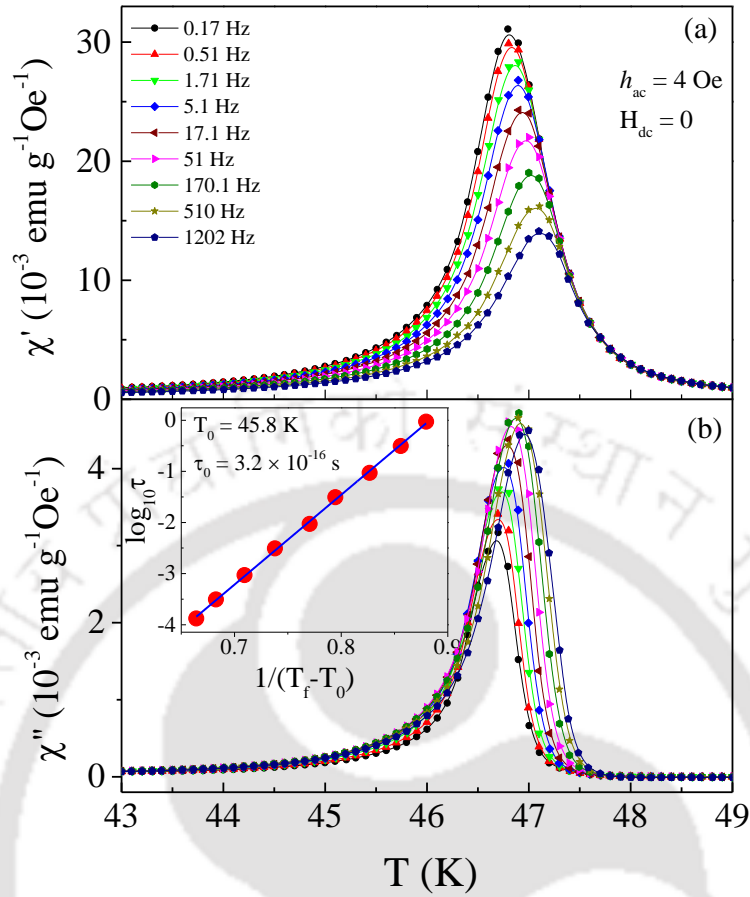
emu/g was observed near 30 K whereas, in Co<sub>2</sub>TiO<sub>4</sub>, maximum in M<sub>R</sub> = 3 emu/g observed near 10 K, which was larger by a factor of about six (will be discussed in section 4.3.5). The ratio of the observed M<sub>R</sub> in Co<sub>2</sub>TiO<sub>4</sub> and Co<sub>2</sub>SnO<sub>4</sub> scales well with the difference in their μ(A) and μ(B) values when normalized with their molecular weights.

**4.3.4 Temperature Dependence of the AC-Magnetic Susceptibilities:**

The temperature dependence of the ac-magnetic susceptibilities, χ'(T) and χ''(T), were measured using ac-magnetic field frequency (f<sub>m</sub>) of 2 Hz with amplitude h<sub>ac</sub> = 4 Oe superimposed with various 'dc' fields H<sub>dc</sub> between 10 Oe and 30 Oe. These results are shown in figure 4.7 in which one can clearly see the splitting of a single peak near 46.5 K into two peaks when H<sub>dc</sub> is increased. In the χ' versus T data, the higher temperature peak shifts toward higher temperature side with increase in H<sub>dc</sub>, whereas, the reverse is true for the lower temperature peak. The transition at 46.5 K was probed further by measuring temperature dependence of χ' and χ'' at nine different frequencies f<sub>m</sub> between 0.17 Hz and 1202 Hz using h<sub>ac</sub> = 4 Oe and H<sub>dc</sub> = 0 (figure 4.8). For χ', the peak at 46.8 K measured at the lowest frequency (0.17 Hz) shifts to higher temperatures with increase in frequency, approaching near 47.11 K at f<sub>m</sub> = 1202 Hz. This kind of frequency dependence of the peak-shift in the ac susceptibility curves are qualitatively similar to what we discussed in previous chapter for Co<sub>2</sub>SnO<sub>4</sub> system. However, a detailed quantitative analysis of the data revealed a marked difference between the two systems. As in the case of Co<sub>2</sub>SnO<sub>4</sub> (section 3.3.4), we tried to analyze the frequency dependence seen of χ'(T) and χ''(T) in Co<sub>2</sub>TiO<sub>4</sub> using both the

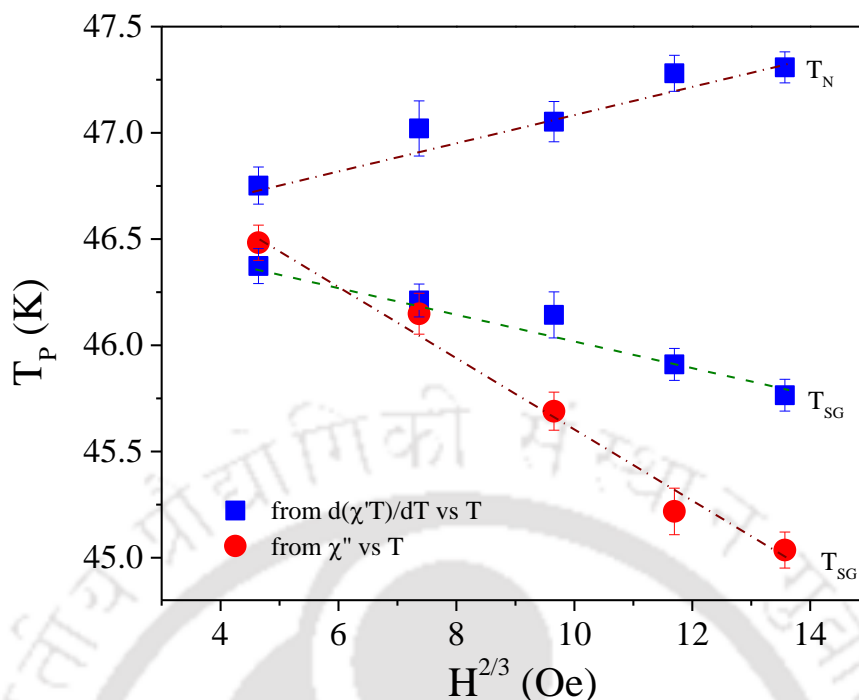


**Figure 4.7:** Temperature variation of the ac-magnetic susceptibility (a) χ'(T), and (b) χ''(T) for Co<sub>2</sub>TiO<sub>4</sub> measured at 2 Hz in h<sub>ac</sub> = 4 Oe with superposed dc-bias fields H<sub>dc</sub> = 0, 10, 20 and 30 Oe.



**Figure 4.8:** Temperature dependence of ac-magnetic susceptibilities (a)  $\chi'(T)$  and (b)  $\chi''(T)$  of  $\text{Co}_2\text{TiO}_4$  measured at various frequencies between 0.17 Hz and 1202 Hz under warming conditions using  $h_{ac} = 4$  Oe and  $H_{dc} = 0$  Oe. The inset shows the best fits of the relaxation times to the Vogel-Fulcher law in  $\text{Co}_2\text{TiO}_4$ .

scaling laws: (i) the Vogel-Fulcher law (VFL;  $\tau = \tau_0 \exp(E_a/k_B(T - T_0))$ ), where  $\tau_0$  is the relaxation time constant,  $T_0$  is a measure of the interaction between magnetic clusters,  $k_B$  is the Boltzmann constant and  $E_a$  is an activation energy parameter), and (ii) Power-law (PL) which describes the critical slowing down in a spin-glass phase transition at  $T_g$ , and is given by:  $\tau = \tau_0 ((T/T_g) - 1)^{-z\nu}$ , where  $T_g$  is the freezing temperature,  $\tau_0$  is related to the relaxation of the individual cluster magnetic moment and  $z\nu$  is a critical exponent. Here  $\tau = 1/\omega = 1/2\pi f$ . While for  $\text{Co}_2\text{SnO}_4$  case, (as discussed in section 3.3.4) we could obtain physically reasonable fit parameters using both the scaling laws albeit using a very limited temperature range, for  $\text{Co}_2\text{TiO}_4$  the situation is different. In inset of figure 4.8 (b), we show the best representation of the data that was obtained using the Vogel-Fulcher law, with  $T_0 = 45.8$  K and  $\tau_0 = 3.2 \times 10^{-16}$  s. However, an attempt to fit the data using the power-law, yielded quite unphysical values of the fit parameters (viz.  $\tau_0 \sim 10^{-33}$  s and  $z\nu > 16$ ), indicating the lack of proper spin-glass phase transition. Nonetheless, the main problem is the difficulty in deciding which law (either VFL or PL) is the best to decide the glassy nature. Souletie and Tholence in 1985 tried to resolve such exasperating aspect and found that the Power-law gives better accountability of the experimental evidence of glassy behavior [162]. As we obtained physically reasonable fit parameters for  $\text{Co}_2\text{TiO}_4$  using the VFL, however, PL gives quite unphysical values of the relaxation

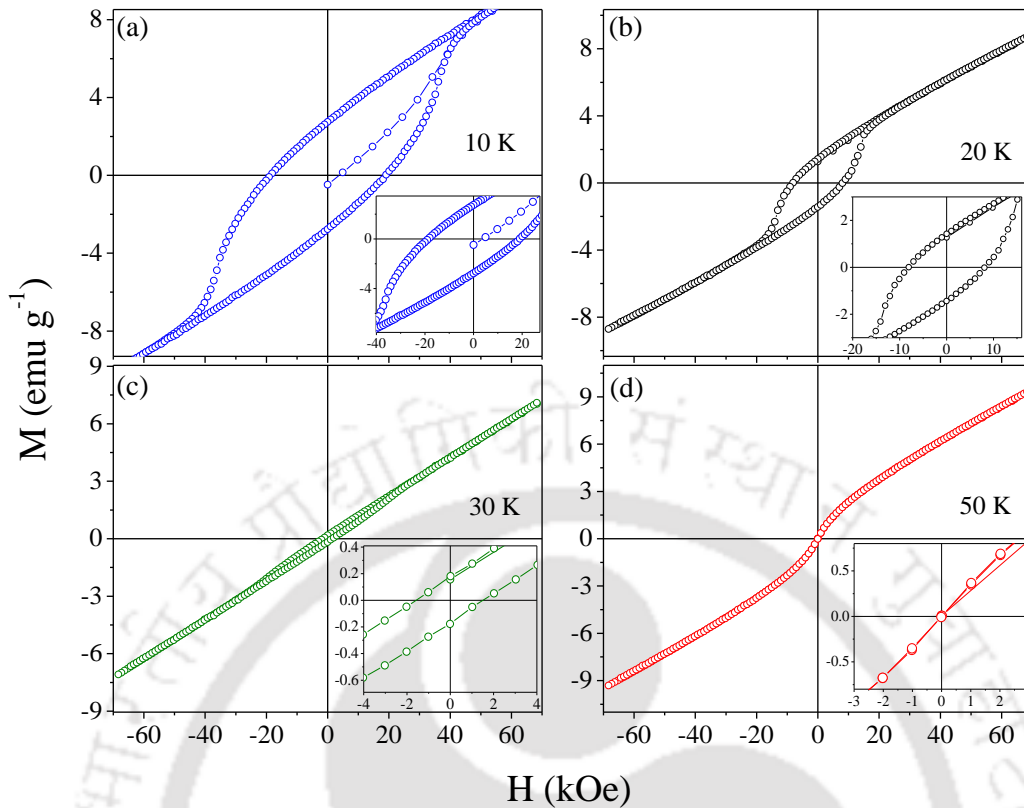


**Figure 4.9:** The de Almeida-Thouless (AT) line  $T_P$  versus  $H^{2/3}$  of  $\text{Co}_2\text{TiO}_4$ . The dotted lines show the linear fit to the experimental data. Inset shows the field dependence of  $T_{SG}$  raised to  $2/3$  power obtained from dc-susceptibility measurement.

time constant ( $\tau_0 = 10^{-33}$  s) and critical exponent ( $z\nu \sim 16$ ), indicating the lack of proper spin-glass transition. Although we saw systematic frequency dispersion of the peaks in  $\chi'(T)$  and  $\chi''(T)$  data and linear behavior in  $H^{2/3}$  versus  $T_P$  (A-T line) (figure 4.9), but, using the PL fitting we concluded that the  $\text{Co}_2\text{TiO}_4$  system exhibits pseudo-spin-glass properties rather than a proper real spin-glass ordering.

#### 4.3.5 Temperature Dependence of the Hysteresis Loop Parameters:

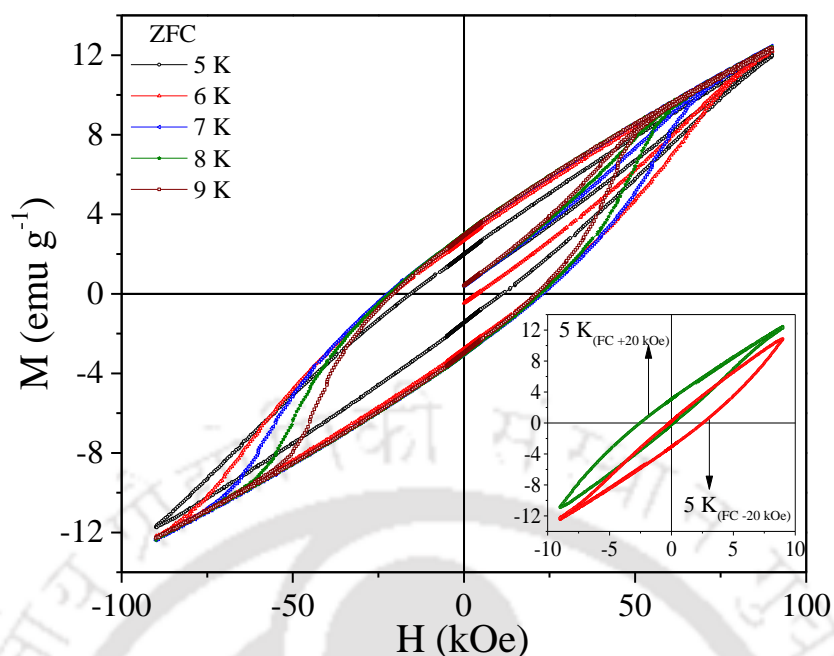
The five cycle  $M$  versus  $H$  hysteresis loop measurements were performed on  $\text{Co}_2\text{TiO}_4$  polycrystalline sample at selected temperatures between  $T = 5$  K and 60 K in the magnetic field from -90 kOe to +90 kOe. The measurements were done in the ZFC (FC) protocol in which the sample is cooled in  $H_{dc} = 0$  Oe ( $H_{dc} = 20$  kOe) from the paramagnetic state to the measuring temperature followed by measurements of  $M$  versus  $H$ . For the data at the next temperature, the sample was again warmed to the paramagnetic state and cooled back to the next measurement temperature. Hysteresis loops, at four selected temperatures, shown in figure 4.10, exhibits that a weak ferromagnetic component  $M_{WF}$  is superimposed on a linear component with  $M_{WF}$  strongly temperature dependent. The inset of the figure 4.11 shows asymmetry in the  $M$ - $H$  loops measured at 5 K under ZFC and FC ( $\pm 20$  kOe) protocol. We used the standard definition of the coercivity  $H_C = (H^+ - H^-)/2$ , loop-shift or Exchange-Bias  $H_{EB} = (H^+ + H^-)/2$  where  $H^+(H^-)$  are magnetic field values for which  $M = 0$ , and the remanence  $M_R$  for the magnetization at  $H = 0$  are used along with  $M_{MAX}$ , the measured magnetization at 90 kOe (shown in figure 4.12 a,b).



**Figure 4.10:** Magnetization versus field ( $M$ - $H$  hysteresis loops) of  $\text{Co}_2\text{TiO}_4$  are shown at selected temperatures of (a) 10 K, (b) 20 K, (c) 30 K and (d) 50 K recorded under zero-field-cooled (ZFC) condition. Insets show the zoomed view of  $M$ - $H$  loops near origin displaying the asymmetry in the loops.

Note that below 10 K, all the  $M$ - $H$  data appear like minor loops, thus, extracted magnitudes of  $H_C$ ,  $H_{EB}$ , and  $M_R$  are underestimated significantly. Due to this reason we have not shown the data for  $T < 10$  K. The noteworthy feature is the large magnitude of  $H_C \sim 20$  kOe at low-temperatures. In addition, there is a minimum in  $M_R$  and  $M_{MAX}$  at 30 K, the temperature for which partial compensation of the two-sublattices was indicated in figure 4.4 and figure 4.5. Observation of non-zero  $M_R$  is the evidence for the presence of  $M_{WF}$ .

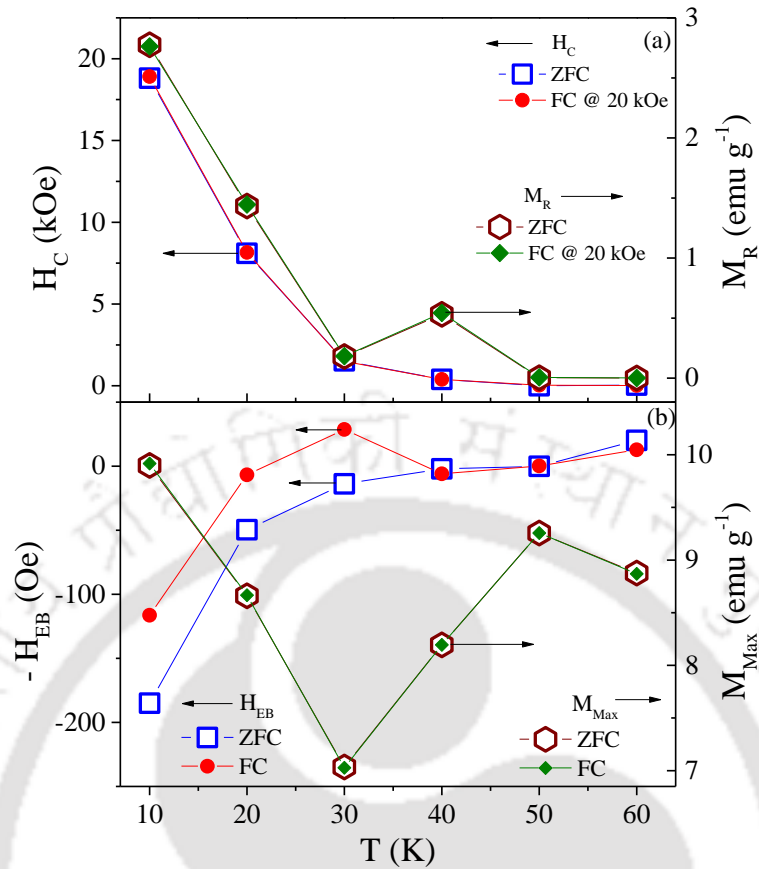
In the Stoner-Wohlfarth (SW) model of coercivity in single-domain particle,  $H_C = K_A/M_S$ , where  $K_A$  is the magneto-crystalline anisotropy constant and  $M_S$  is the saturation magnetization [124, 163]. Below  $T_N$ ,  $K_A \sim (M_S)^n$  where  $n$  is system dependent and can be as large as 10 [124, 163]. Therefore, in the SW model,  $H_C$  should continue to increase with decrease in temperature below  $T_N$ . In the plot of  $H_C$  versus  $T$  in figure 4.12a for  $\text{Co}_2\text{TiO}_4$ , an increase in  $H_C$  with a decrease in  $T$  is observed, reaching a peak at about 10 K below which  $H_C$  decreases and it is accompanied by the appearance of a very significant  $H_{EB}$ . In real systems,  $H_C$  is affected by impurities and grain boundaries which pin down the domain walls and prevent their rotation as the magnetic field is varied. The  $M$  versus  $T$  plot of figure 4.5 shows that below  $T_{COMP}$ , the FC and ZFC curves bifurcate at a certain temperature  $T_b$ , which decreases as  $H_{dc}$  increases. This is similar to the observation reported in Ni-hydroxide layered systems, [18, 164] where, this phenomenon was associated with the blocking temperature of nanocrystallites. In both  $\text{Co}_2\text{TiO}_4$



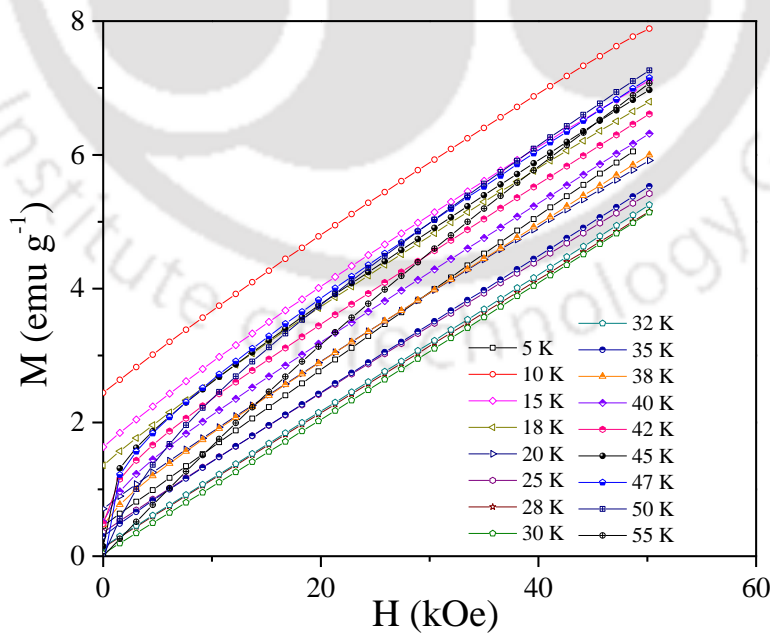
**Figure 4.11:** Magnetization versus field ( $M$ - $H$ ) hysteresis loops measured at low-temperatures  $T = 5$  K, 6 K, 7 K, 8 K and 9 K under zero-field-cooled (ZFC) condition. The insets show asymmetry in the  $M$ - $H$  loops measured at  $T = 5$  K under FC (20 kOe) condition.

and  $\text{Co}_2\text{SnO}_4$ , the crystallite size is in the  $\mu\text{m}$  range. However, because of the substitution of the different magnetic ions with different magnetic moments on the B-sites, the formation of magnetic clusters is very likely. The bifurcation of the  $M(\text{FC})$  and  $M(\text{ZFC})$  curves in figure 4.5 and 4.6, at a specific temperature  $T_b$ , which decreases with increase in  $H_{\text{dc}}$ , which could be due to freezing of these magnetic clusters. The observations of very large  $H_c$  and  $H_{\text{EB}}$  -like behavior at 10 K, in  $\text{Co}_2\text{TiO}_4$ , could be a result from the inability of the spins to follow magnetic field in the frozen clusters.

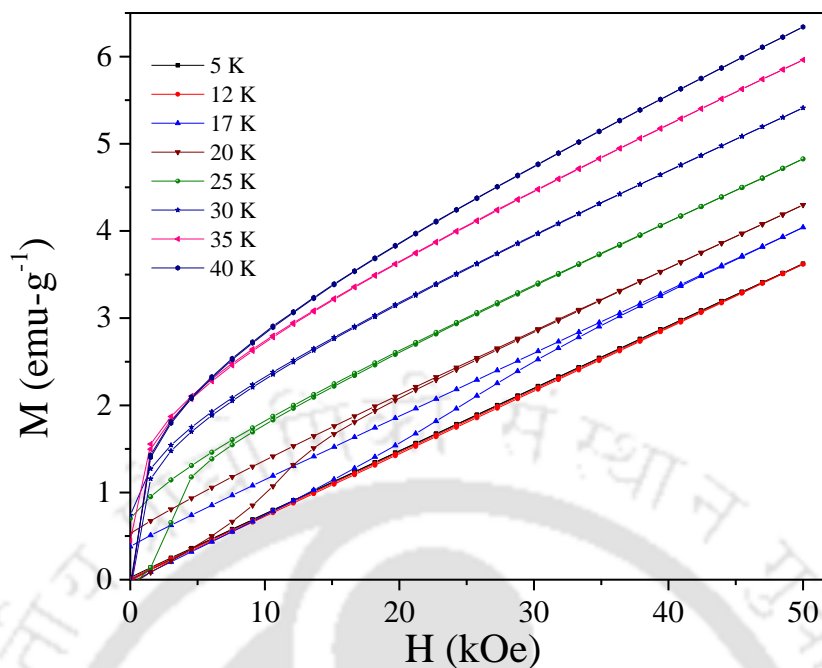
Another noteworthy result in  $\text{Co}_2\text{TiO}_4$  is the lack of saturation of the magnetization in  $H$  up to 90 kOe (figure 4.10 and 4.11). In the results reported by Hubsch *et al.* [77], lack of saturation was evident even up to 150 kOe. These results suggest a non-collinear ordering of spins in  $\text{Co}_2\text{TiO}_4$ . Preliminary neutron diffraction measurements by Hubsch *et al.* [77] reported an evidence for the canting of the spins, which is consistent with non-saturation of the magnetization. Qualitatively, this situation may be akin to that in the spinel  $\text{Mn}_3\text{O}_4$ , for which, the two sublattices were found to be inadequate to describe the magnetic structure below  $T_N$  [138]. In  $\text{Co}_2\text{TiO}_4$ , the B-sites are occupied by two different magnetic ions,  $\text{Co}^{3+}$  and  $\text{Ti}^{3+}$ , as reported here; therefore, at least a three-sublattice model is necessary to describe its magnetic structure. Srivastava *et al.* discussed a three-sublattice model in which magnitudes of the saturation magnetization and temperature dependence of paramagnetic susceptibility were used to solve for the exchange constants [165]. Since in  $\text{Co}_2\text{TiO}_4$ , magnetization does not saturate even up to 150 kOe as noted above, this model cannot be applied to  $\text{Co}_2\text{TiO}_4$ . Thus determining the nature of magnetic ordering of the spins below  $T_N$  in  $\text{Co}_2\text{TiO}_4$  remains an outstanding challenge, both experimentally and theoretically.



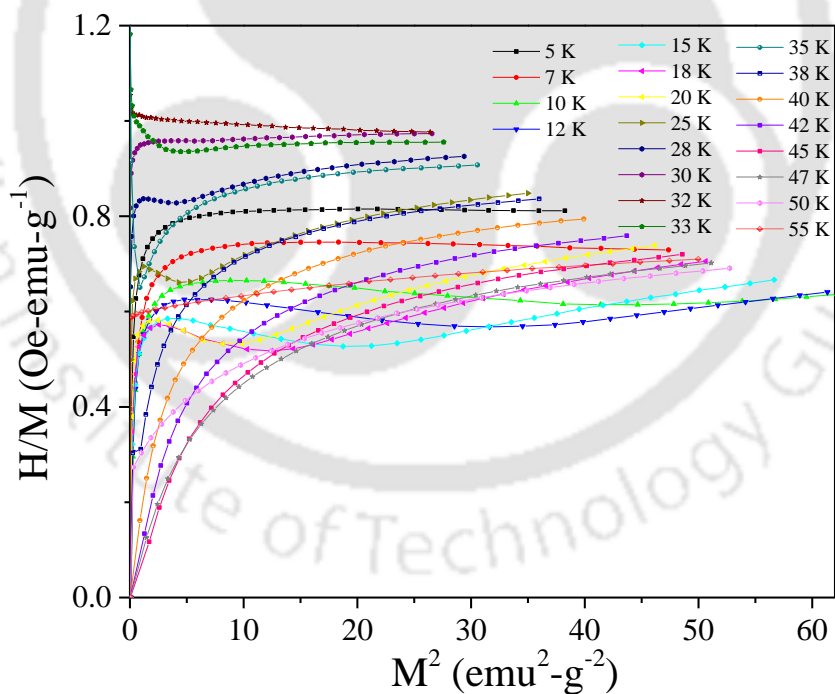
**Figure 4.12:** The temperature variation of (a) coercive field  $H_C(T)$  and Remanence Magnetization  $M_R$  and (b) exchange bias  $H_{EB}(T)$  and high field ( $H \sim 90$  kOe) magnetization  $M_{MAX}$  measured under both ZFC and FC(20 kOe) conditions in  $\text{Co}_2\text{TiO}_4$ . The lines connecting the data points are visual guides.



**Figure 4.13:** The magnetization versus field ( $M$ - $H$ ) isotherms of  $\text{Co}_2\text{TiO}_4$  recorded at various temperatures  $5 \text{ K} \leq T \leq 55 \text{ K}$ .

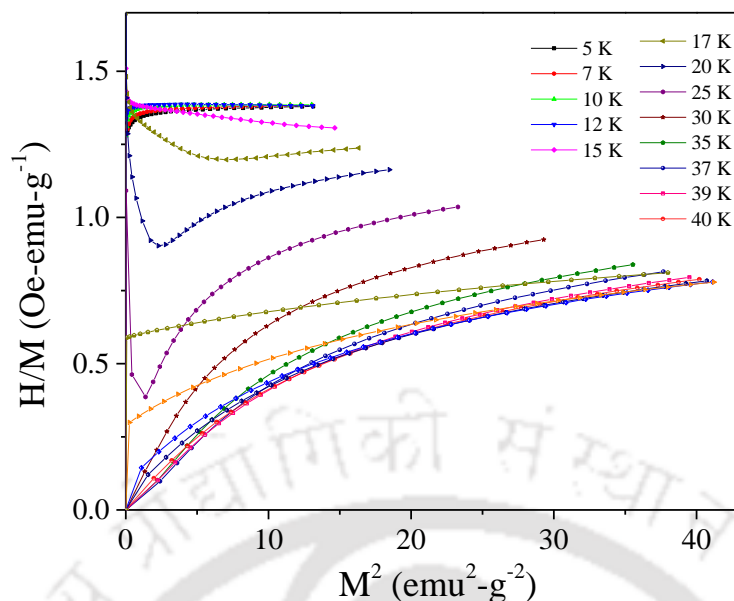


**Figure 4.14:** The magnetization versus field (M-H) isotherms of  $\text{Co}_2\text{SnO}_4$  recorded at various temperatures  $5 \text{ K} \leq T \leq 40 \text{ K}$ .



**Figure 4.15:** Arrott plots ( $H/M$  versus  $M^2$ ) of  $\text{Co}_2\text{TiO}_4$  computed from magnetization (M) field (H) isotherms recorded at different temperatures between 5 K and 55 K.

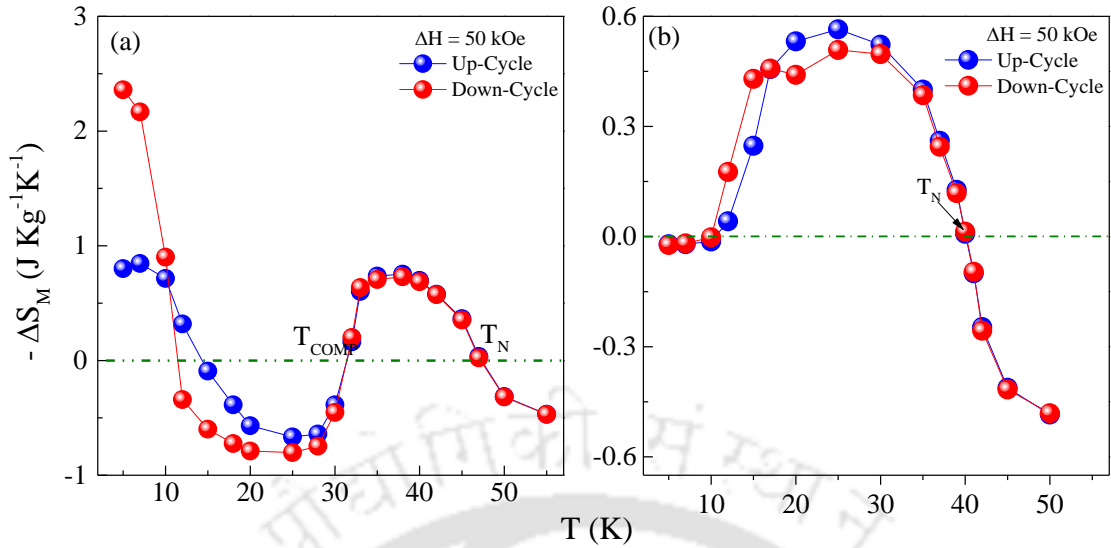
In order to understand the nature of magnetic transitions we plotted the ratio of magnetic field (H) to the value of magnetization (M) versus square of the magnetization ( $H/M$  versus  $M^2$ ) curves. These curves are commonly



**Figure 4.16:** Arrott plots ( $H/M$  versus  $M^2$ ) of  $\text{Co}_2\text{SnO}_4$  computed from magnetization ( $M$ ) field ( $H$ ) isotherms recorded at different temperatures between 5 K and 40 K.

known as Arrott plots. These parameters were extracted from the isothermal magnetization (1<sup>st</sup> quadrant  $M$ - $H$ ) curves recorded at various temperatures in the range of 5 – 48 K (figure 4.13 and 4.14) for both  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  (as depicted in figure 4.15 and 4.16). During the measurement of each  $M$ - $H$  isotherms, the temperature was brought to 300 K to ensure that the measurement should begin from a virgin magnetic state without any magneto-thermal history, followed by a zero-field cooling. Also, the temperature difference ( $\delta T$ ) between the two successive isotherms was set low in the region of the transition, whereas,  $\delta T$  was kept high for  $T > T_{\text{COMP}}$ . The magnetization values were recorded by increasing the magnetic field from zero to 50 kOe. A significant deviation from positive slope of the Arrott plots can be clearly seen in the region  $T \leq T_{\text{COMP}} \leq T_{\text{N}}$  (figure 4.15). In particular, the isotherms recorded between 5 K and 32 K show negative slopes in the  $H/M$  versus  $M^2$  plots confirming the magnetic field induced first-order discontinuous transition across 5-32 K consistent with the behavior of low-field  $\chi_{\text{dc}}(T)$  plots discussed above.

The Arrott plots criterion successfully explains the nature of transitions in both isolated and mixed phase systems with sequential phase changes [166, 167]. Its applicability for the first-order phase transition replicates the fact that the magnetization value remains almost constant at low fields, and an abrupt jump in the magnetization value (metamagnetic-like character) occurs at a critical field called transition field ( $H_{\text{T}}$ ), which corresponds to the point of maximum slope in the magnetization isotherm [166 - 170]. In the case of structurally coupled transitions, which are sensitive to the applied magnetic field,  $H_{\text{T}}$  gradually decreases with increasing temperature, and approaches to zero-near  $T_{\text{N}}$  [171]. Deviation from negative slopes are clearly noticeable on approaching the magnetically ordered regime  $32 \text{ K} \leq T \leq 48 \text{ K}$ , indicating the second-order nature of the transition across Néel temperature ( $T_{\text{N}}$ ) (figure 4.16).



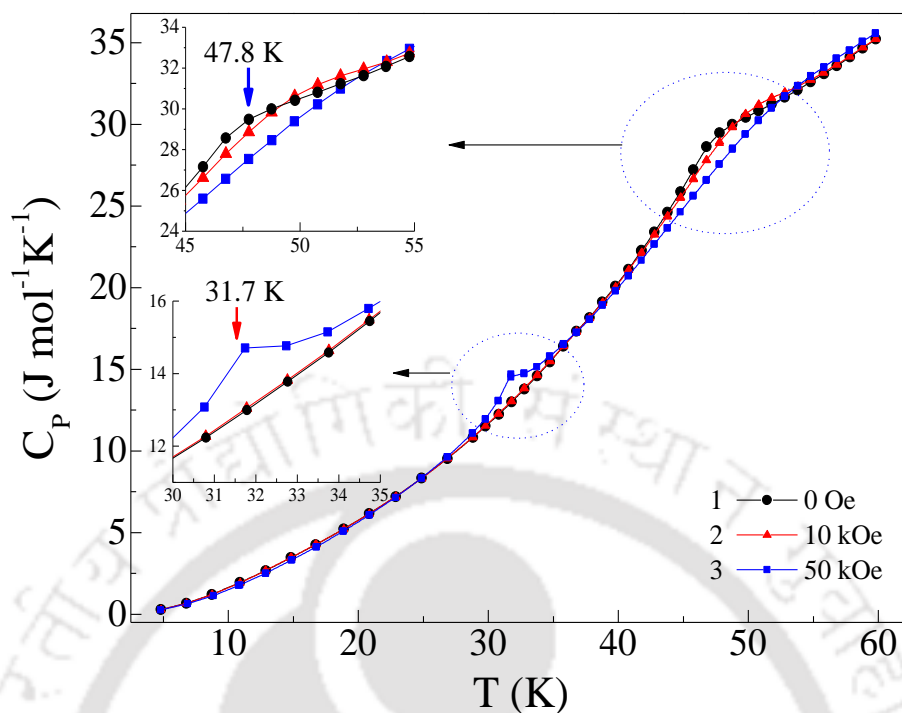
**Figure 4.17:** Temperature dependence of isothermal entropy change ( $\Delta S(T)$ ) computed from M-H isotherms using Maxwell equations for a field change  $\Delta H = 50$  kOe for (a)  $\text{Co}_2\text{TiO}_4$  (b)  $\text{Co}_2\text{SnO}_4$ .

Using the M-H isotherms, magnetic field-induced isothermal entropy changes ( $\Delta S$ ) were derived from the Maxwell equation:  $(\partial S/\partial H)_T = (\partial M/\partial T)_H$ . The temperature dependence of  $\Delta S$  associated to a magnetic field change  $\Delta H$  from 0 to 50 kOe was derived from the following formula:  $\Delta S(T, H) = \partial/\partial T \int M(T, H') dH'$ .

Figures 4.17 (a) and (b) show the temperature variation of isothermal magnetic-entropy changes  $\Delta S_M(T)$ . From the figure 4.17(a) one can clearly noticed the zero-crossover of  $\Delta S_M(T)$  across the  $T_N$  and  $T_{\text{COMP}}$ . Interestingly, the sign change of  $\Delta S_M(T)$  below 10 K is consistent with the first-order-like behaviour noticed from Arrott plots analysis. Such a polarity reversal of  $\Delta S_M(T)$ , sudden drop in the remanent-magnetization values  $M_R$  (figure 4.12a), and sign-reversal exchange-bias  $H_{\text{EB}}$  (figure 4.12b) below the compensation point, is believed to have a common origin associated with the pseudo first-order-like transition observed in both  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  (figure 4.17 (a) and (b)). However,  $\Delta S_M(T)$  for  $\text{Co}_2\text{SnO}_4$  shows a zero-crossover only across  $T_N$  similar trend as that of  $\text{Co}_2\text{TiO}_4$  except no zero-crossover (sign-change) below  $T_N$ , because, the compensation behaviour appears in  $\text{Co}_2\text{SnO}_4$  only in the range 5-10 K.

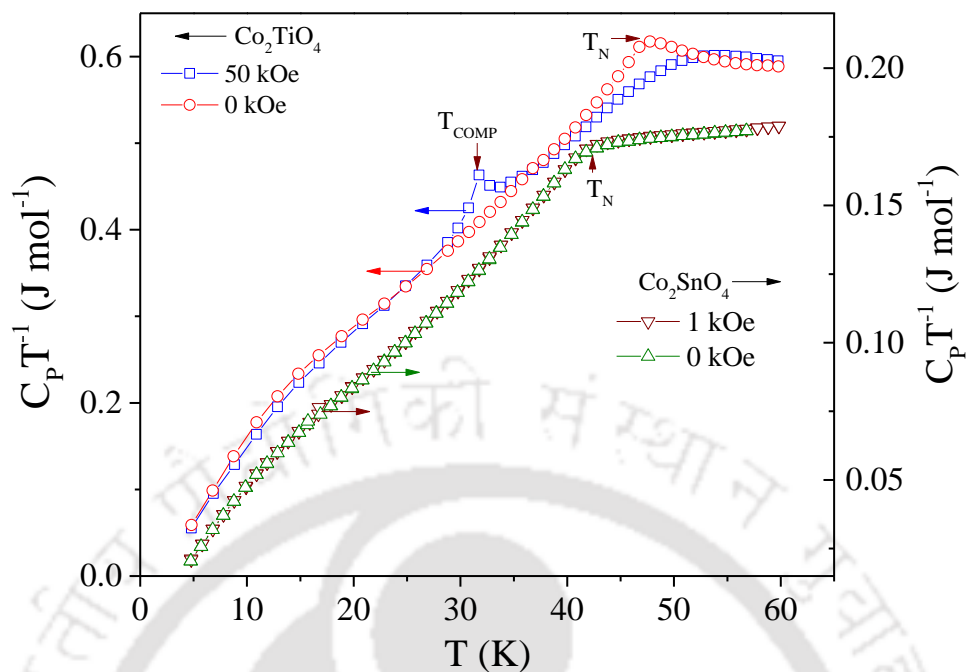
#### 4.3.6 Temperature Dependence of Specific-heat:

The plots of the temperature dependence of the specific heat  $C_p(T)$  of  $\text{Co}_2\text{TiO}_4$  measured in  $H_{\text{dc}} = 0, 10$  kOe and 50 kOe are shown in figure 4.18. From 5 K to 28 K, the data were taken at temperature intervals of 2 K and from 28 K to 60 K in steps of 1 K. In  $H_{\text{dc}} = 0$  Oe, a single shoulder in  $C_p$  versus T is observed at  $T_N = 47.8$  K, very similar to the earlier studies by Ogawa and Waki [80]. In applied field of 10 kOe and 50 kOe, this peak becomes diffused and shifts by a few degrees to higher temperatures (as seen in the inset of figure 4.18). Interestingly, another peak is observed at 31.7 K when  $H_{\text{dc}} = 50$  kOe suggesting some relationship of this peak with the compensation temperature noted above from M versus T data in figure 4.4 and 4.5.

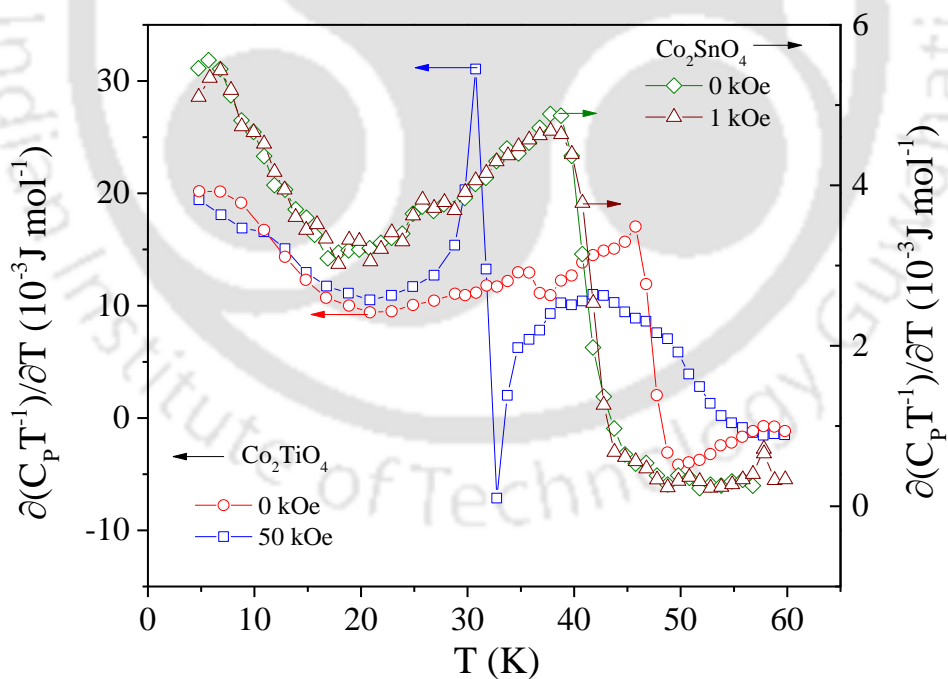


**Figure 4.18:** The temperature variation of specific-heat  $C_P(T)$  for  $\text{Co}_2\text{TiO}_4$  sample recorded at various magnetic fields ( $H_{dc} = 0, 10,$  and  $50$  kOe). The insets show the zoomed view across the ferrimagnetic Néel temperature ( $T_N$ ) and compensation temperature ( $T_{COMP}$ ).

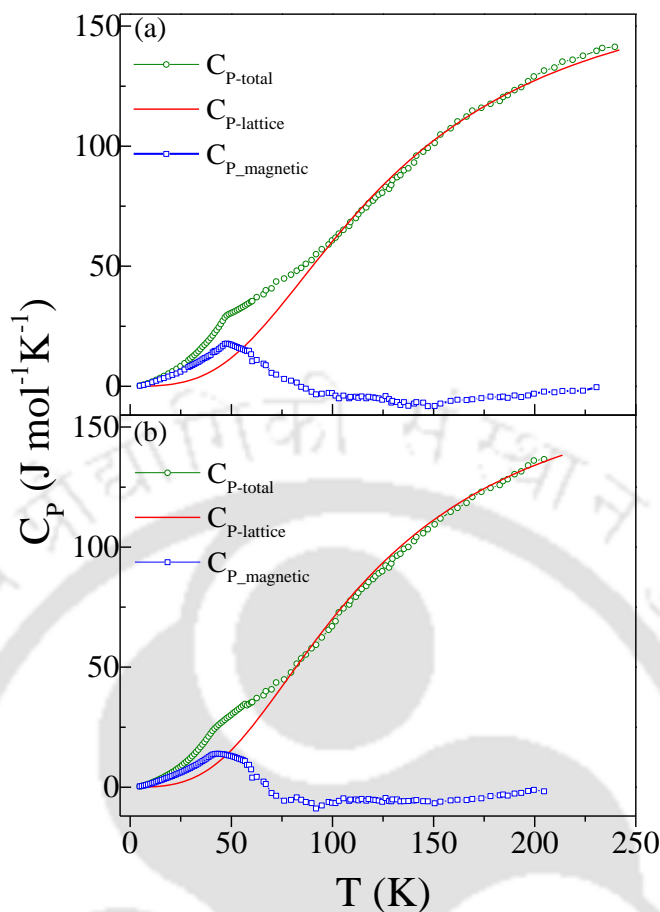
Figure 4.19 depicts the  $C_P T^{-1}$  versus  $T$  in the presence of  $H = 0$  Oe and  $50$  kOe for  $\text{Co}_2\text{TiO}_4$  and  $H = 0$  Oe and  $1$  kOe for  $\text{Co}_2\text{SnO}_4$  (S1350), respectively. We noticed clear changes in  $C_P T^{-1}$  versus  $T$  data for  $T < 50$  K for both  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  suggesting the entropy loss due to spin-glass-like ordering starting near to  $T_{SG}$ . The zero-field  $C_P T^{-1}$  data shows a weak hump across the  $T_N$ , and without any signatures of  $T_{COMP}$ . However, after applying the field, a sharp transition across  $T_{COMP}$  emerged with complete suppression of the hump observed across  $T_N$ . There is a one-to-one concurrence between the location of these anomalies, and, the sharp transitions noticed in  $\chi_{dc}(T)$  data at  $45$  K and  $31.7$  K. Nevertheless, no significant measurable difference was observed in the  $C_P T^{-1}$  values measured at  $H = 0$  and  $50$  kOe except the emergence of  $T_{COMP}$ , and disappearance of weak anomaly across  $T_N$ . The fact that peak in ' $C_P T^{-1}$ ' at ' $T_N$ ' in  $H = 0$  is quite weak compared to peaks observed in typical second order transitions in 3D systems, is due to unconventional ordering in  $\text{Co}_2\text{TiO}_4$  (lack of proper long-range order and presence of spin-glass-like features). Therefore, the absence of sharp peak in the  $C_P T^{-1}(T)$  is a well-known characteristic feature of the existence of disordered spin configuration, and proof to the existence of spin-glass nature [150]. Nonetheless, a rapid decrease in  $C_P T^{-1}$  with decreasing  $T$  beginning near  $15$  K, indicating further changes in the magnetic ordering of the system as noticed from the Arrott plot analysis. These anomalies are clearly evident in the computed plots of  $\partial(C_P T^{-1})/\partial T$  versus  $T$  (figure 4.20).



**Figure 4.19:** Temperature variation of  $C_P T^{-1}$  measured in the presence of  $H = 0$  Oe and 50 kOe for  $\text{Co}_2\text{TiO}_4$  (LHS) and  $H=0$  Oe and 1 kOe for  $\text{Co}_2\text{SnO}_4$  (RHS).



**Figure 4.20:** Temperature variation of  $\partial(C_P T^{-1})/\partial T$  versus  $T$  measured in the presence of  $H = 0$  Oe and 50 kOe for  $\text{Co}_2\text{TiO}_4$  (LHS) and  $H = 0$  Oe and 1 kOe for  $\text{Co}_2\text{SnO}_4$  (RHS).

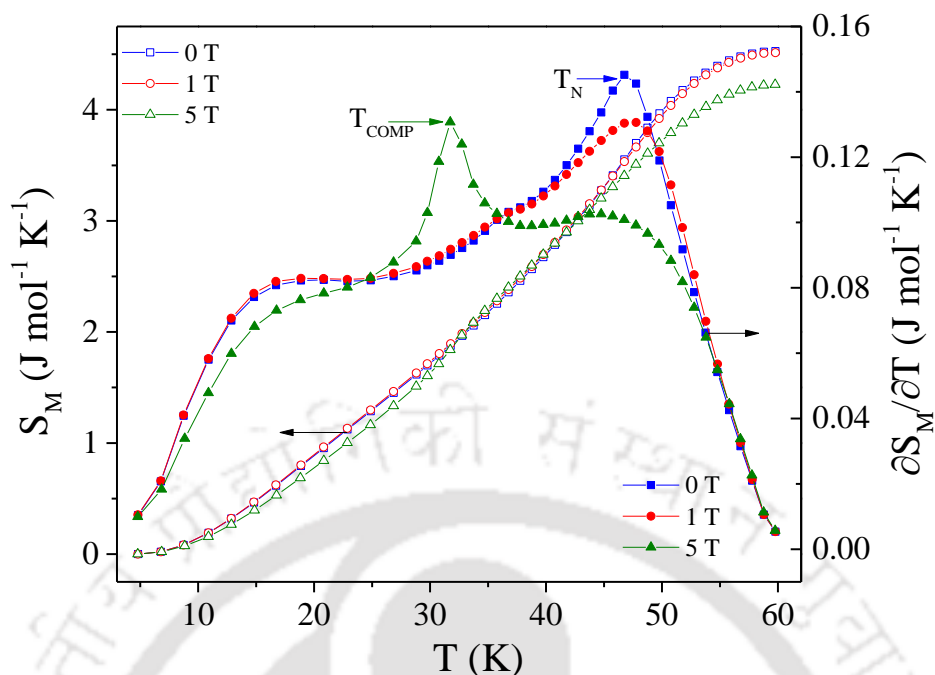


**Figure 4.21:** Temperature dependence of experimentally obtained zero-field heat capacity data of (a)  $\text{Co}_2\text{TiO}_4$  and (b)  $\text{Co}_2\text{SnO}_4$  shown in green color open circles together with the red color solid line represents the specific heat calculated from numerical fits as described in the text and blue hollow square symbols represents the magnetic contribution to the specific heat.

It is well known that the total specific heat  $C_P(T)$  consists of mainly two parts (i) lattice specific heat ( $C_P^{\text{latt}}$ ) (ii) magnetic contribution ( $C_P^{\text{mag}}$ ). The lattice contribution consists of the electronic part  $C_P^{\text{el}}$  and the phonon part

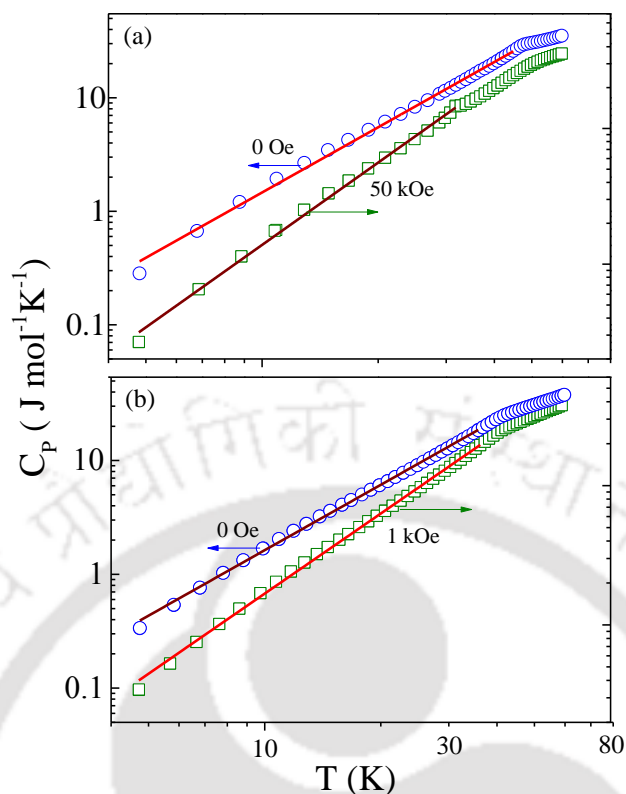
$$C_P^{\text{ph}} (=N f_D(\Theta_D/T)) = 9 N R (T/\Theta_D)^3 \int_0^{\frac{\Theta_D}{T}} \frac{x^4 e^x}{(e^x - 1)^2} dx \text{ where } f_D(\Theta_D/T) (=9R (T/\Theta_D)^3 \int_0^{\frac{\Theta_D}{T}} \frac{x^4 e^x}{(e^x - 1)^2} dx)$$

is the single Debye function,  $N$  is the number of atoms per formula unit,  $R$  is the universal gas constant (8.314 J/mol-K), and  $\Theta_D$  is the Debye temperature. Since the electronic contribution is significant only at very low temperatures, the phonon contribution has been extracted from the total specific heat. For this we have fitted the experimentally obtained specific heat data using Debye function ( $f_D(\Theta_D/T)$ ) at temperatures much higher than the ordering temperature where the magnetic contribution vanishes [172]. Extrapolate data for both the systems are shown in figure 4.21 together with the individual contribution of the phonon and magnetic components obtained from the above relation [172, 173]. Consequently, we obtained  $\Theta_D = 557$  K and 473 K for  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$ , respectively. These values are close to the magnitude ( $\Theta_D = 560$  K) reported by Ogawa and Waki [80] for  $\text{Co}_2\text{TiO}_4$  but less than the  $\Theta_D = 525$  K pure  $\text{Co}_3\text{O}_4$  reported by Roth [174].



**Figure 4.22:** The magnetic entropy ( $S_M$ ) versus temperature ( $T$ ) (L.H.S) and the differential entropy  $\partial S_M/\partial T$  versus  $T$  (R.H.S) plots of  $\text{Co}_2\text{TiO}_4$  for different magnetic fields.

Moreover, temperature variation of the differential magnetic entropy  $\partial S_M/\partial T$  ( $= C_{MP}/T$ ) shows a sharp peak across the  $T_{\text{COMP}}$  of  $\text{Co}_2\text{TiO}_4$  at high fields ( $\geq 50$  kOe) typical to a first-order-like transition, however, this field-dependent anomaly is not sharp at low fields (figure 4.22). Previous studies from Ogawa and Waki revealed that the  $C_P(T)$  data of  $\text{Co}_2\text{TiO}_4$  follows the simple  $T^{3/2}$  dependence in a narrow range of temperatures whereas, the modified  $T^{3/2}$  dependence (according to the equation  $C_M = (k_B/8)(k_B T/\pi\hbar a)^{3/2} F(x)$ ) was noticed over a wide range of temperature (5 K - 30 K). The effective anisotropy constant  $K_a$  ( $\sim 1.2 \times 10^5$  erg/cc) estimated by them was less than  $K_a = 9.3 \times 10^5$  erg/cc as compared to the present case (at  $T = 10$  K) [80]. In the low-temperature regime the logarithmic plot of  $C_P$  versus  $T$  shows a linear variation with slope  $\sim 1.91$  (figure 4.23). This implies that the heat capacity follows  $T^2$  dependence (for  $T < T_N$ ) following the equation  $C_P = AT^2$  with the coefficient ‘ $A$ ’ =  $18.96 \times 10^{-2}$  J/mol K. For  $T < 15$  K, the slope of  $\ln(C_P)$  versus  $\ln(T)$  turns out to be 2.14 with  $A = 14.78 \times 10^{-2}$  J/mol-K. Such  $T^2$  dependence is not natural to a typical canonical spin-glass phase, instead a  $T$ -dependence below the freezing temperature is universally observed [73, 175]. The  $T^2$  dependence of  $C_P$  values at low temperatures has been shown by several compounds such as Kagome spin-glass, frustrate antiferromagnets, diluted 2D antiferromagnets (re-entrant systems). In these compounds the long-range order is set by geometrical frustration and the collective excitations of the spin-liquid; as a result the magnetic-heat capacity shows  $T^2$  dependence [175, 176]. This behavior was found to be robust against the atomic substitution (dilution) for increasing the bond disorder. Therefore, in the present study anomalous  $T^2$ -dependence in heat-capacity data clearly suggests that the spin-liquid like excitations exists in both  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  with non-Heisenberg magnetic interactions at low temperatures [176 - 178].



**Figure 4.23:** Temperature variation of heat-capacity  $C_P(T)$  measured under both zero field and with field for (a)  $\text{Co}_2\text{TiO}_4$ , and (b)  $\text{Co}_2\text{SnO}_4$ . The solid lines correspond to the linear fit to  $AT^2$ .

Similar temperature dependence was found in  $\text{CuCr}_{1-x}\text{V}_x\text{S}_2$  for  $x \sim 0.30$ , in which, the long-range non-collinear order was blocked by the lattice defects [175]. Moreover, the neutron diffraction data of polycrystalline  $\text{Co}_2\text{TiO}_4$  reported by Hubsch *et al.* suggested the presence of canted-spins, likely resulting from magnetic frustration caused by the presence of non-magnetic ‘Ti’ ions on the ‘B’-sites [77]. In addition, the contribution of nuclear specific heat of  $\text{Co}^{59}$  nuclei to the total magnetic specific heat of  $\text{Co}_2\text{TiO}_4$  system cannot be ruled out [80].

#### 4.3.7 Summary:

In this chapter a systematic comparative analysis of the structural and magnetic properties of both  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  was presented. The major results are as follows: (i) Analysis of the temperature dependence of the dc susceptibilities above  $T_N$  using the Néel expression for ferrimagnets yields magnetic moments  $\mu(A) = 3.87 \mu_B$  and  $\mu(B) = 5.19 \mu_B$  ( $4.91 \mu_B$ ) for  $\text{Co}_2\text{TiO}_4$  ( $\text{Co}_2\text{SnO}_4$ ),  $\mu(B)$  being significantly different for the two cases. This difference in  $\mu(B)$  was considered the major reason for differences in their magnetic properties. (ii) Analysis of the XPS data exhibited the electronic structure of  $\text{Co}_2\text{TiO}_4$  to be  $[\text{Co}^{2+}] [\text{Co}^{3+}\text{Ti}^{3+}]\text{O}_4$  as compared to  $[\text{Co}^{2+}][\text{Co}^{2+}\text{Sn}^{4+}]\text{O}_4$  for  $\text{Co}_2\text{SnO}_4$ . This difference in the electronic structures of the ions on the B-sites was used to explain the difference in the observed  $\mu(B)$  values and the lack of definite evidence for the presence of spin-glass transition in  $\text{Co}_2\text{TiO}_4$  in contrast to the observation in  $\text{Co}_2\text{SnO}_4$ ; (iii) A compensation temperature of  $T_{\text{COMP}}$

#### ***Chapter 4: Negative Magnetization and Compensation Effect in Co<sub>2</sub>TiO<sub>4</sub>***

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$\approx 32$  K was observed for Co<sub>2</sub>TiO<sub>4</sub> below which the system retained its ferrimagnetic character. In contrast, similar compensation point was not observed in Co<sub>2</sub>SnO<sub>4</sub> although below 7 K, there was no coercivity or remanence, which are signatures of a compensated state. (iv) The large magnitudes of the coercivity  $H_C$  observed, in Co<sub>2</sub>TiO<sub>4</sub>, in the uncompensated state, most likely considered to be resulted from spin clusters. (v) The low-temperature complex magnetic ordering of Co<sub>2</sub>TiO<sub>4</sub> and Co<sub>2</sub>SnO<sub>4</sub> were studied using temperature dependence magnetization (M), Arrott-plot analysis and specific-heat ( $C_P$ ). Our experimental results demonstrated the signatures of pseudo first-order-discontinuous transitions below the ferrimagnetic Néel temperature in both the systems. In the same temperature regime ( $5 \text{ K} \leq T \leq 33 \text{ K}$ ),  $C_P$  followed  $T^2$  dependence instead of the linear variation in both the systems suggesting the dynamical spin-fluctuation at low temperatures. The random distribution of the cations on the A and B-sites and the different temperature dependence of magnetic moments ( $\mu[A](T)$  and  $\mu[B](T)$ ) were the likely source of such anomalous low-temperature magnetic ordering in Co<sub>2</sub>TiO<sub>4</sub> and Co<sub>2</sub>SnO<sub>4</sub>.



## Tuning the Compensation Point: Role of Sn Substitution in $\text{Co}_2\text{TiO}_4$

### 5.1 Introduction:

Tuning the magnetic properties such as: (i) exchange bias, (ii) anisotropy, and (iii) Curie or Néel temperature by the substitution of non-magnetic cations inside the ferro/ferrimagnets has been a subject of intense research, because, of the potential application of such properties in the field of magneto-electronic devices [179, 180]. For  $\text{Co}_2\text{TiO}_4$  ( $[\text{Co}^{2+}]_A[\text{Co}^{2+}\text{Ti}^{4+}]_B\text{O}_4$ ), tailoring the magnetic compensation point ( $\sim 30$  K), spin-glass ordering temperature (below  $T_N$ ), and polarity of exchange bias, are the key ingredients to examine, which is the subject of the current chapter. To investigate the changes occurring in the above properties systematically by varying the ‘Sn’ doping at the octahedral ‘B’ sites of  $\text{Co}_2\text{TiO}_4$  is the main objective of this chapter. This chapter also deals with the re-entrant spin-glass behaviour and the role of the competing exchange interactions or dilution of magnetic elements [31-36]. It is magnetic frustration resulting from either important to distinguish the role of different non-magnetic elements (‘Ti’ or ‘Sn’) or the alteration of the physical properties of antiferromagnetic  $\text{Co}_3\text{O}_4$  spinel because of its applications viewpoint, which is the main motivation to substitute ‘Sn’ at ‘Ti’ sites in  $\text{Co}_2\text{TiO}_4$  [181]. Moreover, inverse spinels such as  $\text{Co}_2\text{VO}_4$  and  $\text{Co}_2\text{TiO}_4$  continues to receive large attention recently because of their potential applications in Li-ion batteries, thermistors, solid-oxide fuel-cells, magnetic recording, microwave and RF devices [3, 9, 10, 182 - 190].

The cationic distribution and role of non-magnetic doping elements like germanium (Ge) and zinc (Zn) at the ‘Ti’ and Co-sites in the  $\text{Co}_2\text{TiO}_4$  system were first studied by Strooper *et al.* [82, 191] For un-doped case, they obtained the magnitudes of two-sublattice magnetizations as  $M_A(0) = 20450$  (G/cm<sup>3</sup>)/mol and  $M_B(0) = 19750$  (G/cm<sup>3</sup>)/mol,  $T_N \sim 53 \pm 2$  K, Curie constant  $C = 5.4 \pm 0.1$  K cm<sup>3</sup>/mol and exchange constants  $J_{AB} \sim -6.3 \pm 0.3$  K,  $J_{AA} \sim -4.6 \pm 0.3$  K and  $J_{BB} \sim -5.5 \pm 0.3$  K [82, 191]. Although Strooper *et al.* reported the magnetic properties of various compositions of  $\text{Co}_2\text{Ti}_{1-x}\text{Ge}_x\text{O}_4$  and  $\text{Co}_2\text{-xMg}_x\text{TiO}_4$ , but a detailed analysis of the frequency dependence of  $\chi_{ac}(T)$  in such systems is still lacking in the literature [82, 191]. Antic *et al.* reported spin-glass state at 17 K in  $\text{Li}_{0.333}\text{Co}_{1.5}\text{Ti}_{1.167}\text{O}_4$  polycrystalline sample whose cationic distribution is  $(\text{Li}_{0.09}\text{Co}_{0.01})_{8a}[\text{Li}_{0.24}\text{Co}_{0.59}\text{Ti}_{0.17}]_{16d}$  [13]. Except these reports, no other studies are available in the literature dealing with the physical properties of doped cobalt-orthotitanate. At first glance both the compounds  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  appear almost similar (despite slight differences in their ionic radii), but, they exhibit quite different magnetic structure; in-particular the compensation point, giant-exchange bias, and negative magnetization below the ferrimagnetic ordering of  $\text{Co}_2\text{TiO}_4$  were not shown by its sister compound  $\text{Co}_2\text{SnO}_4$  (as discussed in our previous chapter). These issues motivated us to study the magnetic interactions in the polycrystalline  $\text{Co}_2\text{Ti}_{1-x}\text{Sn}_x\text{O}_4$  system. Our experiments were mainly focused to the temperature and frequency dependence of ac-magnetic measurements including the temperature dependence of remanence and coercivity measurements under various magnetic fields. Such measurements are important because they can provide a vital information related to the spin-glass ordering. For

example, estimation of (i) spin-glass freezing temperature ' $T_F$ ', (ii) characteristic frequency of the cluster ' $f_0$ ', critical exponent of correlation length ' $\nu$ ', and relative shift ' $\Omega$ ' of the peak temperature per decade frequency etc. Our experimental results and analysis reveals the following fascinating features in Co<sub>2</sub>Ti<sub>1-x</sub>Sn<sub>x</sub>O<sub>4</sub> system like for example (i) shift in the magnetic compensation point from 31.74 K to 27.1 K, (ii) large zero-field-cooled (ZFC) and field-cooled (FC) bipolar exchange bias effect ( $H_{EB} = 13.6$  kOe (ZFC) and  $\sim 958$  Oe (FC) at 7 K), and (iii) existence of spin-glass ordering at  $T_F \approx 44.05$  K, details of these results, and their discussion are presented in this chapter.

### **5.2 Experimental Details:**

The bulk polycrystalline samples of Co<sub>2</sub>Ti<sub>1-x</sub>Sn<sub>x</sub>O<sub>4</sub> ( $0 \leq x \leq 1$ ) were synthesized by standard solid-state-reaction method. For this stoichiometric amount of Co<sub>3</sub>O<sub>4</sub> (Alfa Aesar, purity 99.99%), TiO<sub>2</sub> (Alfa Aesar, purity 99.99%) and SnO<sub>2</sub> (Alfa Aesar, purity 99.99%) were chosen as precursors. Appropriate amount of these materials was first ground in agate mortar. These mixed powders were pressed into cylindrical pellets of diameter  $\sim 13$  mm using a hydraulic press with a maximum load of 5 ton per cm<sup>2</sup>. All the pellets were finally sintered at 1350°C for 18 h in air. To check the phase purity and crystal structure information X-ray diffraction measurements were performed using a Rigaku X-ray diffractometer (model: TTRAX-III) with Cu-K $\alpha$  radiation ( $\lambda = 1.54056$  Å), and the diffraction data was analyzed using Rietveld refinement of the patterns by means of FullProf programme. The ac-susceptibility and dc-magnetization measurements were performed using a superconducting quantum interference device (SQUID) based magnetometer from Quantum design with temperature (T) and magnetic field (H) capable of reaching 5 K from 320 K and  $H_{dc} = \pm 70$  kOe, respectively.

### **5.3. Characterizations:**

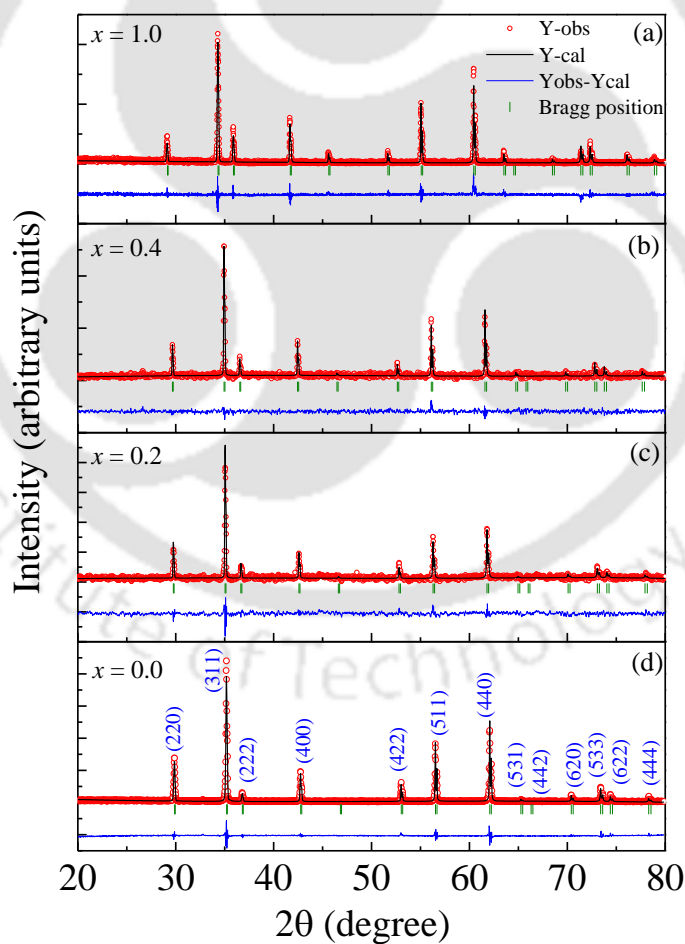
#### **5.3.1 Crystal Structure Analysis:**

Figure 5.1 shows the X-ray diffraction pattern of the Co<sub>2</sub>Ti<sub>1-x</sub>Sn<sub>x</sub>O<sub>4</sub> polycrystalline for different compositions. All these diffraction patterns correspond to the inverse spinel crystal structure with space group  $Fd-3m$  (227) similar to Co<sub>2</sub>TiO<sub>4</sub>. However, the lattice parameter  $a_0 = 8.45 \pm 0.01$  Å (for  $x = 0$  i.e. pure Co<sub>2</sub>TiO<sub>4</sub>) increases progressively with increasing the 'Sn' content, e.g.  $a_0 = 8.512 \pm 0.01$  Å for  $x = 0.4$  and  $a_0 = 8.66 \pm 0.012$  Å for  $x = 1$  (i.e. Co<sub>2</sub>SnO<sub>4</sub>). Approximately 7.5% increase in the unit-cell volume was noticed by incorporating the stannous within the Co<sub>2</sub>TiO<sub>4</sub> matrix at 'Ti' sites. This value is close to the standard calculated value of  $\sim 7.38\%$ . Table-5.1 summarizes the variation of lattice parameters, bond lengths and bond angles for different compositions of Co<sub>2</sub>Ti<sub>1-x</sub>Sn<sub>x</sub>O<sub>4</sub> samples obtained from the Rietveld refinement process. It is clear from the table that the average bond length (B-O) between the oxygen ion and the Ti<sup>4+</sup>-cations present in the octahedral sites increases progressively with the increase of Sn<sup>4+</sup> substitution, while the reverse is true for the tetrahedral sites (A-O). Such deviation in the bond lengths of the octahedral and tetrahedral sites originates from the higher ionic radius of Sn<sup>4+</sup> (0.69 Å) than Ti<sup>4+</sup> (0.605 Å). Similarly, the bond angle A-O-B increases from 120° with increasing the Sn-content, while a

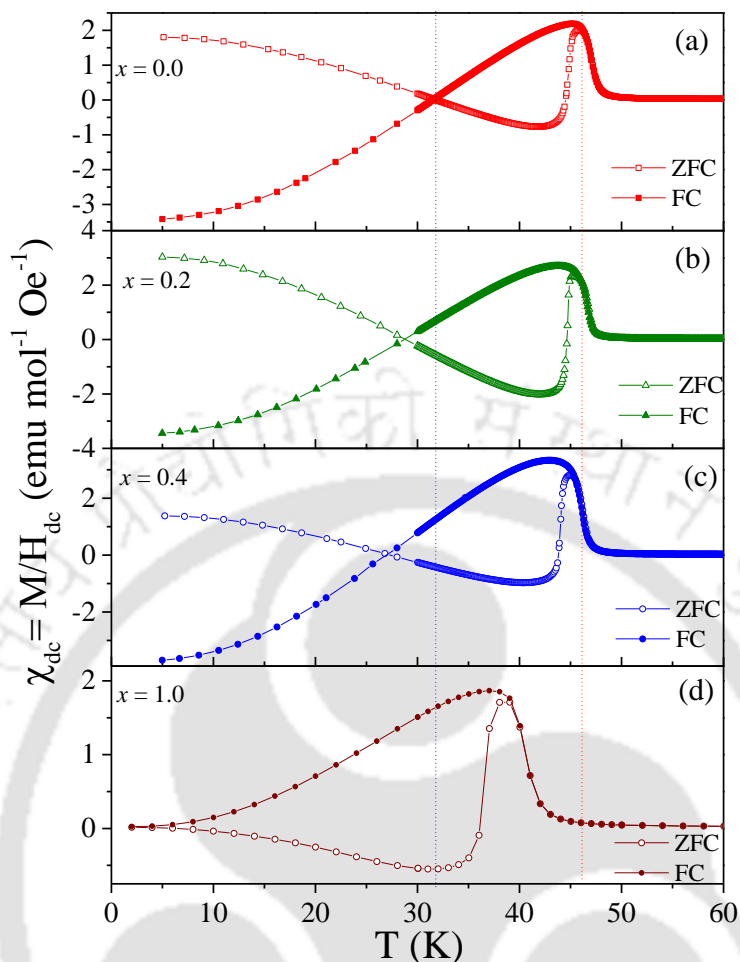
significant deviation from the orthogonality ( $90^\circ$ ) was noticed in B-O-B. Such canted behavior plays a major role in the magnetic ordering of the samples which is discussed below.

**Table 5.1:** List of various crystal structure parameters (i) lattice parameter, (ii) bond Length and (iii) bond angles of various compositions of bulk samples  $\text{Co}_2\text{Ti}_{1-x}\text{Sn}_x\text{O}_4$  ( $0 \leq x \leq 1$ ). [\* $\text{Co}_2\text{TiO}_4$  sample sintered at  $1100^\circ\text{C}$ , results of previous chapter].

System	Lattice Parameter ( $a = b = c$ )	Interaxial angles $\alpha = \beta = \gamma$	Bond Length		Bond Angle	
			A-O	B-O	A-O-B	B-O-B
$\text{Co}_2\text{TiO}_4$	$8.45 \pm 0.01 \text{ \AA}$	$90^\circ$	$1.98 \pm 0.01 \text{ \AA}$	$2.02 \pm 0.02 \text{ \AA}$	$121.68^\circ \pm 0.61^\circ$	$94.93^\circ \pm 0.48^\circ$
$\text{Co}_2\text{Ti}_{0.8}\text{Sn}_{0.2}\text{O}_4$	$8.49 \pm 0.01 \text{ \AA}$	$90^\circ$	$1.95 \pm 0.02 \text{ \AA}$	$2.06 \pm 0.02 \text{ \AA}$	$122.90^\circ \pm 0.62^\circ$	$93.30^\circ \pm 0.47^\circ$
$\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$	$8.51 \pm 0.01 \text{ \AA}$	$90^\circ$	$1.89 \pm 0.02 \text{ \AA}$	$2.09 \pm 0.02 \text{ \AA}$	$124.30^\circ \pm 0.62^\circ$	$91.40^\circ \pm 0.46^\circ$
$\text{Co}_2\text{SnO}_4$	$8.66 \pm 0.01 \text{ \AA}$	$90^\circ$	$1.88 \pm 0.02 \text{ \AA}$	$2.16 \pm 0.02 \text{ \AA}$	$125.01^\circ \pm 0.63^\circ$	$90.37^\circ \pm 0.45^\circ$
* $\text{Co}_2\text{TiO}_4$	$8.45 \pm 0.01 \text{ \AA}$	$90^\circ$	$1.98 \pm 0.01 \text{ \AA}$	$2.03 \pm 0.02 \text{ \AA}$	$121.68^\circ \pm 0.61^\circ$	$94.95^\circ \pm 0.48^\circ$



**Figure 5.1:** The X-ray diffraction pattern together with Reitveld refined data of  $\text{Co}_2\text{Ti}_{1-x}\text{Sn}_x\text{O}_4$  (a)  $x = 1.0$ , (b)  $x = 0.4$  (c)  $x = 0.2$  (d)  $x = 0.0$ , samples sintered at  $1350^\circ\text{C}$  for 18 h in air.



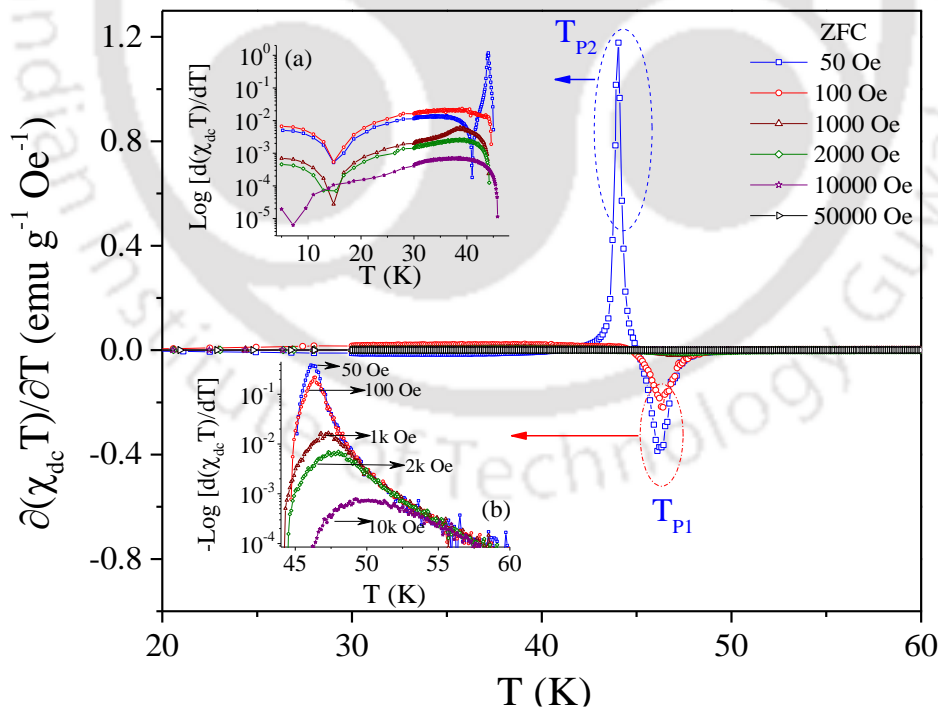
**Figure 5.2:** Temperature dependence of dc-magnetic susceptibility  $\chi_{dc}(T) = M/H_{dc}(T)$  for (a)  $x = 0.0$ , (b)  $x = 0.2$  (c)  $x = 0.4$  (d)  $x = 1.0$  measured under both zero-field-cooled (ZFC) and field-cooled (FC) conditions recorded at magnetic field  $H_{dc} = 50$  Oe.

### 5.3.2 Coexistence of Ferrimagnetism and Spin-glass Ordering:

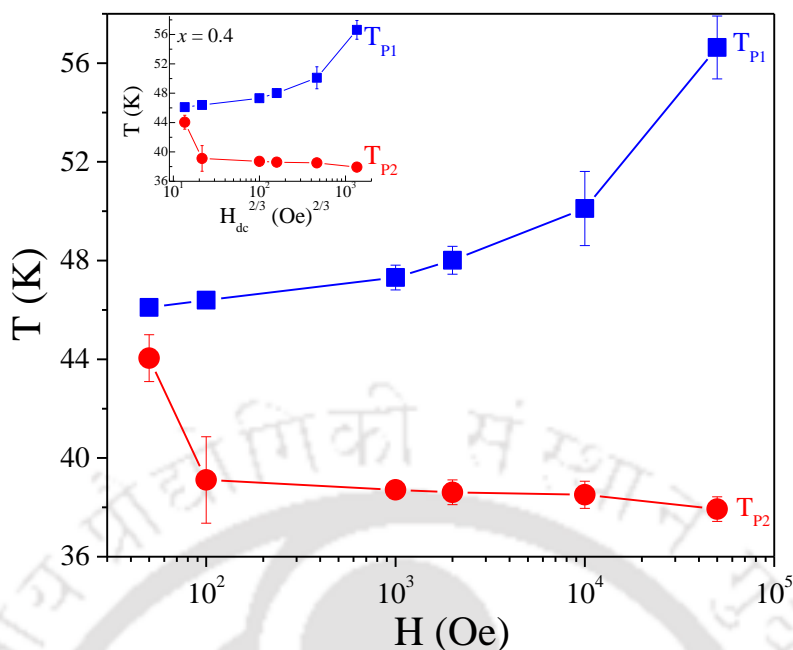
Figure 5.2 shows the temperature variation of dc-magnetic susceptibility  $\chi_{dc}$  ( $=M/H_{dc}$ ) plots for various compositions of  $\text{Co}_2\text{Ti}_{1-x}\text{Sn}_x\text{O}_4$  recorded under both zero-field-cooled (ZFC) and field-cooled (FC,  $H @ 50$  Oe) conditions. For all the compositions both the curves  $\chi_{ZFC}(T)$  and  $\chi_{FC}(T)$  exhibits a characteristic peak  $T_P$  ( $\sim 45.9$  K (ZFC) and  $45.17$  K (FC) for  $x = 0$ ) corresponding to the ferrimagnetic Néel temperature  $T_N$  which decreases continuously with increasing the Sn-content ( $T_P \sim 45.01$  K (ZFC) and  $44.98$  K (FC) for  $x = 0.4$  and  $39.06$  K (ZFC) and  $37.04$  K (FC) for  $x = 1$ ). Also both the curves  $\chi_{ZFC}(T)$  and  $\chi_{FC}(T)$  exhibits strong irreversibility below this peak temperature; while a slight variation in the peak position was noticed with increasing the  $H_{dc}$  values. It is interesting to note that both the susceptibility curves  $\chi_{ZFC}(T)$  and  $\chi_{FC}(T)$  exhibits a crossover in sign across the compensation temperature  $T_{COMP} \sim 31.74$  K ( $\chi_{ZFC}(T) = 0 = \chi_{FC}(T)$ ) where the bulk magnetizations of both sublattices balance each other (figure 5.2). Substitution of ‘Sn’ ions within the octahedral positions of ‘Ti’ in  $\text{Co}_2\text{TiO}_4$  have pronounced effect on the compensation temperature; for example  $T_{COMP}$  decreases exponentially to

27.1 K for  $x = 0.4$ . By extrapolating the experimental data points with the exponential variation  $T_{\text{COMP}} = 24.58 + 7.04 \exp(-2.603x)$ , one can obtain  $T_{\text{COMP}} = 25.103$  K for 100% substitution of ‘Sn’ inside the  $\text{Co}_2\text{TiO}_4$  matrix i.e. for  $x = 1$ . However, this estimated value is quite large as compared to the experimentally obtained values of 6 K from the figure 5.2(d). Although both ‘Sn’ and ‘Ti’ are less-magnetic and their contribution to the global magnetic behavior is negligible as compared to  $\text{Co}^{2+}$ , but, we expect that the magnetic-dilution effect is more prominent in  $\text{Sn}^{4+}$ , due to which, the magnitude of  $T_{\text{COMP}}$  decreases drastically in Co-orthostannate than in Co- orthotitanate. Needless to say that the difference in the ionic sizes of both the ions ( $2r_{\text{Sn}} = 1.38 \text{ \AA} > 2r_{\text{Ti}} = 1.21 \text{ \AA}$ ) is responsible for the magnetic dilution. The temperature dependence of the coercive field  $H_C(T)$  and remanence magnetization  $M_R(T)$  (shown in figure 5.10 and 5.11 which will be discussed in section 5.3.3) both starts decreasing across 25 K and gradually approaches to zero at 6 K. A detailed analysis of such features will be discussed in the later section in terms of temperature dependence of exchange-bias  $H_{\text{EB}}(T)$ ,  $H_C(T)$  and remanence  $M_R(T)$ .

In order to probe the exact magnetic ordering temperatures, we calculated the  $\partial(\chi_{\text{dc}}T)/\partial T$  from the  $\chi$ -T data recorded under the ZFC case, and plotted the differentiated curve against the temperature in figure 5.3. It is well known that for antiferromagnets, the  $T_N$  does not exactly match with the peak temperature  $T_P$  in  $\chi(T)$ , instead it is given by the peak in  $\partial(\chi_{\text{dc}}T)/\partial T$ . Because theoretically the temperature variation of  $\partial(\chi_{\text{dc}}T)/\partial T$  is analogous to the temperature variation of the heat capacity  $C_P(T)$  in the systems which shows antiferromagnetic interactions [6, 18]. Figure 5.3 clearly shows a negative minimum and a positive maximum typical for the ferrimagnetic systems

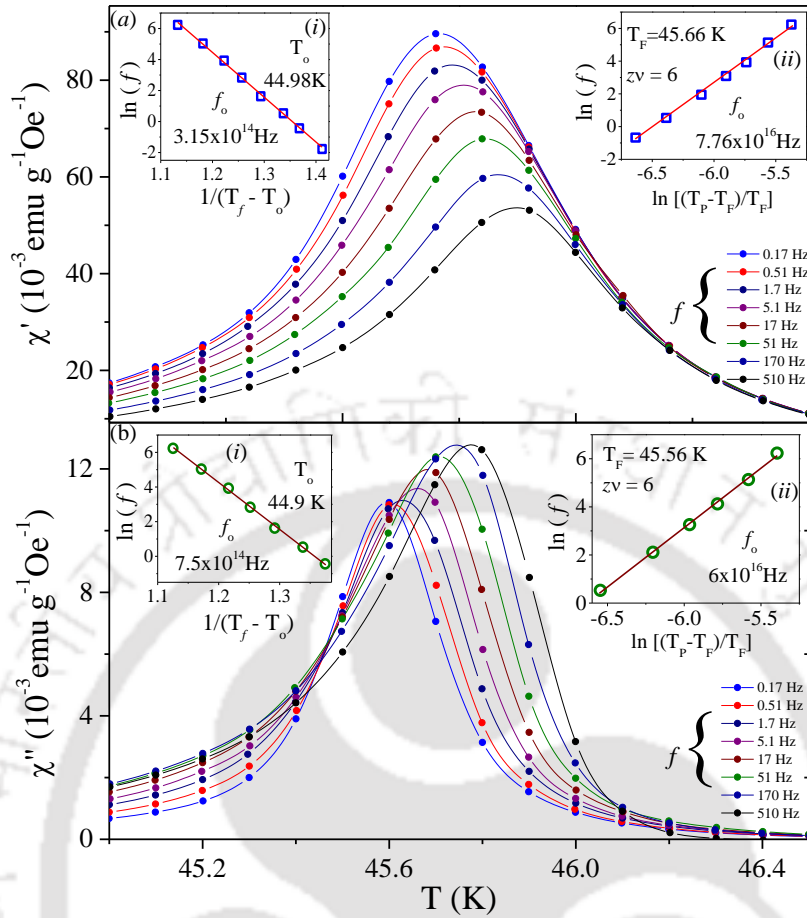


**Figure 5.3:** The plots of  $\partial(\chi_{\text{dc}}T)/\partial T$  versus  $T$  of  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$  sample at various external fields  $H_{\text{dc}} = 50, 100, 1000, 2000, 10000, 50000$  Oe. The inset (a) and (b) of shows the peak variation clearly in logarithmic scale.



**Figure 5.4:** The variation of the transition temperatures  $T_{P1}$  (a) and  $T_{P2}$  (b) of  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$  sample as a function of the applied magnetic field  $H$ . The inset shows variation of the transition temperatures  $T_{P1}$  and  $T_{P2}$  as a function of  $H_{dc}^{2/3}$  for  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$ .

unlike in perfect antiferromagnetic systems, where, only a positive maximum is reported at  $T = T_N$  [77]. An upfront calculation from the Curie-Weiss variation yields  $\partial(\chi T)/\partial T = -C\theta/(T-\theta)^2$ , which will give a negative minimum at  $T = \theta$ , and for negative  $\theta$  (typical of most antiferromagnetic substances with dominant antiferromagnetic interaction) the equation  $\partial(\chi T)/\partial T$  gives a positive maximum, as observed in figure 5.3. For the composition  $x = 0.4$  the data recorded under ZFC protocol depicts a minimum value of  $\partial(\chi T)/\partial T$  at 46.10 K, whereas, the maximum of  $\partial(\chi T)/\partial T$  occurs at 44.05 K for  $H_{dc} = 50$  Oe. This exercise leads to the determination of the Néel temperature ' $T_N$ ' = 46.10 K (designated as  $T_{P1}$  shown in the figure 5.3) and the second transition ' $T_{P2}$ ' = 44.05 K. Inset (a) and (b) depicts the small change in the peak position of  $T_{P1}$  and  $T_{P2}$  for various values of  $H_{dc}$ . The high-field (150 kOe) susceptibility data reported by Hubsch and Gavoille in  $\text{Co}_2\text{TiO}_4$  did not show such two peak behaviour, instead they observed such two peak behaviour in the temperature dependence of remanence  $M_R(T)$  and coercivity  $H_C(T)$  with different ordering temperatures 46 K and 55 K [77]. The existence of second transition at  $T_{P2}$  gives the signatures of spin-glass behaviour just below the  $T_N$ . As the applied magnetic field increases from 50 Oe to 50 kOe the peak at  $T_{P1}$  corresponding to the  $T_N$  becomes broad, and shifts towards higher temperature side ( $T_{P1} \sim 56.64$  K for  $H = 50$  kOe expected for a typical ferrimagnetic transition (inset (b) of figure 5.3). On the contrary, the magnetic field variation of  $T_{P2}$  shows a decreasing trend typical to blocking/freezing of the local spins (figure 5.4). Since all the samples are having bulk grain sizes in the  $\mu\text{m}$  range so blocking effects are ruled out and glassy signatures prevail in the system below  $T_N$ . Such a variation of  $T_{P2}(H_{dc})$  usually shows a straight line behaviour when plotted against  $H_{dc}^{2/3}$  (de Almeida-Thouless (A-T) line) [192]. But, in the present



**Figure 5.5:** Temperature dependence of the ac-magnetic susceptibility of  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$  sample: (a) the real component  $\chi'(T)$ , (b) the imaginary component  $\chi''(T)$  recorded at various frequencies ( $0.17 \text{ Hz} \leq f \leq 510 \text{ Hz}$ ) under warming condition using  $h_{ac} = 3 \text{ Oe}$  and zero static magnetic field. The inset (i) of figure (a) and the inset (i) of figure (b) show the  $\ln f$  versus  $[1/(T_f - T_0)]$  using the peak positions in  $\chi'(T)$  and  $\chi''(T)$  respectively. The solid line shows Vogel-Fulcher law fit of experimental data. The inset (ii) of figure (a) and inset (ii) of figure (b) shows the  $\ln f$  versus  $\ln[(T_p - T_f)/T_f]$  using the peak positions in  $\chi'(T)$  and  $\chi''(T)$  respectively, the solid line shows are the linear fits to the experimental data.

case analysis shown in the inset of figure 5.4 shows a linear behaviour above a threshold value  $H_{dc}^* = 100 \text{ Oe}$ . For a clear understanding of glassy behaviour, we have investigated the temperature variation of the dynamic magnetic susceptibility at various ac-magnetic field frequencies ( $f$ ). Since the experimental time window of the measurement is determined by ' $f$ ' of the ac field, a wide-range of time span can be effortlessly set by changing the ' $f$ ' itself.

Figure 5.5 shows the temperature dependence of in-phase (real component  $\chi'(T)$ ) and out-of-phase (imaginary component  $\chi''(T)$ ) of the ac-magnetic susceptibilities  $\chi_{ac}(T)$  measured at various frequencies between the temperature window  $T_{P2}$  and  $T_{P1}$ . The parameters obtained from the  $\chi_{ac}(T)$  analysis were very sensitive to thermodynamic phase changes and often been employed to probe the spin-glass phase-transition temperature. During the measurement process the amplitude of the peak-to-peak ac-magnetic field  $h_{ac}$  is set to  $\sim 3 \text{ Oe}$  by varying

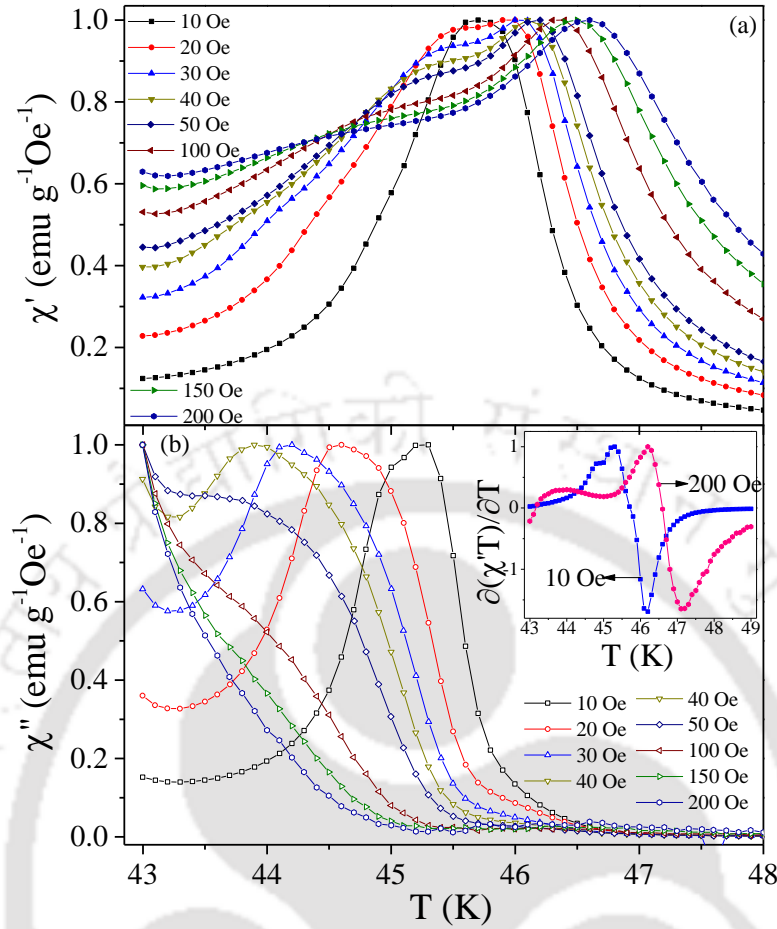
' $f$ ' between 0.17 Hz and 510 Hz under zero  $H_{dc}$ . It is clearly evident from both the graphs figure 5.5(a), (b), that the peak position  $T_P$  in  $\chi'(T)$  and  $\chi''(T)$  shifts towards higher temperature side. A convenient gauge to understand the nature of the spin-glass freezing processes lies in the determination of relative shift ( $\Phi$ ) of the peak temperature per decade frequency using the expression  $\Phi = [\Delta T_P / (T_P \Delta \log f)]$ , where  $\Delta T_P$  is the change in  $T_P$  with change in  $\Delta \log f$ . Consequently, we have calculated the values of  $\Phi = 0.00115$  and  $0.000815$  using  $\chi'$  versus  $T$  and  $\chi''$  versus  $T$ , respectively. From the available literature data corresponding to the number of conventional spin-glass systems and magnetic ultrafine-particles, it is known that  $\Phi \geq 0.13$  is observed in non-interacting nanometre size particles, whereas, for interacting particles  $\Phi$  lies in the range 0.05- 0.13. Thus, ' $\Phi$ ' decreases with increase in the strength of the interaction. For typical spin-glasses, the parameter  $\Phi$  should lie between 0.005 and 0.05 [193]. Therefore, in the present case  $\Phi$  values estimated from both  $\chi'$  versus  $T$  and  $\chi''$  versus  $T$  are consistent with the spin-glass ordering. To examine this issue further the change in  $T_P$  with ' $f$ ' is analysed using the following dynamic scaling equation [42, 194].

$$f = f_0 \left( \frac{T_P - T_F}{T_F} \right)^{zv} \dots (5.1)$$

In the above equation ' $f_0$ ' is the value of attempt frequency, ' $T_F$ ' is the spin-glass transition temperature, ' $z$ ' is the dynamical critical exponent and ' $v$ ' is the critical exponent of correlation length. The insets (ii) in both the figures 5.5(a), (b) shows the frequency variation of the peak position estimated from both  $\chi'(T)$  and  $\chi''(T)$ . In these plots, the solid lines connecting the scattered symbols for both cases, represents the best fit to the above equation which is in good agreement with the experimental data. Further, using the values of  $T_P(\chi')$  and  $T_P(\chi'')$ , we executed the least square fitting of the data by plotting logarithmic variation i.e.  $\ln[f]$  against  $\ln[(T_P - T_F)/T_F]$  by varying  $T_F$  until a straight line is obtained. Such analysis yields the following important parameters for Co<sub>2</sub>Ti<sub>0.6</sub>Sn<sub>0.4</sub>O<sub>4</sub>:  $f_0 = 7.76 \times 10^{16}$  Hz,  $T_F = 45.66$  K and ' $zv$ ' =  $6.009 \pm 0.007$  for  $T_P(\chi')$  and  $f_0 = 6.007 \times 10^{16}$  Hz,  $T_F = 45.56$  K and ' $zv$ ' =  $6.004 \pm 0.003$  for  $T_P(\chi'')$ . These magnitudes of ' $f_0$ ' and ' $zv$ ' are consistent with the previously reported prototype spin-glasses; in particular, the magnitude of  $f_0 \approx 10^{20}$  Hz corresponds to spin-flip frequency of magnetic moments of ions or atoms [192 – 194]. The insets (i) of figures 5.5 (a), (b) show the best fit representation of the data that was obtained using the Vogel-Fulcher law which is usually expressed as

$$f = f_0 \exp \left( \frac{-E_a}{k_B(T - T_0)} \right) \dots (5.2)$$

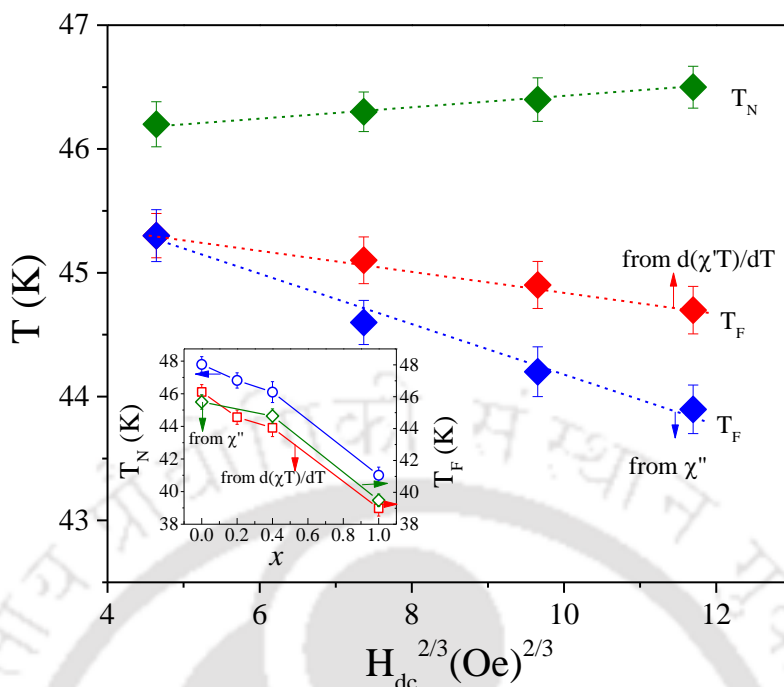
where  $f_0$  is the characteristic frequency of the clusters,  $T_0$  is a measure of the interaction between magnetic clusters,  $k_B$  is the Boltzmann constant and  $E_a$  is the activation energy or the potential barrier separating two adjacent clusters. This exercise yields  $T_0 = 44.98$  K (44.90 K) and  $f_0 = 3.15 \times 10^{14}$  Hz ( $7.5 \times 10^{14}$  Hz) for  $\chi'(\chi'')$ . Such large values of  $f_0$  has been seen in other systems as well, for example AgMn,[192] CuMn,[120] and AuFe [195] which indicates the presence of interacting magnetic spin clusters of significant sizes in the system. The competition between ferrimagnetism and magnetic frustration in the system is the main source of existence of spin clusters



**Figure 5.6:** Temperature dependence of ac-magnetic susceptibility (a) real part  $\chi'(T)$ , and (b) imaginary  $\chi''(T)$  components of bulk  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$  recorded at various bias fields  $H_{dc}$  ( $10 \text{ Oe} \leq H_{dc} \leq 200 \text{ Oe}$ ) with constant frequency 2 Hz and amplitude of 3 Oe. The insets of figure b depict the temperature variation of  $\partial(\chi'_{ac}T)/\partial T$  plots at different bias fields  $H_{dc} = 10$  and 200 Oe.

which leads to a short range order occurring below  $T_N$ . Earlier studies related to the magnetic properties of  $\text{Y}_{0.7}\text{Ca}_{0.3}\text{MnO}_3$  and  $\text{La}_{0.96-y}\text{Nd}_y\text{K}_{0.04}\text{MnO}_3$  ( $0 \leq y \leq 0.4$ ) reported the formation of such spin-clusters with short-range order [121, 196].

Previous studies on un-doped  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  by Srivastava *et al.* reported four transitions in the  $\chi_{ac}(T)$  data recorded in the presence of ( $f = 21 \text{ Hz}$ ,  $V_{p-p} \sim 0.5 \text{ Oe}$ ) with dc-magnetic field in the range 285 Oe - 460 Oe [79, 108]. The location of first two transitions and their field dependence is consistent with the  $T_N(T_{P1})$  and  $T_F(T_{P2})$  observed in the  $\chi_{ZFC}(T)$  data as discussed above. Accordingly, for  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$  system we have performed a detailed temperature dependence of the ac-magnetic susceptibilities superimposed with various dc-bias fields  $H_{dc}$  ( $10 \text{ Oe} \leq H_{dc} \leq 200 \text{ Oe}$ ) similar to that discussed in chapter 3. During the measurement frequency and ac-peak amplitude  $h_{ac}$  was kept constant at  $f = 2 \text{ Hz}$  with  $h_{ac} = 3 \text{ Oe}$ , respectively. The data were recorded in close temperature intervals of  $\sim 0.1 \text{ K}$  between 43 K and 48 K to probe the small features present if any and avoid any error in the location of transition. Figure 5.6 shows the  $\chi'(T)$  and  $\chi''(T)$  measured at various  $H_{dc}$ . The amplitude of



**Figure 5.7:**  $H_{dc}^{2/3}$  dependence of ferrimagnetic Néel temperature  $T_N$  and freezing temperature  $T_F$ . The solid lines show the linear fit to the data (often called the de Almeida-Thouless AT line). The inset shows compositional variation of  $T_N$  and  $T_F$ .

both  $\chi'(T)$  and  $\chi''(T)$  decreases significantly with increasing the  $H_{dc}$ , however, two peaks are clearly evident in  $\chi'(T)$  curves with the extent of splitting increases with increase of  $H_{dc}$ . This behavior is consistent with the two-peak scenario in dc-susceptibility data ( $\chi_{ZFC}(T)$ ) discussed above.

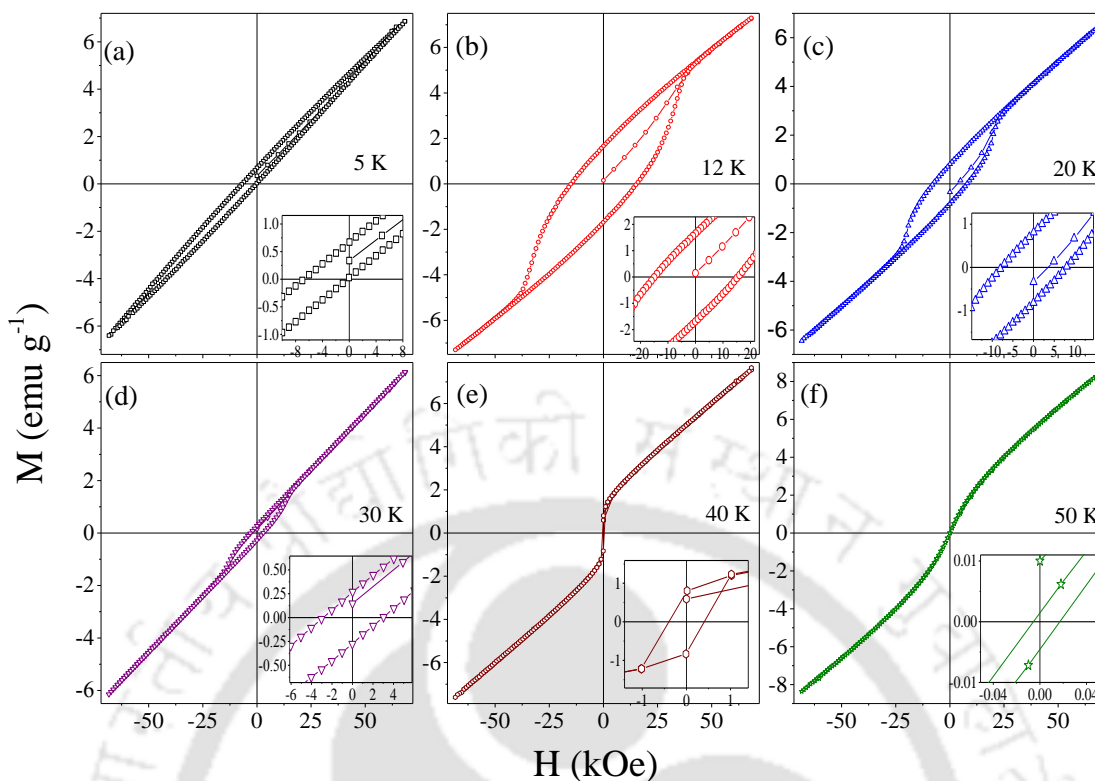
The out-of-phase susceptibility  $\chi''$  exhibits only a broad cusp with a weak shoulder. The amplitude of this cusp decreases and shifts to lower temperatures with increase in  $H_{dc}$ . As  $H_{dc}$  approaches to zero, the cusp in  $\chi''$  is centered across 45.30 K which is lower than the  $T_N = 46.10$  K. Since  $\chi''(T)$  is the out-of-phase component of the  $\chi_{ac}(T)$ , it is related with the transverse spin components. These observations depict the coexistence of ferrimagnetism in the longitudinal spin component at  $T_N$  and spin-glass ordering of the transverse spin component at a slightly lower temperature  $T_F$ . Such phenomenon of semi-spin-glass state was predicted in the papers by Gabay and Toulouse [122], and Villian [40] in insulators with non-magnetic impurities. Subsequently, the temperature dependence of  $\chi''$  and  $\partial(\chi''T)/\partial T$  are found to be comparable in many systems which have a strong theoretical basis [6, 77, 78]. The inset of figure 5.6(b) clearly shows two-peaks corresponding to  $T_F$  and  $T_N$ . These observed peaks in  $\chi''$  and  $\partial(\chi''T)/\partial T$  are almost analogous near the magnetic phase transitions similar to  $\text{Co}_2\text{SnO}_4$  data (discussed in the chapter 3) and the nanoparticles of quasi-two-dimensional ferromagnet  $\alpha\text{-Ni}(\text{OH})_2$  [124]. The dc-magnetic field variations ( $T_P$  versus  $H_{dc}^{2/3}$ ) of the two peaks in  $\chi''$ , and positive and negative points in  $\partial(\chi''T)/\partial T$  are plotted together in figure 5.7. The peak associated with  $T_N$  has been justified, since, its shift towards higher temperature with increase in the field is characteristic of ferromagnets because of the direct coupling of the order parameter

with applied magnetic field [117, 118]. Also  $\chi'$  being the in-phase component represents the longitudinal spin constituent. The straight line behavior in figure 5.7 also shows that the position of the second peak in  $\partial(\chi'/T)/\partial T$  and the single peak in  $\chi''$ , and their shifts with magnetic field are identical. Such characteristic  $H^{2/3}$  variation of this peak position, shown in the figure 5.7, is consistent with the A-T line like behavior [192]. The A-T line analysis is a well-established model often used to examine the presence of spin-glass-like characteristics in a variety of disordered systems [124, 127 - 130]. The inset of figure 5.7 shows the variation of  $T_N$  and  $T_F$  as a function of 'Sn' doping concentration: since the unit-cell volume increases progressively with increasing composition, which in turn, affects the exchange interaction between the magnetic ions and finally leading to the alteration of  $T_N$  and  $T_F$ .

### **5.3.3 Observation of Giant-Coercivity and Exchange Bias:**

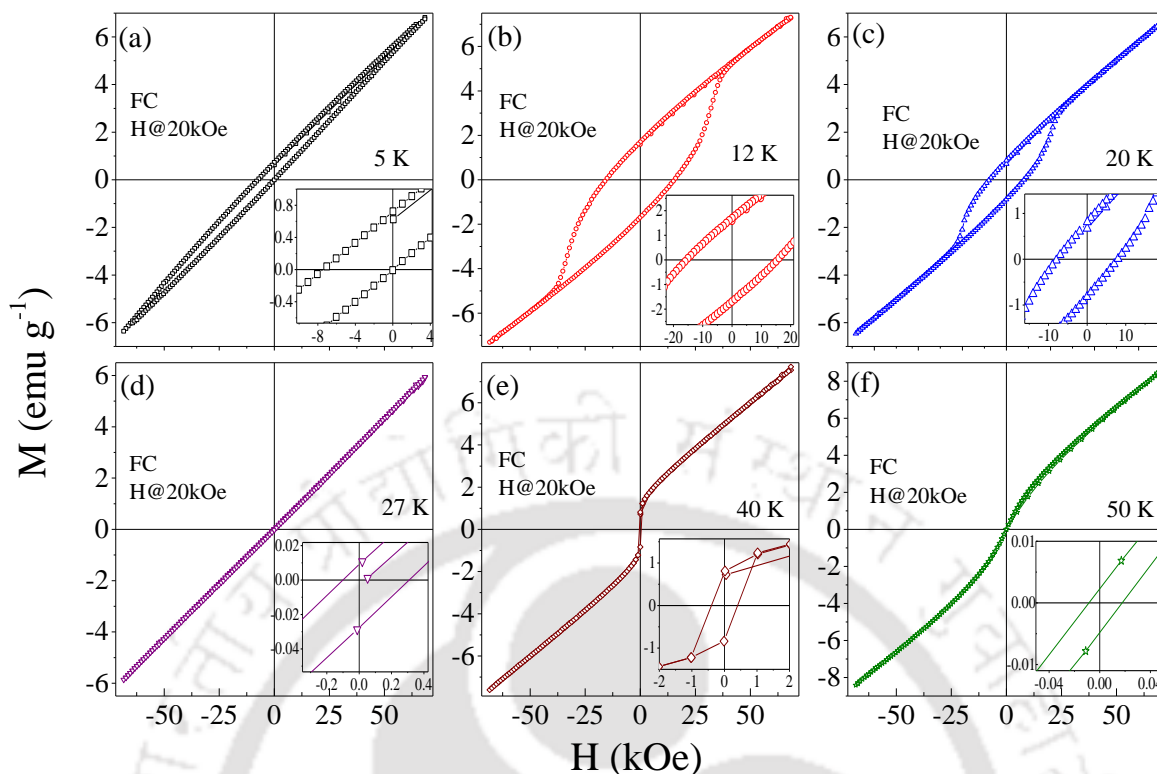
The coercive field  $H_C$  is often considered as a measure of canting of the spin configuration, because, Néel theory predicts that the mean-square value of the disordered transverse spin component significantly increases the coercive field [77]. Therefore, for a detailed understanding of the nature of magnetic ordering below  $T_N$ , we performed a series of hysteresis loop measurements at different temperatures. Such magnetization versus field (M-H) measurements were executed under both ZFC and 20 kOe field-cooled (FC) conditions for  $x = 0.4$  (Co<sub>2</sub>Ti<sub>0.6</sub>Sn<sub>0.4</sub>O<sub>4</sub>). During the measurement of each M-H loop the system was brought to the perfect paramagnetic state by increasing the temperature above  $T_N$ . In the course of FC mode, the sample was first cooled down to 5 K in the presence of 20 kOe magnetic field from the paramagnetic state, and the M-H loops was ramped in the range  $-70 \text{ kOe} \leq H_{dc} \leq 70 \text{ kOe}$ . This whole process was repeated for different temperatures. Figures 5.8 and 5.9 depict the complete M-H hysteresis loops at selected temperatures recorded under both ZFC and FC conditions. The coercive field ( $H_C$ ), remanence magnetization ( $M_R$ ), and the loops asymmetry ( $H_{EB}$ ) (EB = exchange-bias) were measured from the above loop asymmetry, and their temperature dependence are plotted separately in the figures 5.10 and 5.11. All these hysteresis loops are unsaturated even up to 68 kOe and exhibits anomalous temperature dependence with giant  $H_C$  values ( $\sim 15.52 \text{ kOe}$ ) for  $T < 20 \text{ K}$  under both ZFC and FC conditions. A clear anomaly across the compensation temperature is evident from  $H_C$ -T,  $H_{EB}$ -T and  $M_R$ -T curves (as indicated by arrow marks in figure 5.10 and 5.11). At very low temperatures  $T \leq 5 \text{ K}$ , these M-H loops exhibit linear behavior with lesser  $H_C$  values, and shift towards left from the origin. However, as the temperature approaches 10 K, M-H loop opens-up widely, and exhibits maximum  $H_C$  value, thereafter, starts decreasing continuously with increasing the temperature, as shown in the figures 5.10 and 5.11. Finally, the  $M_R$  and  $H_C$  approach to zero as  $T \rightarrow T_N$ .

The most striking feature of these M-H loops (measured under the ZFC condition) is that a substantial shift towards left side from the origin. This feature becomes more significant under FC condition (with  $H @ 20 \text{ kOe}$ ), as depicted in the figure 5.9. Using this key result we quantified the loop asymmetry by defining the exchange-bias field  $H_{EB}$ , i.e., the amount of shift in the center of M-H loop with respect to the origin as  $H_{EB} = (H_+ + H_-)/2$ , and the resultant coercive field, i.e.,  $H_C = (H_+ - H_-)/2$ , where  $H_+$  and  $H_-$  characterizes the magnitude of field at



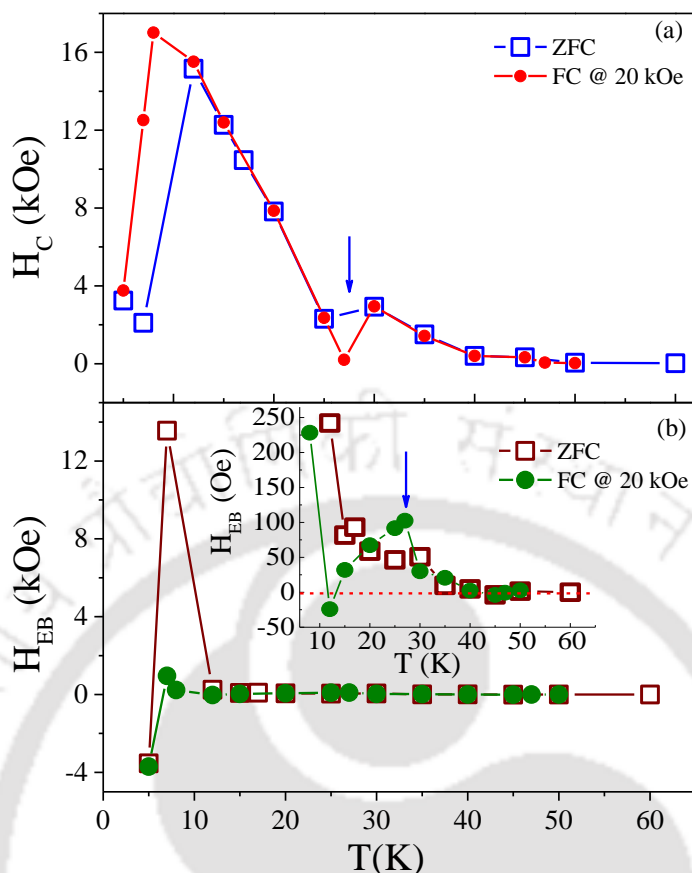
**Figure 5.8:** The magnetization ( $M$ ) versus field ( $H$ ) hysteresis loops of  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$  samples recorded at select temperatures (a) 5 K, (b) 12 K, (c) 20 K (d) 30 K (e) 40 K and (f) 50 K under zero-field-cooled ZFC condition. The insets show the zoomed view of  $M$ - $H$  loops near origin showing the asymmetry in the loops.

right-hand-side and left-hand side of the origin of  $M$ - $H$  graph. Figure 5.10 shows the temperature variation of such exchange-bias  $H_{\text{EB}}(T)$  and coercive field  $H_{\text{C}}(T)$  under both ZFC and FC conditions. Both  $H_{\text{C}}(T)$  and  $H_{\text{EB}}(T)$  takes peak shape across  $T = 8$  K and drops suddenly. Also, for  $T < T_{\text{COMP}}$ , the  $M_{\text{R}}(T)_{\text{ZFC}}$  and  $M_{\text{MAX}}(T)_{\text{ZFC}}$  show a cusp like shape with the maximum value of  $M_{\text{R}}^{\text{Max}} = 1.36 \text{ emu g}^{-1}$ . For  $T > T_{\text{COMP}}$ , both the curves  $M_{\text{MAX}}(T)$  and  $M_{\text{R}}(T)$  again start to increase up to  $T_{\text{N}}$  and fall off gradually beyond  $T_{\text{N}}$  (identical scenario was observed in FC condition as well). Both  $H_{\text{EB-FC}}(T)$  and  $H_{\text{EB-ZFC}}(T)$  gradually decrease with increasing temperature, and approaches zero across  $T_{\text{N}}$ . The increase of the coercive field below  $T_{\text{F}}$  may be due to the growing up of the spin-glass component. The  $H_{\text{C}}(T)$  curve takes a peak shape with maximum value  $H_{\text{C}}^{\text{Max}} = 17.02 \text{ kOe}$  at 8 K under ZFC and  $\sim 15.52 \text{ kOe}$  at 12 K under FC. It is interesting to note that an unusual crossover of sign from positive to negative values of  $H_{\text{EB}}$  ( $= -3.71 \text{ kOe}$  and  $-3.53 \text{ kOe}$  under ZFC and FC conditions, respectively) was observed below 7 K (clearly shown in the inset of figure 5.10b). Such giant bipolar switching of  $H_{\text{EB}}$  clearly signifies the role of field induced negative magnetization due to the underlying magnetic compensation effect. On the other hand, the  $M_{\text{R}}$  versus  $T$  and the temperature dependence of maximum magnetization values  $M_{\text{MAX}}$  measured at  $H = 68.3 \text{ kOe}$  drops to zero at  $T_{\text{COMP}}$  where the two-sublattice magnetizations ( $M_{\text{A}}$  and  $M_{\text{B}}$ ) balances with each other (figure 5.11). Also, the  $M_{\text{R}}$  versus  $T$  curve exhibits a second maximum centered at  $T_{\text{SG}}$  and finally drops to zero. Generally,  $H_{\text{EB}}$  has been experimentally witnessed only in the systems cooled under the presence of external magnetic field well above the



**Figure 5.9:** The magnetization ( $M$ ) versus field ( $H$ ) hysteresis loops of  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$  samples recorded at select temperatures (a) 5 K, (b) 12 K, (c) 20 K (d) 27 K (e) 40 K and (f) 50 K under @ 20 kOe field-cooled (FC) condition. The insets show the zoomed view of  $M$ - $H$  loops near origin showing the asymmetry in the loops.

Néel temperature or spin-glass freezing point. Such systems usually comprises of variety of interfaces like ferromagnetic (FM) - antiferromagnetic (AFM) [130], FM-SG [131], FM-ferrimagnetic [132], AFM-ferrimagnetic [133] and AFM-SG [134, 135]. However, few recent papers have reported significant  $H_{\text{EB}}$  even under the zero-field cooled samples of bulk Ni-Mn-In alloys [136] and in bulk  $\text{Mn}_2\text{PtGa}$  [137]. The source of such unusual  $H_{\text{EB}}$ , under zero-field-cooled sample, was attributed to the presence of complex magnetic interfaces such as ferrimagnetic/spin-glass or AFM/spin-glass phases [135, 136]. Few recent reports suggested that large exchange anisotropy originating from the exchange interaction between the compensated host and ferromagnetic clusters that arise from intrinsic anti-site-disorder (ASD) [179, 197]. It is believed that the origin of  $H_{\text{EB}}$  in the present context is likely resulting from similar phenomenon since the  $\text{Co}_2\text{TiO}_4/\text{Co}_2\text{SnO}_4$  intrinsically possess disorder due to the dilution effect (by Ti/Sn atoms). Such disorder is expected to enhance even more by disturbing the spinel lattice with the incorporation of slightly different ionic size of Sn. The double perovskite like systems usually possesses high degree of ASD due to which mixed exchange interactions become prominent, and finally leading to the spin-glass like phase at low-temperatures. Such process in-turn cause loop-asymmetry (or exchange-bias) through the microscopic interfaces of spin-glass phase and ferrimagnetic phase [198]. Since the current system  $\text{Co}_2\text{Ti}_{0.06}\text{Sn}_{0.04}\text{O}_4$  exhibits coexistence of spin-glass ordering and ferrimagnetic behavior, we expect the ASD is likely source of giant  $H_{\text{EB}}$  noticed at low-temperatures. The sign-reversal behavior of the exchange-bias

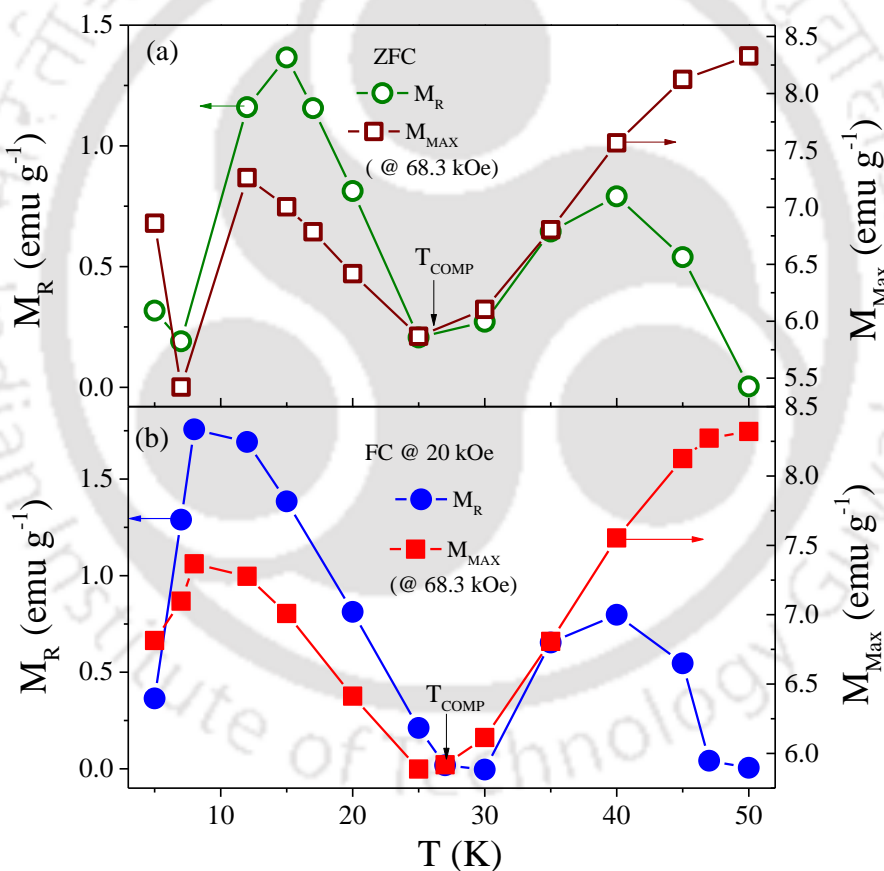


**Figure 5.10:** The temperature variation of (a) coercive field  $H_C(T)$  and (b) exchange bias  $H_{EB}(T)$  of  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$  recorded from the M-H curves measured under both ZFC and FC conditions. The inset of Figure (b) clearly shows the anomalous behaviour of  $H_{EB}$  across the  $T_{\text{COMP}}$ .

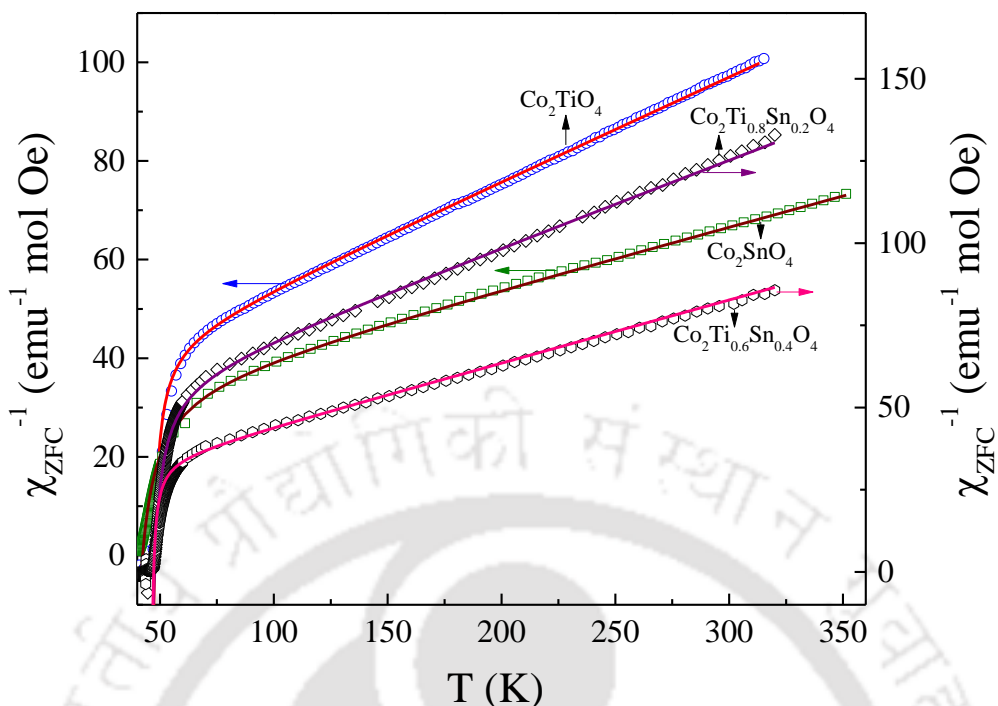
effect is clearly evident in both the pristine compounds  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{SnO}_4$  together with intermediate system  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$ . Nevertheless, the magnitude of  $H_{EB}$  measured under FC protocol (below 10 K) is much lower than  $H_{EB}$  obtained in ZFC case for all the investigated systems. For  $T > 10$  K, the magnitude of  $H_{EB}$  is quite small as compared to the  $H_{EB}$  values measured at lower temperatures, yet the anomalous behavior of  $H_{EB}(T)$  is prominent across the ordering temperatures  $T_{\text{COMP}}$ ,  $T_{\text{SG}}$  and  $T_{\text{N}}$  (Figure 5.10). Moreover, the sign reversal of  $H_{EB}$  closely related with large increase in the magnetic entropy  $dS/dT$  (not shown) and ground state spin configuration of  $\text{Co}^{2+}$  ions in the field of tetrahedral crystal field symmetry [152]. The inability of the spins in the frozen clusters to follow the magnetic field below 10 K, is one main possible source of obtaining very large  $H_C$  and  $H_{EB}$  values.

Following the Néel's theory, the collapse of  $M_R$  and  $H_C$  near the  $T_{\text{COMP}}$  is frequently related to the corresponding collapse of the mean-square value of the disordered transverse spin component considered over a macroscopic scale [199, 200]. Yet, we believe that the reversal of the magnetic moments on either side of the  $T_{\text{COMP}}$  leads to the sign reversal of  $H_{EB}$ . Therefore, in the presence of magnetic field the transition at  $T_{\text{COMP}}$ ,  $M_R$  suddenly collapses, and anomalies observed in  $H_{EB\text{-FC}}(T)$  have a common origin of the local spin-reversal of the  $\text{Co}^{2+}$  magnetic moments occupied in the A- and B-sites of the spinel configuration. The concept of magnetization

reversal can be clearly seen in the figure 5.11, where, a sudden decrease of the  $M_{\text{MAX}}$  values to  $6 \text{ emu g}^{-1}$  occurs exactly at  $T_{\text{COMP}} = 27 \text{ K}$  for  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$ . Since the ground state ( $^4T_1$ ) spin configuration of  $\text{Co}^{2+}$  ions in the octahedral symmetry, is significantly split by the spin-orbit coupling into six Kramers doublets. Thus, one can expect a distinctly different spin arrangement of all the ions occupied in the tetrahedral crystal field. Therefore, the interaction of externally applied magnetic field with such diverse spin configuration, significantly alters the net alignment of magnetization with unequal amounts, and finally resulting in the sign reversal of total magnetization on either side of  $T_{\text{COMP}}$ . Such features may appear more significant at very high fields, for example,  $H_{\text{dc}} \geq 50 \text{ kOe}$ , because, at low fields (10 - 20 kOe) the transition in  $C_p(T)$  for the  $x = 0$  system (chapter 4, section 4.3.7) shows a feeble anomaly at 31.74 K, but, this anomaly becomes more prominent at  $H_{\text{dc}} \geq 50 \text{ kOe}$ . Similarly, we expect even larger values of  $H_{\text{EB-FC}}(T)$  than - 3.71 kOe at 5 K, if we cool the system in the presence of higher magnetic fields greater than 50 kOe.



**Figure 5.11:** Left-hand-side scale shows the remanence magnetization versus temperature ( $M_R$  versus  $T$ ) of  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$  system measured under (a) zero-field-cooled (ZFC), and (b) field-cooled (FC) conditions. The right-hand-side scale shows the variation of the high field ( $H \sim 68.3 \text{ kOe}$ ) magnetization versus temperature measured under both (a) ZFC and (b) FC conditions. All these curves clearly show the sudden drop of magnetization value across the  $T_{\text{COMP}} (\sim 27 \text{ K})$ .



**Figure 5.12:** Temperature variation of the inverse-magnetic susceptibility  $\chi^{-1}(T)$  of  $\text{Co}_2\text{Ti}_{1-x}\text{Sn}_x\text{O}_4$  ( $0 \leq x \leq 1$ ). The solid lines are best-fits to the Néel's expression for ferrimagnets as discussed in the text.

### 5.3.4 Temperature Dependence of the Paramagnetic Susceptibility:

The temperature dependence of inverse dc-magnetic susceptibility curves  $\chi^{-1}(T)$ , for various compositions of  $\text{Co}_2\text{Ti}_{1-x}\text{Sn}_x\text{O}_4$  samples, recorded under zero-field cooled condition is fitted to the Néel's expression  $(1/\chi) = (T/C) + (1/\chi_0) - [\sigma_0/(T - \theta)]$  for ferrimagnets, as shown figure 5.12. The scattered symbols are representing the experimental data points and the solid curve is theoretical fit to the above expression. The fitting parameters obtain from the Néel's expression are shown in table 5.2. The strength of the antiferromagnetic exchange coupling, between the two  $\text{Co}^{2+}$  spins on the tetrahedral 'A' and octahedral 'B' sites, are often termed as asymptotic Curie temperature  $T_a = C/\chi_0$ . The corresponding values of  $T_a$  being 162.11 K, 177.55 K, 121.67 K, 112.133 K for the compositions  $x = 0, 0.2, 0.4, 1.0$  respectively. The effective magnetic moment  $\mu_{\text{eff}} = 6.16 \mu_B$  per formula unit (f.u.) of parent compound  $\text{Co}_2\text{TiO}_4$  is determined using  $C = N\mu_{\text{eff}}^2/3k_B$ . Since the tetrahedral co-ordination does not allow orbital contribution, the magnetic moment at A-site of  $\text{Co}^{2+}$  ions is fixed as  $\mu(A) = 3.87 \mu_B$  with spin  $S = 3/2$  and  $g = 2$  and  $\mu(B) = 4.79 \mu_B$  is estimated using the formula  $\mu_{\text{eff}}^2 = [\mu(A)]^2 + [\mu(B)]^2$  for  $\text{Co}_2\text{TiO}_4$ . Table 5.2 summarizes the magnetic moments at tetrahedral A- and octahedral B- sites for various compositions of 'Sn' substituted  $\text{Co}_2\text{TiO}_4$ . The important feature of  $\text{Co}_2\text{TiO}_4$ , is that the observation of compensation temperature at 32 K below which the system retains its ferrimagnetic character. On the contrary, similar compensation point was not exhibited by  $\text{Co}_2\text{SnO}_4$  even though for  $T < 7$  K, there was no coercive force or remanence magnetization in this system which is typical characteristics of a compensated state. The large magnitudes of the coercivity, observed in tin substitute cobalt-orthotitanate, in the uncompensated state is most likely results from the growth

**Table 5.2:** The list of various parameters obtained from the Néel's fits of  $\chi^{-1}$  versus T curve with the experimental data points of various compositions of Co<sub>2</sub>Ti<sub>1-x</sub>Sn<sub>x</sub>O<sub>4</sub> ( $0 \leq x \leq 1$ ) recorded under zero-field-cooled condition. [\*Co<sub>2</sub>TiO<sub>4</sub> sample sintered at 1100°C, results of previous chapter].

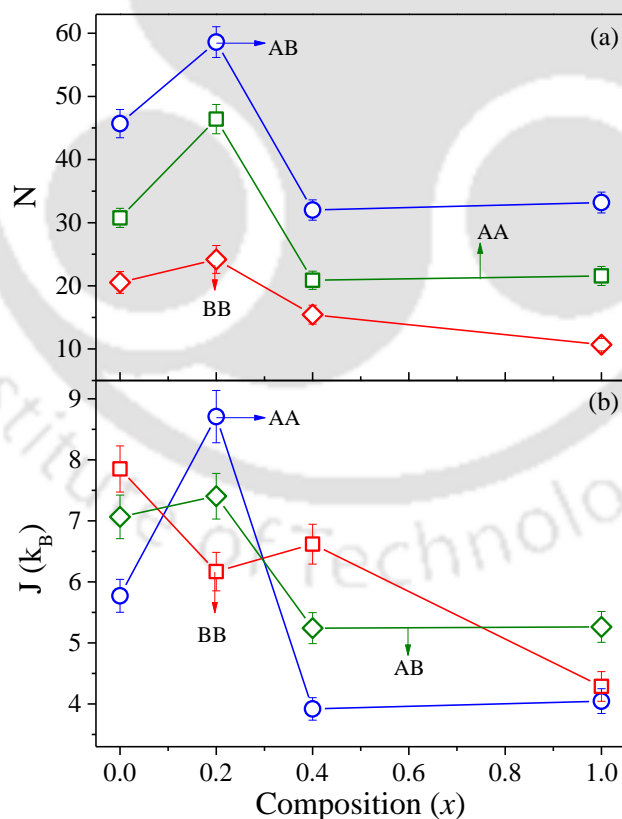
System	C	$\chi_0$	$\sigma_0$	$\theta$	$\mu_{\text{eff}}$	$\mu$ (A)	$\mu$ (B)
	(emu K mol <sup>-1</sup> Oe <sup>-1</sup> )	(emu mol <sup>-1</sup> Oe <sup>-1</sup> )	(emu <sup>-1</sup> Oe mol K)	(K)	( $\mu_B$ )	( $\mu_B$ )	( $\mu_B$ )
Co <sub>2</sub> TiO <sub>4</sub>	4.75±0.02	0.029±0.013	98.04±0.01	45.48±0.01	6.16±0.01	3.87	4.79±0.01
Co <sub>2</sub> Ti <sub>0.8</sub> Sn <sub>0.2</sub> O <sub>4</sub>	3.79±0.01	0.021±0.012	201.97±0.01	44.19±0.01	5.50±0.0	3.87	3.91±0.01
Co <sub>2</sub> Ti <sub>0.6</sub> Sn <sub>0.4</sub> O <sub>4</sub>	5.09±0.01	0.042±0.011	32.83±0.01	46.50±0.01	6.38±0.01	3.87	5.07±0.01
Co <sub>2</sub> SnO <sub>4</sub>	4.89±0.01	0.044±0.012	102.37±0.01	39.5±0.01	6.25±0.01	3.87	4.91±0.01
*Co <sub>2</sub> TiO <sub>4</sub>	5.25±0.02	0.042±0.012	31.55±0.01	49.85±0.01	6.5±0.01	3.87	5.19±0.01

of frozen-spin clusters formed as a result of the different magnetic moments of the cations residing in the octahedral B-sites. Also, the field dependent magnetization reversal, and lack of saturation of the magnetization noticed in these systems, below the ferrimagnetic ordering in magnetic fields up to as high as 150 kOe, suggests the complex canting of the magnetic moments, which can be best determined by neutron diffraction measurements.

### 5.3.5 Compositional Dependence of Exchange-Interaction:

Usually, the superexchange interaction in magnetically ordered insulators with spinel-crystal structure was adequately described by three nearest neighbour exchange constants ( $J_{AA}$ ,  $J_{AB}$  and  $J_{BB}$  where A and B refer to the ions on the tetrahedral and octahedral sites, respectively). Among various theoretical and experimental techniques established to evaluate the magnitude of such exchange-parameters, the temperature dependence of paramagnetic susceptibility is one constructive experimental method through which one can estimate the precise values of  $J$ . Using the parameters obtained from the Néel's fits we have determined the molecular field constants ( $N_{AA}$ ,  $N_{BB}$  and  $N_{AB}$ ) and the corresponding exchange constants ( $J_{AA}$ ,  $J_{BB}$  and  $J_{AB}$ ) for all the compositions (figure 5.13a and 5.13b) [131]. The magnitudes of antiferromagnetic exchange constants evaluated from the Néel's expression are  $J_{AA} = 3.92 k_B$  (5.77  $k_B$ ),  $J_{BB} = 6.62 k_B$  (7.85  $k_B$ ) and  $J_{AB} = 5.24 k_B$  (7.07  $k_B$ ) for Co<sub>2</sub>Ti<sub>0.6</sub>Sn<sub>0.4</sub>O<sub>4</sub> (un-doped), respectively. Below 'T<sub>N</sub>' the net small moment of 0.92  $\mu_B$  per f.u ( $\mu(B) - \mu(A)$ ) was noticed from the M-T data. With increasing the 'Sn' content, the  $\mu_{\text{eff}}$  decreases first to 5.50  $\mu_B$  for 20 at% of 'Sn', and then increases to 6.38  $\mu_B$  for  $x = 0.4$ . This effect is consistent with the variation of the exchange integral (J) with respect to the Sn-composition ( $x$ ), as shown in the figure 5.13b. It is interesting to note that for the composition  $x = 0.2$ , both the 'A' and 'B' sites magnetic moments becomes almost equal ( $\Delta\mu = \mu(B) - \mu(A) \sim 0.04 \mu_B$ ), signifying the lacking

of spin-orbit coupling on the B-sites of  $\text{Co}_2\text{T}_{0.8}\text{Sn}_{0.2}\text{O}_4$ . Whereas, the difference in the magnetic moments at A and B sites  $\Delta\mu \sim 1.20 \mu_B$  and  $1.03 \mu_B$  for  $\text{Co}_2\text{T}_{0.6}\text{Sn}_{0.4}\text{O}_4$  and  $\text{Co}_2\text{SnO}_4$  systems, respectively suggesting the signature of spin-orbit coupling on the B-sites. The molecular field constants and exchange constants of various compositions of  $\text{Co}_2\text{T}_{1-x}\text{Sn}_x\text{O}_4$  ( $0 \leq x \leq 1$ ) are listed in table-5.3. Generally, for antiferromagnetic interaction between two spins, the estimated molecular field constants should satisfy the general requirements of  $N_{BB} > N_{AA}$  (for spinels), however, in the present case, we noticed that  $N_{AB}$  is dominant over  $N_{BB}$  and  $N_{AA}$  for all the compositions [18]. It is clear from the figure 5.13a that all the molecular field constants show maximum value for 20 at% Sn substituted  $\text{Co}_2\text{TiO}_4$  sample. Also, the exchange constant  $J_{AA}$  shows maximum value for  $\text{Co}_2\text{T}_{0.8}\text{Sn}_{0.2}\text{O}_4$ . On the other hand, for 100% Sn substitution (i.e.  $\text{Co}_2\text{SnO}_4$ ) the exchange constants follows the trend  $J_{AB} > J_{BB} > J_{AA}$ , whereas  $J_{BB}$  is dominating over other two exchange constants in the  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_2\text{T}_{0.6}\text{Sn}_{0.4}\text{O}_4$  samples (figure 5.13b). As discussed in the above section that possibility of ASD could result mixed exchange interactions, which may cause the collapse of long-range order, and lead to the spin-glass like phase at low-temperatures [137]. Dionne *et al.* reported that two entirely different set of exchange constants are needed to fit the inverse-magnetic- susceptibility data [201]. Moreover, the substitution of non-magnetic ions inside the magnetic-spinel sublattice alters the exchange-constants drastically, as, noticed in the current study for the intermediate composition  $x = 0.2$   $J_{AA} > J_{AB} > J_{BB}$ . Nevertheless, a complicated three-sublattice (A, B', B'')



**Figure 5.13:** The compositional variation of the (a) molecular field constants, and (b) exchange constants of  $\text{Co}_2\text{T}_{1-x}\text{Sn}_x\text{O}_4$ .

**Table 5.3:** The list of molecular-field constants, exchange constants and Landé g-splitting factors ( $g_A = 2$  and  $g_B$ ) obtained from the Néel's fits of paramagnetic susceptibility  $\chi^{-1}$  versus T for various compositions of Co<sub>2</sub>Ti<sub>1-x</sub>Sn<sub>x</sub>O<sub>4</sub> ( $0 \leq x \leq 1$ ) recorded under zero-field-cooled condition. \*Co<sub>2</sub>TiO<sub>4</sub> sample sintered at 1100°C.

System	N <sub>AA</sub>	N <sub>BB</sub>	N <sub>AB</sub>	J <sub>AA</sub> (k <sub>B</sub> )	J <sub>BB</sub> (k <sub>B</sub> )	J <sub>AB</sub> (k <sub>B</sub> )	g <sub>B</sub>
Co <sub>2</sub> TiO <sub>4</sub>	30.76±1.51	20.54±1.72	45.69±2.23	5.77±0.27	7.85±0.38	7.07±0.36	2.47±0.02
Co <sub>2</sub> Ti <sub>0.8</sub> Sn <sub>0.2</sub> O <sub>4</sub>	46.41±2.32	24.18±2.21	58.62±2.43	8.71±0.43	6.17±0.32	7.40±0.37	2.02±0.02
Co <sub>2</sub> Ti <sub>0.6</sub> Sn <sub>0.4</sub> O <sub>4</sub>	20.88±1.44	15.44±1.50	32.01±1.61	3.92±0.18	6.62±0.33	5.24±0.25	2.61±0.03
Co <sub>2</sub> SnO <sub>4</sub>	21.56±1.51	10.68±0.98	33.20±1.65	4.05±0.20	4.28±0.24	5.26±0.25	2.53±0.03
*Co <sub>2</sub> TiO <sub>4</sub>	17.32±1.54	35.70±1.71	12.72±1.12	3.25±0.16	3.18±1.51	4.47±0.24	2.47±0.02

molecular-field approximation model with different routes of superexchange interaction via the ligands was suggested by Srivastava *et al.* [165]. This approach is more appropriate for the inverse-spinel ferrite like compounds such as M<sup>2+</sup>Fe<sup>3+</sup>O<sub>4</sub> (M = Cu<sup>2+</sup>, Li<sub>0.5</sub><sup>+</sup>, Fe<sub>0.5</sub><sup>3+</sup>, Mn<sup>2+</sup>, Co<sup>2+</sup>, Ni<sup>2+</sup>, Fe<sup>2+</sup>, Fe<sub>0.5</sub><sup>3+</sup>) than the two-sublattice model proposed by Néel [165]. The molecular-field ( $H_i$ ) experienced by each ion located on the  $i^{\text{th}}$  sublattice, is related with the corresponding magnetization ( $M_j$ ) and molecular-field constant ( $N_j$ ) located at  $j^{\text{th}}$  sublattice through the following equations;  $H_A = N_{AA}M_A - N_{AB}M_{B'} - N_{AB'}M_{B''}$ ,  $H_B = -N_{AB}M_A + N_{B'B'}M_{B'} + N_{B'B''}M_{B''}$ , and  $H_C = -N_{AB'}M_A + N_{B'B'}M_{B'} + N_{B'B''}M_{B''}$ . In these equations, the quantity  $N_{ij}$  is equivalent to  $2Z_{ij}J_{ij}/\lambda_j g_j \mu_B^2$ , where,  $Z_{ij}$  is the number of nearest neighbour atoms on the  $j^{\text{th}}$  sublattice to an atom on the  $i^{\text{th}}$  sublattice,  $\lambda_j$  is the number of atoms per unit volume on the  $j^{\text{th}}$  sublattice,  $g_i$  and  $g_j$  are the Landé factors for the ions on the  $i^{\text{th}}$  and  $j^{\text{th}}$  sublattice respectively, and  $\mu_B$  is the Bohr magneton. On the basis of the above procedure Srivastava *et al.* reported six superexchange constants for various types of inverse spinels [165]. For example, CoFe<sub>2</sub>O<sub>4</sub> with lattice constant  $a_0 \sim 8.38 \text{ \AA}$  and the number of  $d$ -electrons ( $n$ ) = 7, the three-sublattice model yields  $-J_{AA} \sim 15 \text{ K}$ ,  $-J_{AB'} \sim 22.7 \text{ K}$ ,  $-J_{AB''} \sim 26 \text{ K}$ ,  $-J_{B'B'} \sim 18.5 \text{ K}$ , and  $-J_{B'B''} \sim 7.5 \text{ K}$  for the configurations  $d^{n-5} - d^{n-5}$ ,  $d^{n-5} - d^{n-6}$ ,  $d^{n-5} - d^{n-5}$ ,  $d^{n-6} - d^{n-6}$ ,  $d^{n-5} - d^{n-6}$ , and  $d^{n-5} - d^{n-5}$ , respectively. Similar analysis for the current systems may provide additional information, which will be helpful to completely understand the nature of the re-entrant magnetic ordering of the current system.

### 5.3.6 Summary:

To sum-up, the nature of magnetism in 'Sn' doped Co<sub>2</sub>TiO<sub>4</sub> was studied using detailed temperature dependence of dc-magnetization and ac-susceptibility. Our experimental results demonstrates the co-existence of ferrimagnetic ordering, and reentrant spin-glass state together with a magnetic compensation effect, similar to

## ***Chapter 5: Tuning the Compensation Point: Role of Sn Substitution in Co<sub>2</sub>TiO<sub>4</sub>***

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Co<sub>2</sub>TiO<sub>4</sub> but with different ordering temperatures e.g.  $T_N \sim 46.1$  K and  $T_F \sim 44.05$  K, and  $T_{COMP} = 27.1$  K for Co<sub>2</sub>Ti<sub>0.6</sub>Sn<sub>0.4</sub>O<sub>4</sub>. The interesting finding is polarity-reversal giant exchange-bias effect below  $T_{COMP}$  under both ZFC and FC conditions (i.e. coexistence of positive and negative  $H_{EB}$ ), and the collapse of  $M_R$  and  $H_C$  in the proximity of  $T_{COMP}$ . The ferrimagnetic transition at  $T_N$  is associated with ordering of the longitudinal-spin-component, whereas, spin-glass transition  $T_F$  is due to the freezing of the transverse spin component. These observations confirm the theoretical predictions proposed by Villian [40] in insulating magnetic systems containing the nonmagnetic impurities. The molecular field constants ( $N_{AA} = 20.88$ ,  $N_{BB} = 15.44$ , and  $N_{AB} = 32.01$ ) determined from the fitting of experimentally obtained temperature dependence of inverse paramagnetic susceptibility to the Néel's expression for ferrimagnetism were found to be antiferromagnetic in nature. Subsequently, the effective magnetic moments evaluated from the above method at A- and B-sites are  $\mu(A) = 3.87 \mu_B$  and  $\mu(B) = 5.07 \mu_B$  respectively.



## Crystal Structure, Vibrational Excitations, Dielectric and Magnetic Properties of Co<sub>3</sub>O<sub>4</sub> and Co<sub>2</sub>TiO<sub>4</sub> Two-Phase Composites

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### 6.1 Background:

The physical and chemical properties of binary transition-metal oxides (e.g: CoO, NiO, MnO, CuO etc.) and their alloys are well studied in the literatures because of their potential applications in Li-ion batteries, catalysis, transformer cores, sensors and ultra-high density magnetic recording media [3, 153, 202]. Such oxides with spinel crystal structure (Co<sub>3</sub>O<sub>4</sub>, Mn<sub>2</sub>O<sub>3</sub> and Mn<sub>3</sub>O<sub>4</sub>) are unique compounds because of their interesting physics resulting from a variety of distribution of magnetic cations between the tetrahedral A-sites and octahedral B-sites [103, 174, 203, 204]. Among such spinels tricobalt tetraoxide (Co<sub>3</sub>O<sub>4</sub>) and its solid-solutions under reduced-dimension, and bulk grain size have received much attention recently due to their unique photocatalytic properties, heterogeneous catalytic activity for NO<sub>x</sub> reduction, carbon monoxide oxidation, and removal volatile organic compounds (VOC) [10, 134, 205]. Co<sub>3</sub>O<sub>4</sub> (Co<sup>2+</sup>[Co<sup>3+</sup>]<sub>2</sub>O<sub>4</sub>) belongs to a normal spinel family with occupation of tetrahedral sites by Co<sup>2+</sup> ions and octahedral sites by Co<sup>3+</sup> ions respectively. The net magnetic moment arises due to Co<sup>2+</sup> ions largely because of spins, with a small contribution from spin–orbit coupling. On the other hand, the ground state configuration of the free Co<sup>3+</sup> ion is 3d<sup>6</sup>. In the strong crystal field limit, the 3d electrons are paired in the t<sub>2g</sub> levels and the Co<sup>3+</sup> is in the low spin state. Thus, Co<sup>3+</sup> ions have no permanent magnetic moment as a consequence of the splitting of 3d levels by the octahedral crystal field and complete filling of t<sub>2g</sub> levels. Co<sub>3</sub>O<sub>4</sub> shows an antiferromagnetic to paramagnetic transition with Néel temperature T<sub>N</sub> ≈ 40 K with each Co<sup>2+</sup> ion in the A-site having four neighboring Co<sup>2+</sup> ions of opposite spins [134, 174]. Recently, many studies have been initiated due to its prospective application in various field [206 - 208]. In particular, Jeong *et al.* reported that Cr-doped Co<sub>3</sub>O<sub>4</sub> nanorods can act as chemi-resistor for ultra-selective monitoring of methyl benzene [209]. Wu *et al.* reported that Li-doped Co<sub>3</sub>O<sub>4</sub> nanopowders with particle size 30 nm can act as promising oxygen evolution reaction (OER) catalysts [210]. Investigations on Ce-doped Co<sub>3</sub>O<sub>4</sub> nanostructures divulge the existence of multi-emission centers and ferromagnetic ordering at room-temperature caused by the surface effects and oxygen vacancies [211]. Origin of such long-range magnetic ordering is debatable due to the fact that Co<sub>3</sub>O<sub>4</sub> exhibits antiferromagnetic behavior with Néel temperature (T<sub>N</sub> = 30 K) far below the room-temperature [10, 205, 206]. Recent studies by Durand *et al.* affirmed that the anomalous magnetic and structural properties exhibited by the LaCoO<sub>3</sub> are due to the presence of crystalline impurity phases, predominately that of Co<sub>3</sub>O<sub>4</sub> [212]. Wang *et al.* suggested that nanocomposites made-up of N-doped porous carbon and Co<sub>3</sub>O<sub>4</sub> can assist as potential anode material for lithium-ion batteries [213].

Excellent battery-cycling stability was noticed in the composites comprising of Co<sub>3</sub>O<sub>4</sub> and mesoporous carbon with large surface area as compared with the reference system synthesized in pure ethanol [214]. The Co<sub>3</sub>O<sub>4</sub>

nanowires decorated with functionalized carbon-nanotubes have been explored recently for the high-performance super-capacitive properties ( $559 \text{ F g}^{-1}$ ) as compared with the pristine compound. Such 3D nanostructures exhibit exceptional cycling-stability i.e. little increase in the capacitance value instead of degradation after  $10^3$  cycles of charge-discharge process performed at the rate of  $2 \text{ A g}^{-1}$  [215]. Furthermore, Lin *et al.* exploited the gas-sensing characteristics of 1D  $\text{Co}_3\text{O}_4$ /polyethyleneimine-carbon-nanotube composite [216]. Development of such complexes may open a constructive approach to create low-cost and large-scale production of carbon monoxide and  $\text{NH}_3$  gas sensors. Majority of the reports in the literature are focused on the catalytic properties, gas sensing features, and enhanced electrode performance in Li-ion batteries by either substituting different elements within the  $\text{Co}_3\text{O}_4$  matrix or making nanocomposites consisting of  $\text{Co}_3\text{O}_4$  [214 - 218]. Previous studies by Inagaki *et al.* reported that  $\text{Co}_2\text{TiO}_4$  decomposes to  $\text{Co}_3\text{O}_4$  and  $\text{CoTiO}_3$  at  $727^\circ\text{C}$  [219]. The submicron particles of  $\text{TiO}_2$  and  $\text{Co}_3\text{O}_4$  react at about  $700^\circ\text{C}$  to form the  $\text{CoTiO}_3$ , which crystallizes into ilmenite crystal structure. However, this phase is not stable at very high temperatures  $T > 1200^\circ\text{C}$ , instead  $\text{Co}_2\text{TiO}_4$  forms as a stable phase. Despite of various reports available, a systematic study of ‘Ti’ doped  $\text{Co}_3\text{O}_4$  or the solid solutions of  $\text{Co}_3\text{O}_4$  and  $\text{Co}_2\text{TiO}_4$  were not reported in the literature when we started to work on this problem. Therefore, a detailed study related to the diffusion of  $\text{TiO}_2$  within the  $\text{Co}_3\text{O}_4$  matrix was initiated in this chapter. Eventually, the solid-solution system forms a stable two-phase composite system comprising of both  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_3\text{O}_4$ . We synthesized various compositions ( $x$ ) of the solid solutions of  $(1-x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  ( $0 \leq x \leq 1$ ) and investigated the changes occurring in their (i) crystal structure, (ii) elemental analysis and local environment, (iii) vibrational excitation spectroscopy, (iv) magnetic, and (v) dielectric properties.

## **6.2. Experimental Details:**

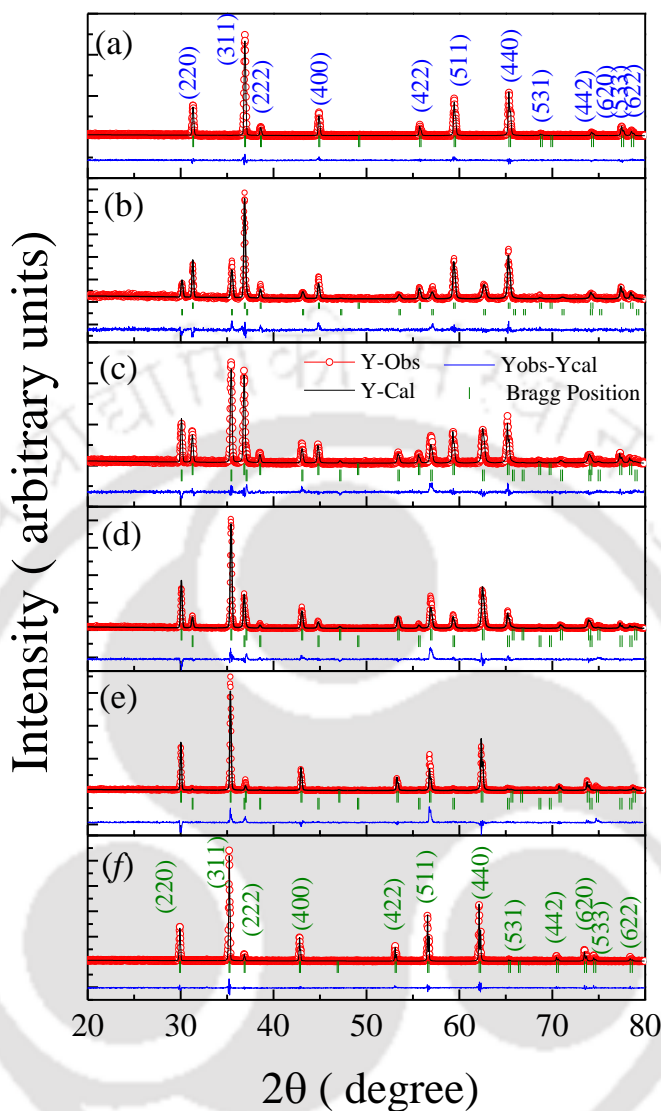
Various compositions of two-phase composites  $(1-x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  ( $0 \leq x \leq 1$ ) were synthesized by solid state reaction method starting with the stoichiometric amount of  $\text{Co}_3\text{O}_4$  (Alfa Aesar, purity 99.99%) and  $\text{TiO}_2$  (Alfa Aesar, purity 99.99%) as precursors. These mixed powders were first ground in an agate mortar and then pressed into cylindrical pellets of 13 mm diameter using a hydraulic press, followed by sintering at  $1200^\circ\text{C}$  for 8 h in air to yield final compound. To examine the structural properties of these samples an X-ray diffractometer from Rigaku (model: TTRAX III) with  $\text{Cu-K}_\alpha$  radiation of wavelength  $\lambda = 1.5406 \text{ \AA}$  was employed. Microstructure of the samples were examined using a Scanning Electron Microscope (SEM, LEO 1430 VP) equipped with energy dispersive X-ray analyzer. Raman spectra were recorded on the powder samples at room temperature using a micro-Raman spectrometer from Horiba Jobin Vyon (LabRam HR) operating at 514 nm wavelength excitation laser. For the low-temperature Raman measurements (down to 25 K) a different (Jobin Yvon T64000) spectrometer was employed, which is equipped with a dedicated heating/cooling sample stage (Linkam, THMS600). All the spectra of sintered samples were recorded in back-scattered geometry equipped with a 50x objective, appropriate edge filter, and a Peltier cooled charge-coupled device detector. An  $\text{Ar}^+$  ion excitation laser

source under high-resolution dispersive geometry was used for these low-temperature micro-Raman measurements with wavelength  $\lambda = 514$  nm and an 1800 lines/mm grating. The spectral resolution of the system is approximately  $1 \text{ cm}^{-1}$ . For high degree of positional accuracy the grating was fixed at unmoved condition during the entire temperature scan. The FTIR spectra of the compounds were recorded using a Perkin-Elmer 180 Spectrometer in the range of  $4000\text{--}400 \text{ cm}^{-1}$  with the spectral resolution of  $\pm 2 \text{ cm}^{-1}$ . A small amount of sample was first diluted with 150 milligrams of vacuum-dried IR-grade potassium bromide powder and subjected to a pressure of 39.2 bar. For the elemental analysis of the elements present in the samples, a dual source X-ray photoelectron spectroscope (Al- $K_\alpha$  @ 1486.8 eV, Mg- $K_\alpha$  @ 1253.6 eV) from VG Microtech, equipped with ultra-high vacuum ( $8 \times 10^{-10}$  Torr) chamber with pass energy of 100 eV, was employed. The XPS spectra were recorded using mono-chromatized Al- $K_\alpha$  radiation, and the binding energies were calibrated against the C-1s peak 284.5 eV. Both dc-magnetization and frequency dependence (0.17 Hz - 1.2 kHz) of ac-magnetic susceptibility measurements were performed using a superconducting quantum interference device (SQUID) based magnetometer from Quantum Design with temperature capabilities of 5 K – 320 K and magnetic field (H) up to  $\pm 70$  kOe. High frequency ( $100 \text{ Hz} \leq f \leq 30\text{MHz}$ ) ac-electrical resistivity and dielectric permittivity studies of all the composites were performed between the temperatures -120 K and 570 K using the impedance and gain-phase analyzer from from Novocontrol Alpha AN impedance analyzer with Quatro cryosystem. A pour-fill liquid nitrogen cryostat was assembled with the impedance analyzer to achieve the low-temperatures below 300 K, where as a home-made heater was designed to realize high temperature measurements.

### **6.3. Characterizations:**

#### **6.3.1. Structural Analysis:**

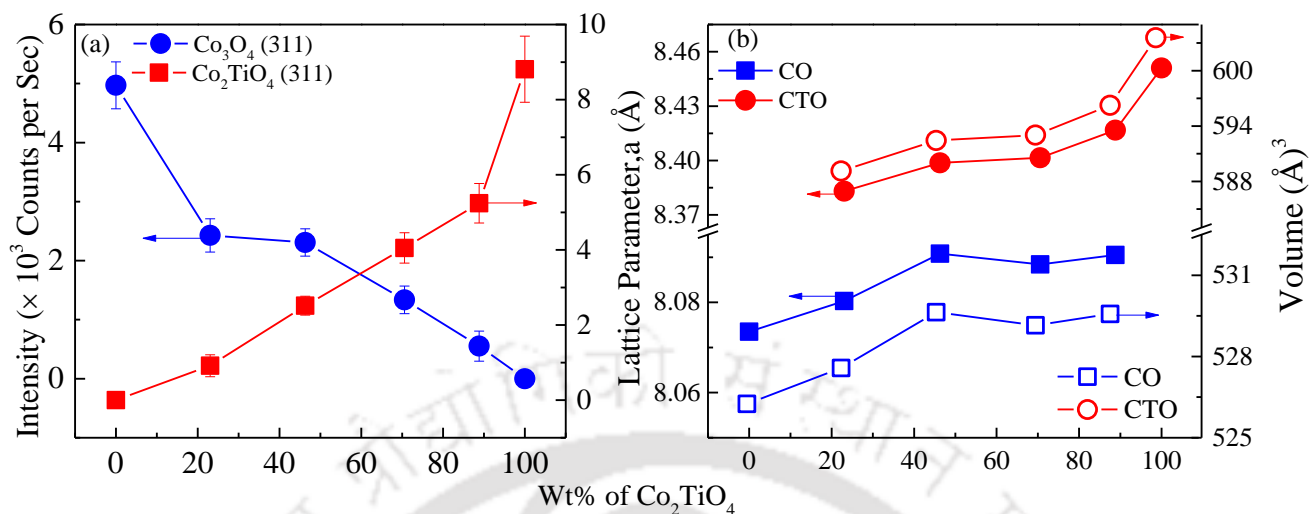
Figure 6.1 shows the X-ray diffraction pattern and the corresponding Rietveld refinement data of  $(1 - x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  samples for different values of  $x$  wt% including pure  $\text{Co}_3\text{O}_4$  ( $x = 0$  wt%) and  $\text{Co}_2\text{TiO}_4$  ( $x = 100$  wt%). The Rietveld refinement was performed using FullProf suite. For the un-doped case (i.e.  $\text{Co}_3\text{O}_4$ ) and lower values of 'x' i.e. dilute substitution of  $\text{Co}_2\text{TiO}_4$ . The X-ray diffraction patterns were analogous to the normal spinel structure similar to that of pure  $\text{Co}_3\text{O}_4$  without any secondary phase. All these diffraction pattern were corresponding to the space group  $Fd\bar{3}m$  (227) [JCPDS 43-1003]. However, slight difference in the lattice parameter ('a' = 8.074 Å) was noticed as compared with the standard values of  $\text{Co}_3\text{O}_4$  ('a' = 8.077 Å). As the composition increases, the diffraction peaks corresponding to the inverse spinel cobalt-orthotitanate ( $\text{Co}_2\text{TiO}_4$ ) becomes more prominent (lattice parameter  $a = 8.45$  Å). This secondary phase formation increases progressively with increasing the  $x$ . The Miller indices of planes are shown in blue color in figure 6.1 and the obtained lattice constant is in close agreement with the standard value 8.434 Å [JCPDS 39-1410]. The weight % of both these phases were quantitatively analyzed using the following equation [110].



**Figure 6.1:** The X-ray diffraction pattern together with the Rietveld refined data of composite system  $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$  for (a)  $x = 0$ , (b)  $x = 0.23$ , (c)  $x = 0.463$ , (d)  $x = 0.706$ , (e)  $x = 0.882$ , and (f)  $x = 1$ .

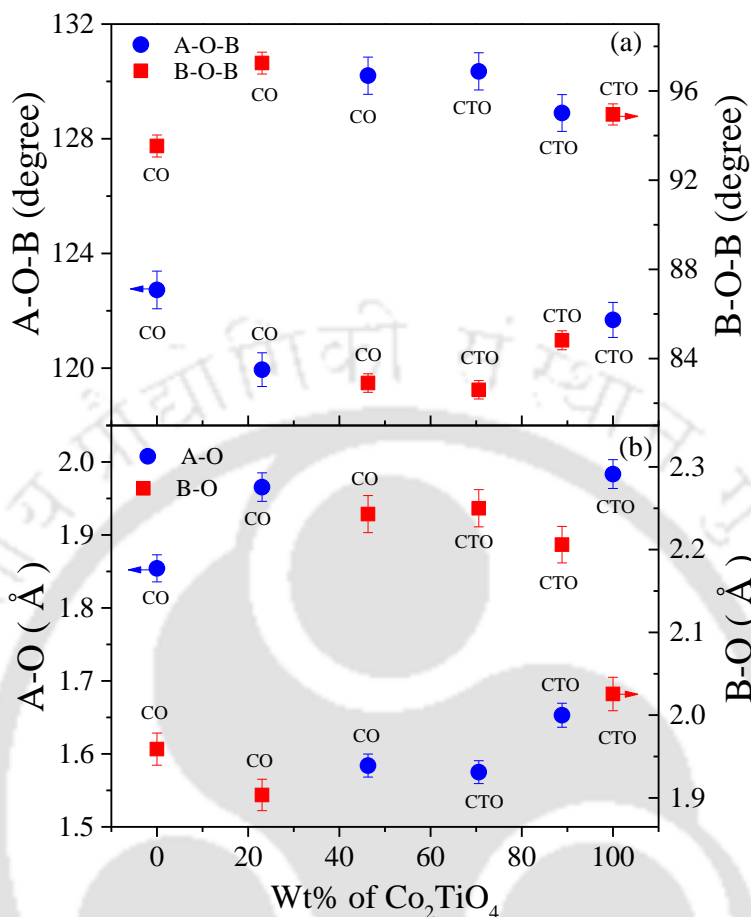
$$W_{\text{CTO}} = [1/\{1 + 1.265 (I_{\text{CO}}/I_{\text{CTO}})\}] \times 100 \quad \dots (6.1)$$

where  $W_{\text{CTO}}$  indicates the weight fraction of the  $\text{Co}_2\text{TiO}_4$  phase,  $I_{\text{CTO}}$  and  $I_{\text{CO}}$  represents the strongest X-ray diffraction line intensities of the  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_3\text{O}_4$ , respectively. In the present case, diffraction intensity of (311) peak of both the phases were considered as highest intensity peak. Using the above equation the evaluated weight % ( $x$ ) of  $\text{Co}_2\text{TiO}_4$  are  $x = 0, 23.05, 46.3, 70.6, 88.8$  and  $100\%$  consistent with the theoretically estimated weighed quantities  $0, 23, 45, 70, 88$  and  $100\%$  respectively. The intensity ratio of the XRD peak intensities of two phases  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_3\text{O}_4$  are shown as a function of wt% (figure 6.2(a)).



**Figure 6.2:** (a) Intensity of the (311) reflection of both  $\text{Co}_3\text{O}_4$  and  $\text{Co}_2\text{TiO}_4$  phases of the composites ( $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$  [ $0 \leq x \leq 1$  (100 wt%)]) (b) The composition variation of lattice parameter ‘ $a$ ’ and unit-cell volume ‘ $V$ ’ of  $\text{Co}_3\text{O}_4/\text{Co}_2\text{TiO}_4$  two phase composite. Note: The contribution of both the phases ( $\text{Co}_3\text{O}_4$  and  $\text{Co}_2\text{TiO}_4$ ) is plotted separately.

Figure 6.2(b) shows the variation of lattice parameters ‘ $a$ ’ and the volume of the unit-cell ‘ $V$ ’ as a function of  $\text{Co}_2\text{TiO}_4$  wt% ( $x$ ). Up to  $x = 0.463$  both ‘ $a$ ’ and ‘ $V$ ’ increases (for  $\text{Co}_3\text{O}_4$ ) and attains a maximum value of 8.09  $\text{\AA}$ , beyond which no significant variation was noticed. On the contrary, for  $\text{Co}_2\text{TiO}_4$  both ‘ $a$ ’ and ‘ $V$ ’ were found to increase progressively with increasing the ‘ $x$ ’. Since the ionic radius of either  $\text{Ti}^{4+}$  ( $= 0.605 \text{\AA}$ ) or  $\text{Ti}^{3+}$  ( $= 0.67 \text{\AA}$ ) is larger than the ionic radius of  $\text{Co}^{3+}$  ( $0.545 \text{\AA}$ ) at the octahedral location (i.e. B-sites), one can expect a significant expansion of the unit-cell volume due to the substitution of ‘Ti’ ions at the  $\text{Co}^{3+}$  locations in the  $\text{Co}_3\text{O}_4$  matrix. Nevertheless, for  $x = 0.463$  the formation of  $\text{Co}_2\text{TiO}_4$  grains disturbs the ‘A’ and ‘B’ sites of  $\text{Co}_3\text{O}_4$  system which may cause some alteration in the average unit cell volume. Beyond  $x = 0.463$ , the secondary phase  $\text{Co}_2\text{TiO}_4$  dominates over  $\text{Co}_3\text{O}_4$  phase and no significant change in the ‘ $a$ ’ and ‘ $V$ ’ values was noticed for both the systems. For a clear understanding of such fine variations in ‘ $a$ ’ and ‘ $V$ ’ we have estimated the bond-angles (A-O-B and B-O-B) and bond-lengths (A-O and B-O) of major phase for various compositions as shown in figure 6.3. These bond-angles and bond-lengths are corresponding to the major phase (i.e. normal spinel  $\text{Co}_3\text{O}_4$ ) up to  $x = 0.463$  (46.3 wt%), beyond which, the bond-angles and bond-lengths parameters corresponding to the inverse spinel  $\text{Co}_2\text{TiO}_4$  phase, which is the dominant phase in the composite system. For lower compositions the bond angle A-O-B ( $122.72^\circ$ ) at first decreases and then suddenly increases reaching a maximum value of  $130.35^\circ$  for  $x = 0.706$  (70.6 wt%), and again starts decreasing as the formation of inverse-spinel structure dominates. However, exactly opposite trend was noticed in the case of B-O-B angle. As the system transforms from normal to inverse spinel the bond length A-O = 1.854  $\text{\AA}$  for  $x = 0$  (i.e. for  $\text{Co}_3\text{O}_4$ ) and 1.984  $\text{\AA}$  for  $x = 1$  (100 wt% or  $\text{Co}_2\text{TiO}_4$  as a whole) and B-O = 1.958  $\text{\AA}$  for  $x = 0$  (i.e. for  $\text{Co}_3\text{O}_4$ ) and 2.025  $\text{\AA}$  (i.e. for  $\text{Co}_2\text{TiO}_4$ ). Nonetheless, these values are slightly higher as compared to the standard bond angles ( $121^\circ_{\text{A-O-B}}$ ,  $95.7^\circ_{\text{B-O-B}}$ ) of  $\text{Co}_3\text{O}_4$ . No significant lattice strain was

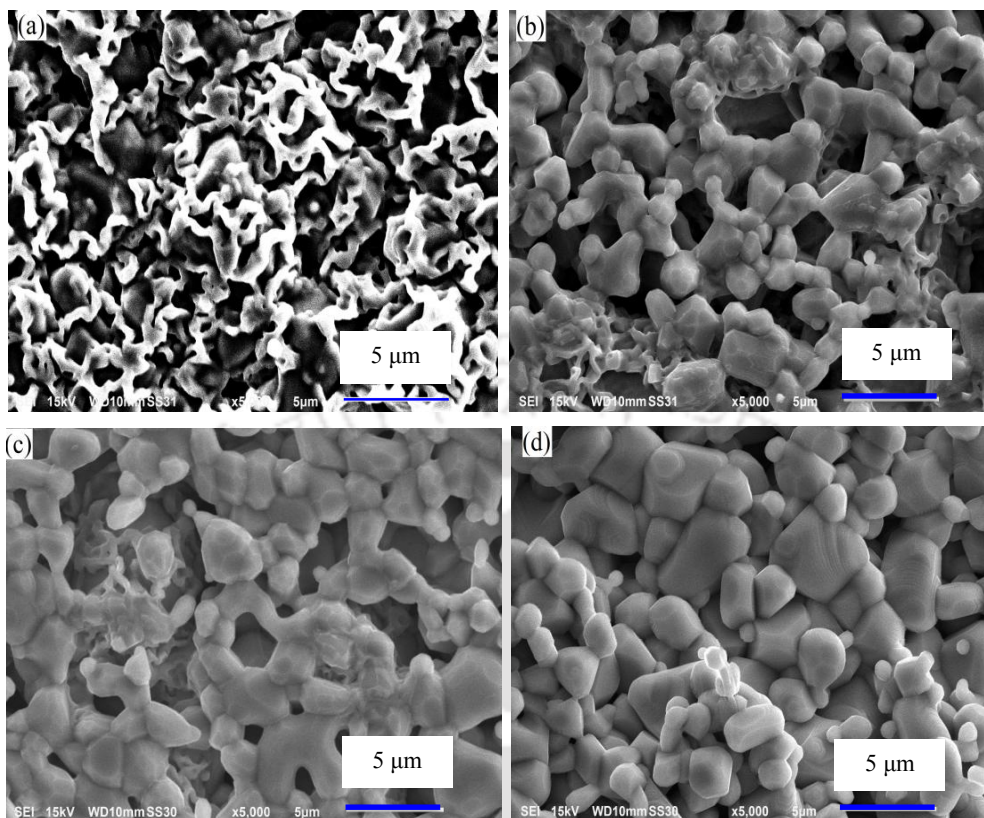


**Figure 6.3:** The composition variation of (a) bond-angles [(B-O-B) and (A-O-B)] (b) and bond-lengths [(A-O) and (B-O)].

detected from the X-ray line-broadening (with very less micro-strain  $\eta \leq 2.5 \times 10^{-3}$ ) as estimated from the Williamson-Hall analysis when the  $\text{Co}_2\text{TiO}_4$  content increases inside the parent  $\text{Co}_3\text{O}_4$  matrix. The average grain sizes lies in the micrometer range and is consistent with the values obtained from SEM-micrographs recorded under secondary electron mode.

### 6.3.2 Morphology and Microstructure Analysis:

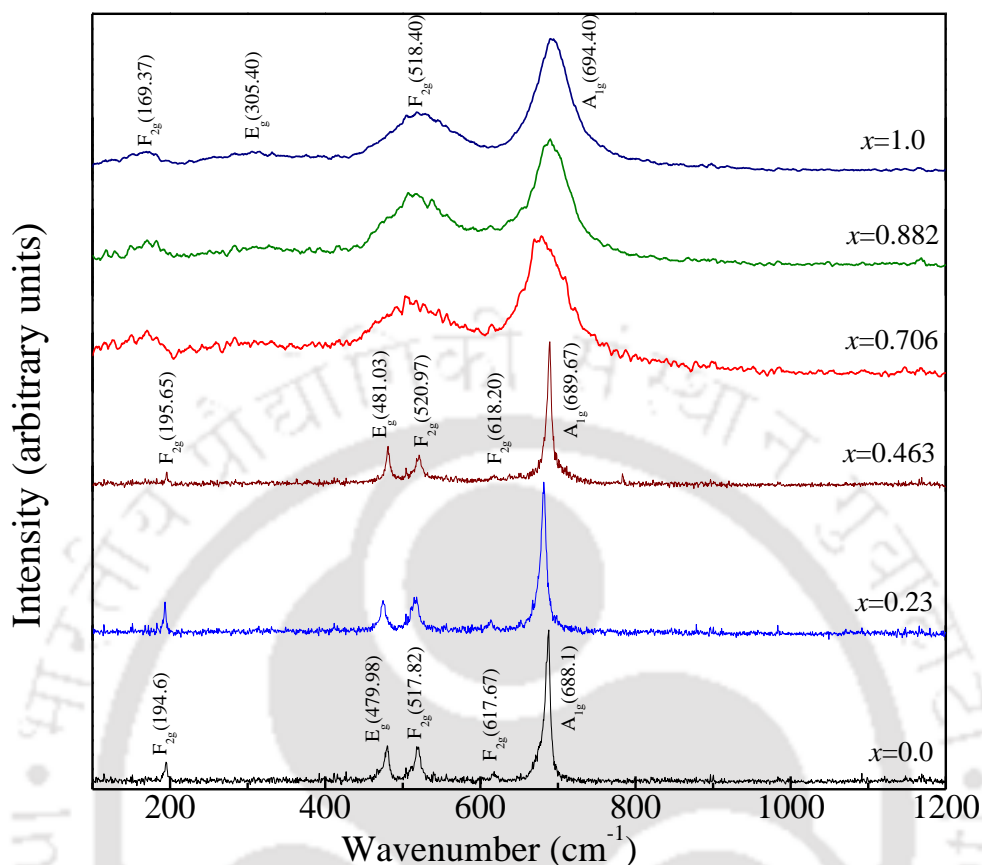
Figure 6.4a shows the SEM images of pure  $\text{Co}_3\text{O}_4$  bulk sample sintered at  $1200^\circ\text{C}$  for 8 h in air without any  $\text{Co}_2\text{TiO}_4$ . For this sample the grain sizes are lying in the range 0.8 to 0.95  $\mu\text{m}$ . Figures 6.4(b), 6.4(c) and 6.4(d) show the 0.463 (46.3 wt %), 0.706 (70.6 wt %) and 1 (100 wt %) of  $\text{Co}_2\text{TiO}_4$  grains inside the  $\text{Co}_3\text{O}_4$  matrix having the grain sizes in the range 1.5 – 1.65  $\mu\text{m}$ , 1.7 – 1.8  $\mu\text{m}$  and 2.2 – 2.35  $\mu\text{m}$ , respectively. From these figures we noticed a progressive increase of grain sizes with increase of quantity of secondary phase  $\text{Co}_2\text{TiO}_4$ .



**Figure 6.4:** Scanning electron micrographs of two-phase composites recorded under secondary-electron (SE) mode for different compositions (a)  $x = 0$ , (b)  $x = 0.463$ , (c)  $x = 0.706$ , and (d)  $x = 1$ .

### 6.3.3 Vibrational Excitations and Micro-Raman Spectroscopy:

In order to probe the phonon dynamics (vibrational excitations) of investigated oxides we have performed the Raman spectroscopy measurements both at room temperature and low-temperatures down to 25 K using liquid helium. In the literature till now there have been no Raman spectroscopic studies of either  $\text{Co}_2\text{TiO}_4$  or its solid-solutions. Figure 6.5 shows the room temperature Raman spectra of the investigated system. We observed five Raman active modes centered at 194.6, 480, 517.8, 617.7 and 688.1  $\text{cm}^{-1}$  for pure  $\text{Co}_3\text{O}_4$  (i.e. for  $x = 0$  wt %). The strongest modes appeared across 688.1  $\text{cm}^{-1}$  correspond to symmetric stretching of oxygen ( $\text{O}_2^-$ ) in tetrahedral groups ( $\text{AO}_4$ ), and according to accepted convention, can be considered as  $\text{A}_{1g}$  symmetry. The vibrational modes  $\text{E}_g \sim 480 \text{ cm}^{-1}$  corresponds to symmetric bending of oxygen with respect to cations in tetrahedral surrounding. The two vibrational  $\text{F}_{2g}$  modes,  $\text{F}_{2g}(2) \sim 517.8 \text{ cm}^{-1}$  and  $\text{F}_{2g}(3) \sim 617.7 \text{ cm}^{-1}$  are due to the asymmetric stretching and bending of the oxygen anion in the octahedral group ( $\text{BO}_6$ ). The mode at 194.6  $\text{cm}^{-1}$  ( $\text{F}_{2g}(1)$ ) is due to translational movement of the whole tetrahedron. These results are consistent with the previous findings of Hadjiev *et al.* who identified five Raman-active modes ( $\text{A}_{1g}$ ,  $\text{E}_g$  and  $3\text{F}_{2g}$ ) in the single-crystals of  $\text{Co}_3\text{O}_4$  samples measured at 312 K except slight shift of about 2  $\text{cm}^{-1}$  towards the lower wavenumber side [220].

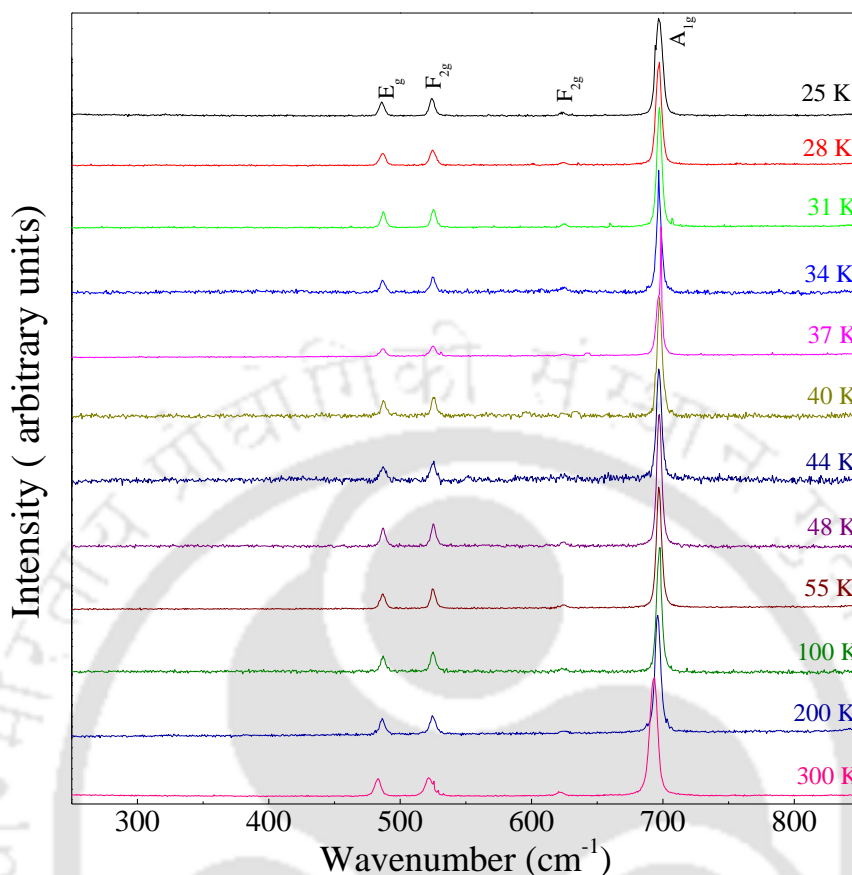


**Figure 6.5:** Room temperature Raman spectra (intensity versus wavenumber) of the two-phase composites  $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$  ( $0 \leq x \leq 1$ ). The peaks represent various vibrational modes of the spectra.

The vibrational modes of normal cubic-spinel  $\text{Co}_3\text{O}_4$  (space group  $F_{d3m}-O_h^7$ ) with fourteen atoms in the primitive unit cell can be represented as-

$$\Gamma (k = 0) = A_{1g} + E_g + 3F_{2g} + 5F_{1u} + 2A_{2u} + 2E_u + 2F_{2u} \dots (6.2)$$

Following the extensive investigations of the vibrational modes, of Rousseau *et al.* [221], the 42-dimensional representation ‘ $\Gamma$ ’ at  $k = 0$  can be reduced into 16 irreducible representations of the factor group  $O_h$  (listed above) [220 - 223]. Among the five  $F_{1u}$  modes, four are infrared active and one is acoustic mode. The remaining modes  $F_{1g}$ ,  $2A_{2u}$ ,  $2E_u$  and  $2F_{2u}$  are inactive. The  $A_{1g}$ ,  $E_g$ , and the three  $F_{2g}$  modes are Raman active. For moderate substitution of  $\text{Co}_2\text{TiO}_4$  inside the  $\text{Co}_3\text{O}_4$  matrix, the intensity of  $F_{2g}$  mode located at  $617.7 \text{ cm}^{-1}$  starts decreases and disappears altogether when the system transforms to complete inverse spinel  $\text{Co}_2\text{TiO}_4$ . Also, it is interesting to observe that the  $A_{1g}$  mode shifts by  $\sim 6.3 \text{ cm}^{-1}$  towards the higher wavenumber side with giant peak broadening for pure  $\text{Co}_2\text{TiO}_4$  sample. Also, the  $F_{2g}(3)$  and  $F_{2g}(2)$  modes are unable to distinguish in  $\text{Co}_2\text{TiO}_4$ , instead a highly broadened peak centered at  $517.82 \text{ cm}^{-1}$  was noticed. Nevertheless, a giant bathochromic red shift  $\sim 25.23 \text{ cm}^{-1}$  of  $F_{2g}$  mode is noticed in the case of  $\text{Co}_2\text{TiO}_4$ . Such shift occurs due to the substitution of ‘Ti’ ions in the octahedral



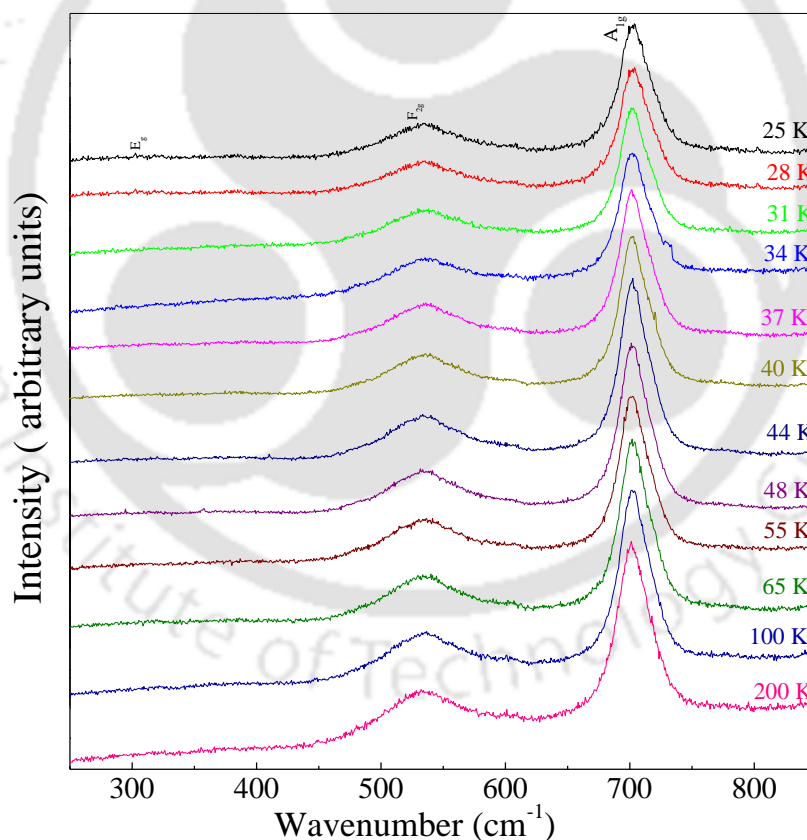
**Figure 6.6:** Raman spectra of  $\text{Co}_3\text{O}_4$  recorded at various temperatures in the range 300 K – 25 K.

sites, which enhanced the bond length between the octahedral cations and oxygen (B-O) [224]. The list of positions and the full-width-of-half-maxima (FWHM) of the Raman active phonon modes of both  $\text{Co}_3\text{O}_4$  and  $\text{Co}_2\text{TiO}_4$  together with  $x = 0.463$  samples measured at 300 K are listed in the table 6.1. The unusual behavior of the intensity and the shape of the peak can be related to the distribution of cations in the solid-solutions of the series  $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$ . The electron hopping between the  $\text{Co}^{2+}$  and  $\text{Co}^{3+}$  ions in pure  $\text{Co}_3\text{O}_4$  causes polaronic conduction at room temperature. But, when we incorporate Ti ions, it disturbs the polaronic conduction as a result peak broadening occurs. The reason for anisotropic Raman line shape may be due to random cationic distribution in the octahedral site and little amorphous nature present in the system [225, 226].

For a detailed understanding of the temperature induced changes in the vibrational modes we have performed the low-temperature Raman measurements (up to 25 K) on both the systems  $\text{Co}_3\text{O}_4$  and  $\text{Co}_2\text{TiO}_4$ . Figures 6.6 and 6.7 show the Raman spectra measured at different temperatures between 300 K and 25 K. The temperature variation of peak positions of  $A_{1g}$  and  $F_{2g}$  modes up to 25 K is separately shown in the figure 6.8. It is clear from the figure that both the phonon modes show clear anomalies across 25 K to 55 K which is associated with their change in the paramagnetic to antiferromagnetic ordering. For  $\text{Co}_3\text{O}_4$  case we observed a sharp rise in the shift of

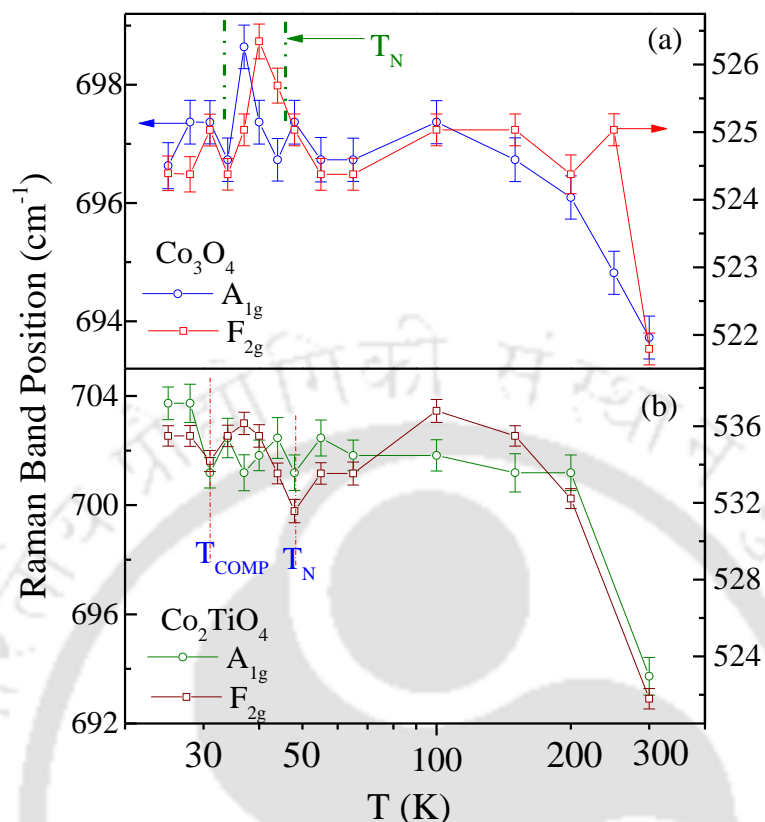
**Table 6.1:** Line positions and widths (FWHM) of the Raman-active modes of  $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$  ( $x = 0, 0.46(46.3)$  and  $1(100 \text{ wt}\%)$ ) sintered at  $1200^\circ\text{C}$  in air recorded at Room temperature.

Phonon mode	$\text{Co}_3\text{O}_4$ ( $x = 0 \text{ wt}\%$ )		$x = 0.463(46.3 \text{ wt}\%)$		$\text{Co}_2\text{TiO}_4$ ( $x = 1(100 \text{ wt}\%)$ )			
	Present data		Ref. [40]					
	Peak Position ( $\text{cm}^{-1}$ )	FWHM ( $\text{cm}^{-1}$ )	Peak Position ( $\text{cm}^{-1}$ )	FWHM ( $\text{cm}^{-1}$ )	Peak Position ( $\text{cm}^{-1}$ )	FWHM ( $\text{cm}^{-1}$ )		
$\text{F}_{2g}$	194.6	10.7	194.4	4.9	195.6	4.2	169.4	47.7
$\text{E}_g$	480	9.9	482.4	6.0	481.0	6.3	305.4	16.1
$\text{F}_{2g}$	517.8	11.0	521.6	9.5	520.9	8.4	518.4	93.3
$\text{F}_{2g}$	617.7	10.1	618.4	6.7	618.2	10.5	--	--
$\text{A}_{1g}$	688.1	10.8	691.0	6.2	689.7	7.0	694.4	51.4



**Figure 6.7:** Raman spectra of the inverted spinel  $\text{Co}_2\text{TiO}_4$  at various temperatures between 300 K and 25 K.

both phonon modes  $\text{A}_{1g}$  and  $\text{F}_{2g}$  across 40 K. Such sharp change is associated with the change in the magnetic ordering of  $\text{Co}_3\text{O}_4$  across the Néel temperature  $T_N \sim 30 \pm 10 \text{ K}$  [174]. On the other hand, the  $\text{A}_{1g}$  and  $\text{F}_{2g}$  peak of



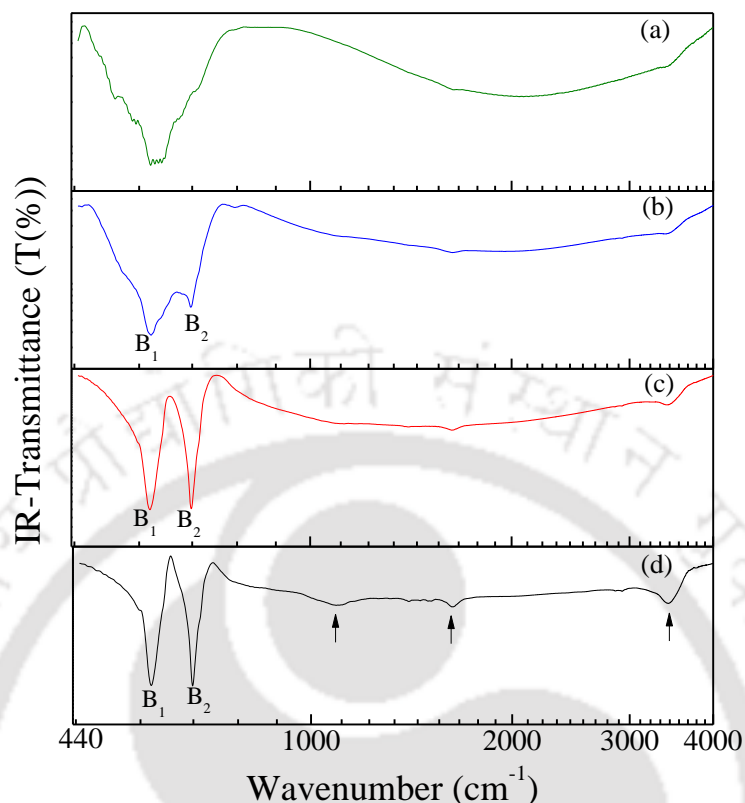
**Figure 6.8:** Temperature variation of the location of Raman active phonon modes  $A_{1g}$  and  $F_{2g}$  of (a) normal spinel  $\text{Co}_3\text{O}_4$ , and (b) inverse spinel  $\text{Co}_2\text{TiO}_4$ .

$\text{Co}_2\text{TiO}_4$  shifts to high frequency side with anomalies across 31 K and 48 K associated with the magnetic compensation temperature and ferrimagnetic Néel temperature, respectively (figure 6.8b) [77, 80].

It is well known that  $\text{Co}_2\text{TiO}_4$  exhibits clear change in the temperature dependent dc-magnetic susceptibility across 31 K and 48 K. The change across 48 K was due to the ferrimagnetic ordering which is resulting from different magnetic moments of  $\text{Co}^{2+}$  on the A-sites ( $3.87 \mu_B$ ) and B-sites ( $5.19 \mu_B$ ). On the other hand, the transition at 31 K is associated with the magnetic compensation temperature effect, where the bulk-magnetization of two-sublattices balances each other. The impact of such magnetic ordering is on the  $A_{1g}$  and  $F_{2g}$  modes are significant as seen from the anomalies noticed in figure 6.8.

#### 6.3.4. Fourier Transform Infrared (FTIR) Spectroscopy:

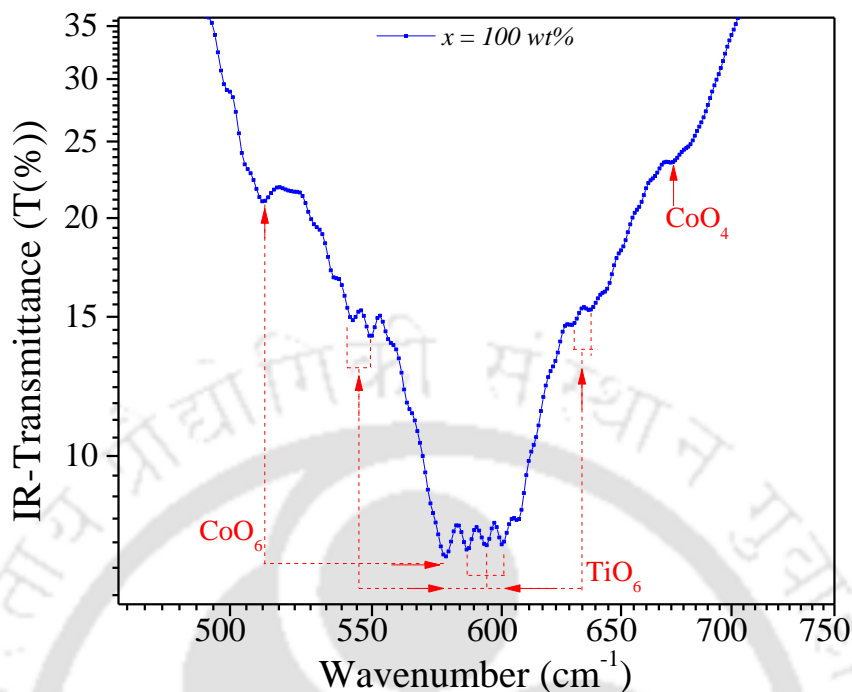
Figure 6.9 shows the FTIR spectra (Transmittance  $T$  (%) versus wavenumber ( $\text{cm}^{-1}$ )) of various compositions of the two-phase composites. All the spectra were recorded between the wavenumbers 400 and  $4000 \text{ cm}^{-1}$ . For all the samples except the higher compositions, IR spectra exhibits two distinct bands across  $576 \text{ cm}^{-1}$  and  $665 \text{ cm}^{-1}$  indicated by  $B_1$  and  $B_2$  respectively. These bands originate from the vibrational stretching of the metal-



**Figure 6.9:** Transmittance (T(%)) versus wavenumber ( $\text{cm}^{-1}$ ) of Fourier-transform infrared spectroscopy (FTIR) spectra of  $(1 - x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  two-phase composites recorded at room temperature for different compositions (a)  $x = 1$ , (b)  $x = 0.706$ , (c)  $x = 0.23$ , (d)  $x = 0$ .

oxygen bonds of length  $\sim 195.8$  pm and  $\sim 185.4$  pm. The intensity of sharp bands located at  $B_1$  and  $B_2$  gradually smeared-off as the system changes from normal to inverse spinel structure. For  $x = 0$  ( $\text{Co}_3\text{O}_4$  case) the  $B_1$  band is associated with the vibrational stretching of bonds between the cations located at octahedral sites *i.e.*  $\text{B-O-B}_3 \Rightarrow \text{Co}^{3+}\text{-O-}[\text{Co}^{3+}]_3$  of normal spinel-lattice [227- 229]. The second band  $B_2$  was attributed to the vibrational stretching of bonds between cations located at tetrahedral and octahedral sites *i.e.*  $\text{A-B-O}_3 \Rightarrow [\text{Co}^{2+}\text{-Co}^{3+}\text{-O}_3]$  [229 - 231]. For dilute compositions the IR spectrum shows similar kind of stretching vibrations as that of pure  $\text{Co}_3\text{O}_4$  with slight changes in the intensity of ‘ $B_1$ ’ and ‘ $B_2$ ’. In general, for spinel systems, the bond vibrational between the oxygen ion and highest-valence cation, exhibits highest intensity IR-absorption at higher wavenumber side (*i.e.* in the high-frequency range) regardless of the co-ordination of the cation [227, 232].

The absorption bands appeared in the mid- and higher-wavenumber regimes often exhibits complex vibrational spectrum. Nevertheless, the IR spectrum of inverse spinel compound  $\text{Co}_2\text{TiO}_4$  is completely different. Figure 6.10 shows the zoomed-view of the transitions appeared in figure 6.9(a) in the wavenumber range  $500 \text{ cm}^{-1} - 700 \text{ cm}^{-1}$ . Two more transitions are viewed across  $578 \text{ cm}^{-1}$  and  $\sim 511 \text{ cm}^{-1}$ , which are associated with the  $\text{CoO}_6$  octahedra in which cobalt possess trivalent oxidation state in the octahedral vacancy. These findings are in-line

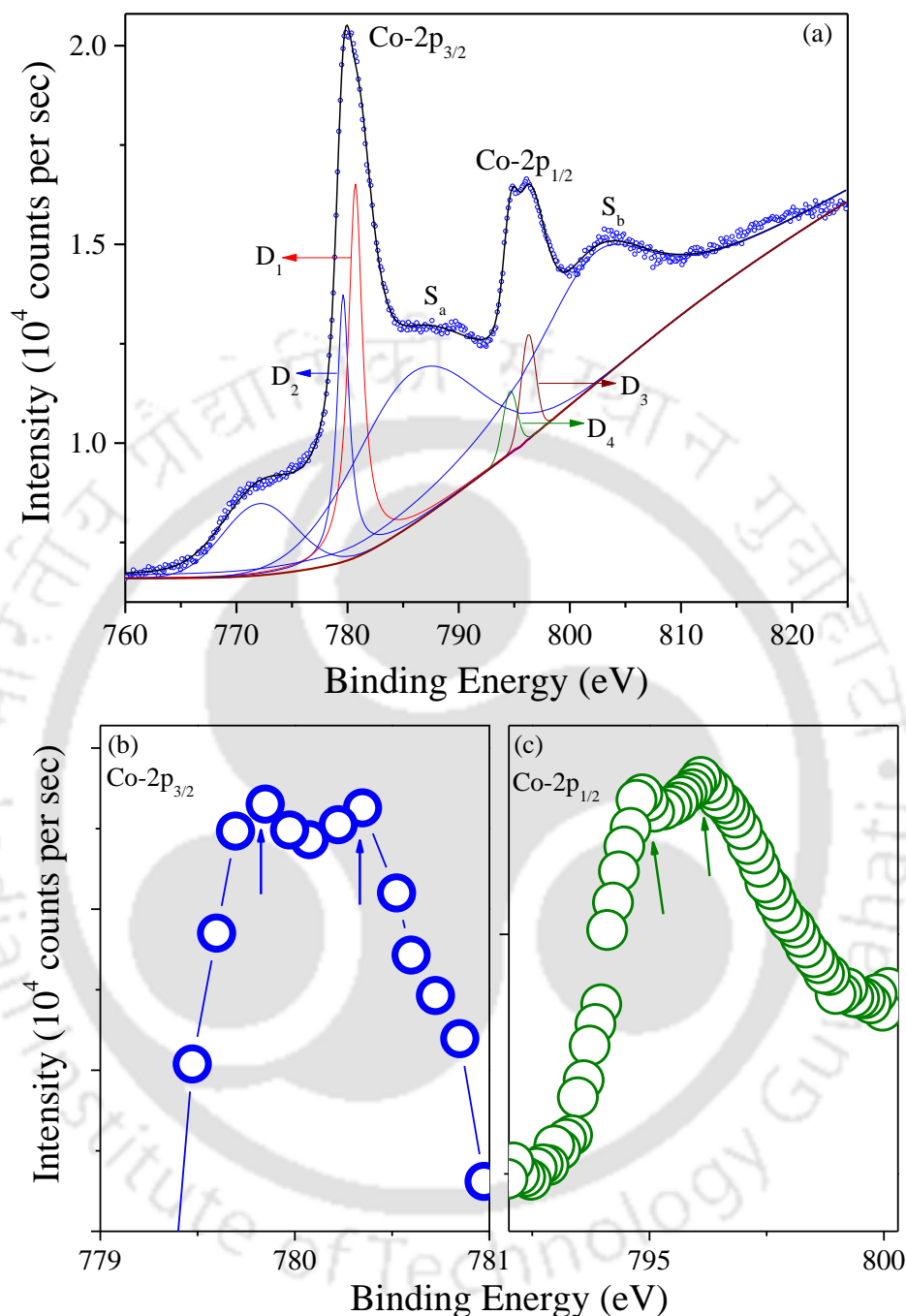


**Figure 6.10:** The enlarge view of the Fourier-transform infrared spectroscopy (FTIR) spectra of  $\text{Co}_2\text{TiO}_4$  sample between  $450$  to  $750\text{ cm}^{-1}$ .

with the previously reported data by Tang *et al.* [229]. The absorption bands noticed in the range  $550 - 650\text{ cm}^{-1}$  are associated with the vibrational stretching frequency of Ti-O bond of the condensed  $[\text{TiO}_6]$  octahedral groups, which is consistent with the earlier reports [227, 233 - 237]. The final isolated vibrational mode observed at  $673\text{ cm}^{-1}$  is the characteristic to the vibrational stretching frequency of  $\text{Co}^{2+}\text{-Co}^{3+}\text{-O}_3$ , in which  $\text{Co}^{2+}$  ions occupies the tetrahedral sites of inverse spinel lattice [229, 238]. Moreover, the absorption bands observed around  $3427\text{ cm}^{-1}$ ,  $1632\text{ cm}^{-1}$  and  $1084\text{ cm}^{-1}$  (shown by the arrow marks in figure 6.9(d) are assigned to the stretching and bending vibrations of the water molecules absorbed by the potassium bromide sample [239, 240].

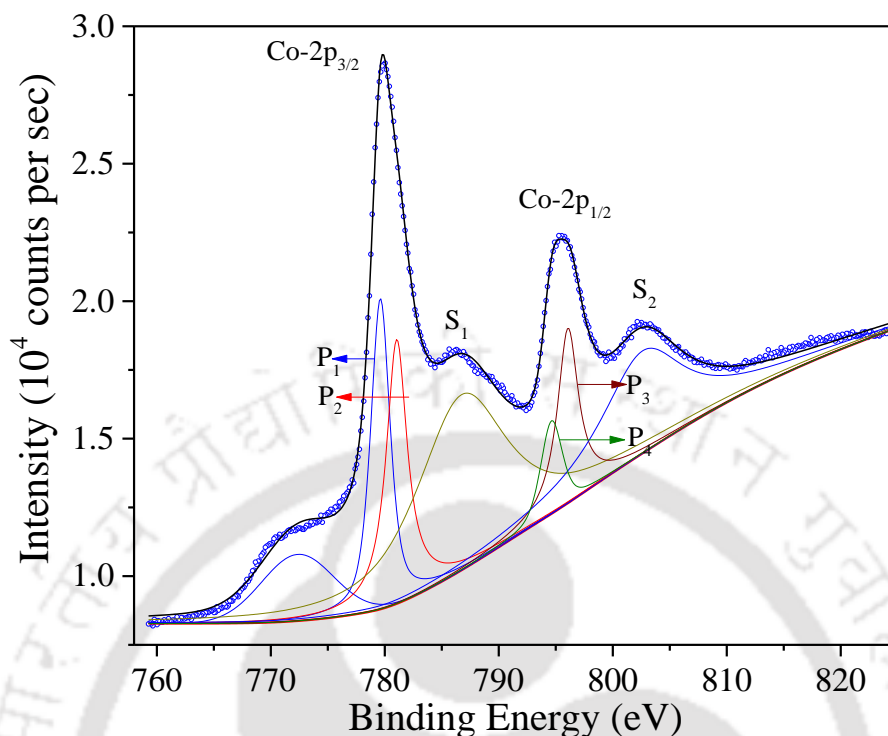
### 6.3.5 Elemental Analysis using X-ray Photoelectron Spectroscopy:

For a detailed understanding of the valance state of the cations we have performed the X-ray photoelectron spectroscopy (XPS) measurements for both the systems  $\text{Co}_3\text{O}_4$  ( $x = 0$ ) and  $\text{Co}_2\text{TiO}_4$  ( $x = 1$ ) in the form of sintered pellets. Figure 6.11 and 6.12 show the XPS spectra of Co-2*p* orbitals for  $\text{Co}_3\text{O}_4$  and  $\text{Co}_2\text{TiO}_4$  samples respectively. Both these spectra exhibits two characteristic peaks at  $780\text{ eV}$  and  $796\text{ eV}$  corresponds to Co-2*p*<sub>3/2</sub> and Co-2*p*<sub>1/2</sub>, respectively along with two satellite peaks at  $789.7\text{ eV}$  and  $803.1\text{ eV}$ . It is well known that both Co(II) and Co(III) exhibit similar binding energy peaks but the energy splitting  $\Delta E$  between the two levels is different due to different spin-orbit coupling of  $\text{Co}^{2+}$  and  $\text{Co}^{3+}$  states with  $\Delta E = 15.7\text{ eV}$  and  $15.0\text{ eV}$ , respectively [112 - 114]. Figures 6.11b and 6.11c show the zoomed view of transitions Co-2*p*<sub>3/2</sub> and Co-2*p*<sub>1/2</sub>, which clearly depicts the



**Figure 6.11:** The core-level X-ray photoelectron spectra of (a) Co-2p peak of un-doped  $\text{Co}_3\text{O}_4$  sample, (b) and (c) shows the enlarged views of Co-2p<sub>3/2</sub> and Co-2p<sub>1/2</sub> peaks, respectively.

splitting of these levels at  $D_1 = 779.8$  eV,  $D_2 = 780.3$  eV and  $D_3 = 794.8$  eV,  $D_4 = 796.1$  eV, respectively. These values are in good agreement with the previously reported data by Chuang *et al.* [158]. The energy separation obtained between the doublet peaks  $\Delta E_{D_1-D_3} = 15.1$  eV and  $\Delta E_{D_2-D_4} = 15.7$  eV are very close to the standard values



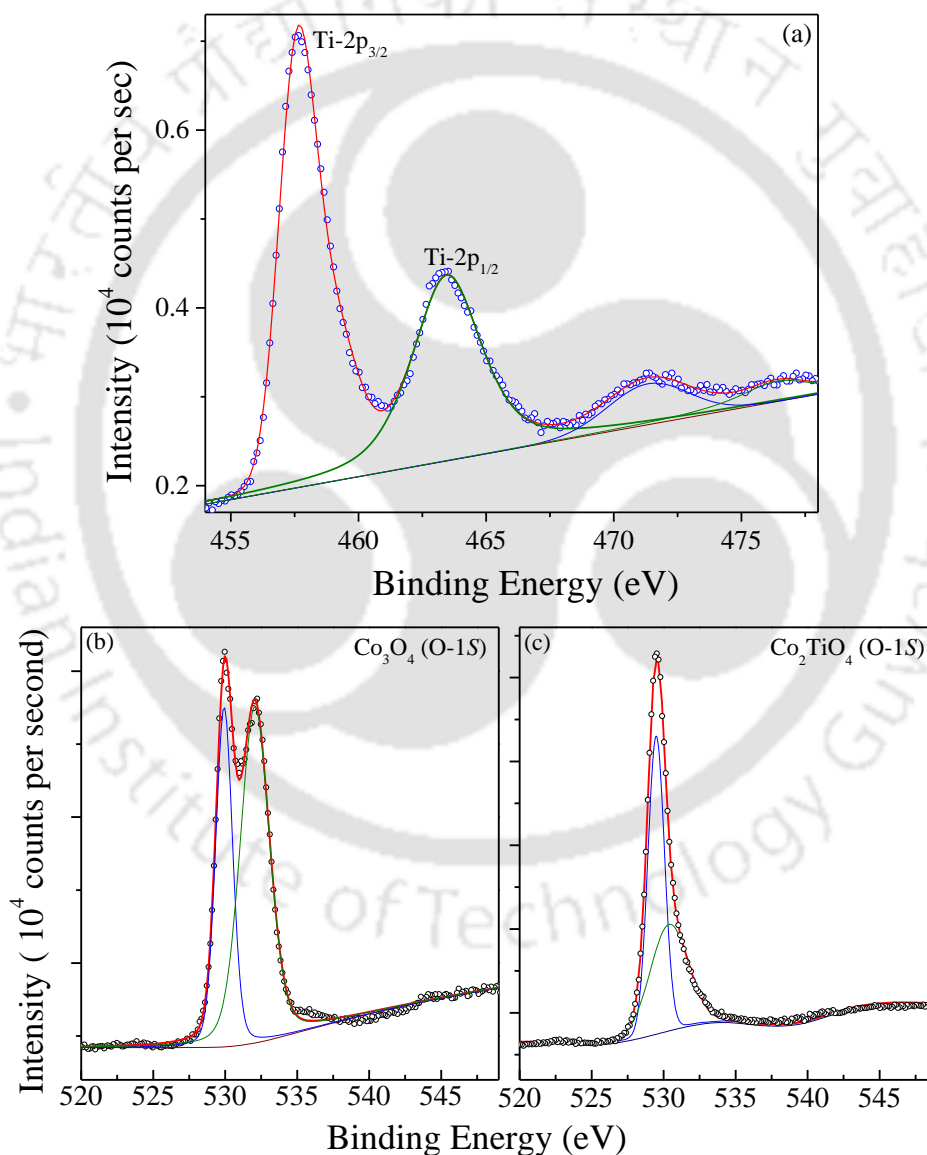
**Figure 6.12:** The core-level X-ray photoelectron spectra of Co-2*p* peak of  $\text{Co}_2\text{TiO}_4$  sample.

15 eV and 15.7 eV for the  $\text{Co}^{3+}$  and  $\text{Co}^{2+}$ , respectively in  $\text{Co}_3\text{O}_4$  bulk system, which signify the presence of trivalent and divalent cobalt cations in the  $\text{Co}_3\text{O}_4$  system. Moreover, the XPS spectra of Co-2*p*<sub>3/2</sub> and Co-2*p*<sub>1/2</sub> for  $\text{Co}_2\text{TiO}_4$  sample are slightly different (Figure 6.12). This figure consists of the raw-data as well as the Gaussian-Lorentzian fitting of Co-2*p* which depicts two different intensity doublets labeled by P<sub>1</sub> and P<sub>2</sub> for Co-2*p*<sub>3/2</sub> and P<sub>3</sub> and P<sub>4</sub> for Co-2*p*<sub>1/2</sub>. The difference between those two doublets turns out to be  $\Delta E_{P_1-P_3} = 15$  eV and  $\Delta E_{P_2-P_4} = 15.4$  eV respectively, which confirms the signature of both  $\text{Co}^{2+}$  and  $\text{Co}^{3+}$  [112 - 115]. In general, trivalent configuration of cobalt cation is not possible in the inverted spinel  $\text{Co}_2\text{TiO}_4 = [\text{Co}^{2+}(\text{Co}^{2+}\text{Ti}^{4+})\text{O}_4]$ . However, in the present case, we observed the signatures of  $\text{Co}^{3+}$  contribution at the octahedral sites of  $\text{Co}_2\text{TiO}_4$ , which may play a vital role on the magnetic properties [section 4.3.3]. This trivalent configuration also decides most of the properties including the internal d-d transitions.

In most cases, the standard binding energy of Ti-2*p*<sub>3/2</sub> state in titanium-dioxide  $\text{TiO}_2$  locates at 459.5 eV which corresponds to the ‘4<sup>+</sup>’ oxidation state of titanium ion [159]. But, the maximum intensity peak for Ti-2*p*<sub>3/2</sub> appears at 457.6 eV in  $\text{Co}_2\text{TiO}_4$  as shown in the figure 6.13a. Also, a second highest intensity peak was noticed at 463.5 eV which is associated with Ti-2*p*<sub>1/2</sub>. This result confirms the existence of ‘3<sup>+</sup>’ oxidation state of ‘Ti’ instead of ‘Ti<sup>4+</sup>’ in  $\text{Co}_2\text{TiO}_4$  [section 4.3.2]. The Ti<sup>3+</sup> peak positions are consistent with the previously reported data of Ti<sup>3+</sup> surface defects at 457.7 eV in  $\text{TiO}_2$  system [241]. These results also rule out the presence of any metallic ‘Ti’ ions

in  $\text{Co}_2\text{TiO}_4$  matrix, which usually shows their signatures in the XPS spectra  $\sim 454$  eV. The line separation between  $\text{Ti-}2p_{3/2}$  and  $\text{Ti-}2p_{1/2}$  was  $\delta E = 5.87$  eV, which is greater than the standard binding energy difference (5.7 eV) between the  $\text{Ti-}2p_{3/2}$  and  $\text{Ti-}2p_{1/2}$  states of  $\text{Ti}^{4+}$  configuration [241 - 244]. In case of Anatase  $\text{TiO}_2$  powders both the tetravalent  $\text{Ti-}2p_{3/2}$  and  $\text{Ti-}2p_{1/2}$  locates at 458.8 eV and 464.6 eV respectively, although slight decrease of these binding energies was noticed in Co-doped Anatase  $\text{TiO}_2$  powders [242].

Often the binding energy (BE) difference between the O-1s and  $\text{Ti-}2p_{3/2}$  ( $\Delta[\text{O}1s - \text{Ti}2p_{3/2}] = \text{BE}(\text{O-}1s) - \text{BE}(\text{Ti-}2p_{3/2})$ ) is used to characterize the standard valence state of the ‘Ti’ ions and also be used to avoid the contributions



**Figure 6.13:** The core-level X-ray photoelectron spectra of (a)  $\text{Ti-}2p$  peak of  $\text{Co}_2\text{TiO}_4$  sample, (b) and (c) are O-1s peak of  $\text{Co}_3\text{O}_4$  and  $\text{Co}_2\text{TiO}_4$  respectively.

**Table-6.2:** Atomic quantification of the normal-spinel  $\text{Co}_3\text{O}_4$  and the inverse-spinel  $\text{Co}_2\text{TiO}_4$  using the XPS data.

System	Atoms	I/F	Atomic concentration (%)		Theoretically calculated atomic concentration (%)
$\text{Co}_2\text{TiO}_4$	O-1s	49671.21	59.48		57.14
	Ti-2p	9739.47	11.66		14.28
	Co-2p	24092.20	28.85	$\text{Co}^{3+} = 9.37$ $\text{Co}^{2+} = 19.48$	28.57
$\text{Co}_3\text{O}_4$	O-1s	27688.39	64.58		57.14
	Co-2p	15180.20	35.41	$\text{Co}^{3+} = 21.99$ $\text{Co}^{2+} = 13.41$	42.85

from different energy scale calibration and charging effects [244]. The transfer of valance electrons from ‘Ti’ to ‘O’ plays a vital role in deciding the Ti-O chemical bond formation which in-turn cause in the shift of binding energy positions of Ti-  $2p_{3/2}$  to higher level and O-1s to lower level. To avoid such sensitive discrepancies it is often convenient and advantageous to use the binding energy difference criterion  $\Delta[\text{O}1s\text{-Ti}2p_{3/2}]$  for characterizing the exact electronic state of the ‘Ti’ cations. In the present case, the characterizing parameter  $\Delta[\text{O}1s\text{-Ti}2p_{3/2}]$  turnout to be 71.8 eV for trivalent state, which was slightly higher as compared to the 71.4 eV for tetravalence ‘Ti’ ions [245- 247]. For  $\text{Ti}^{2+}$  case the BE difference  $\Delta[\text{O}1s\text{-Ti}2p_{3/2}]$  is quite high  $\sim 75\text{-}76.7$  eV [248, 249]. It has been reported that relatively higher BE difference (72.9 - 73.4 eV) of  $\text{Ti}^{3+}$  containing compounds such as  $\text{Ti}_2\text{O}_3$ ,  $\text{Sn}_{0.5}\text{NbTiP}_3\text{O}_{12}$  and  $\text{Fe}_{0.33}\text{NbTiP}_3\text{O}_{12}$  [248, 250, 251].

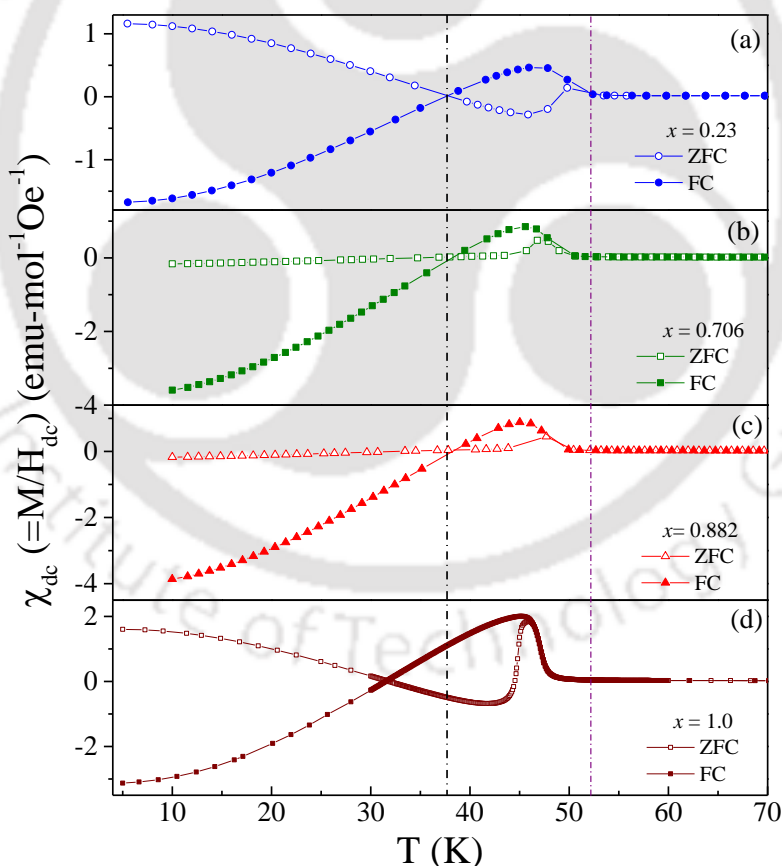
The XPS peak of O-1s spectra deconvoluted into two different Gaussian sub-peaks centered at 529.9 eV and 532.2 eV, reflecting two different oxygen environment existing in the  $\text{Co}_3\text{O}_4$  system (shown in figure 6.13b) [126, 248, 249, 252, 253]. The peak centered at 529.9 eV arises from the oxygen atoms bonded with nearest neighbor metal ions in the lattice. The peak located at 532.2 eV is attributed to the oxygen atoms in the vicinity of an oxygen vacancy and also the surface oxygen presence in the system [254]. On the other hand, for the case of  $\text{Co}_2\text{TiO}_4$  the O-1s peak appears at  $\sim 529.52$  eV (Figure 6.13c) with some weak signature of surface oxygen (530.5 eV), in  $\text{Co}_2\text{TiO}_4$  bulk system [248, 249, 253]. Since the difference of the electronegativity’s of ‘Ti’ (1.54) and ‘O’ (3.44) is higher than the difference between the ‘Co’ (1.88) and ‘O’, titanium tends to combine more strongly with oxygen anion. Thus ‘Ti’ dopant behaves as an oxygen vacancy suppressor, which also reduces the amount of surface oxygen in cobalt-orthotitanate [255, 256].

The XPS data are also fitted using a relative area ratio of 1:2 for the  $2p$  component peaks keeping the constant FWHM of all core level peaks. Generally, the atomic percentage in A-B-O type system was evaluated using the

correlation between the atomic concentration, photoelectron intensity ‘I’ and atomic sensitivity factor ‘F’, using the following equation [257].

$$\text{Atomic \% of } A = \frac{\frac{I_A}{F_A}}{\frac{I_A}{F_A} + \frac{I_B}{F_B} + \frac{I_C}{F_C}} \times 100 \dots (6.3)$$

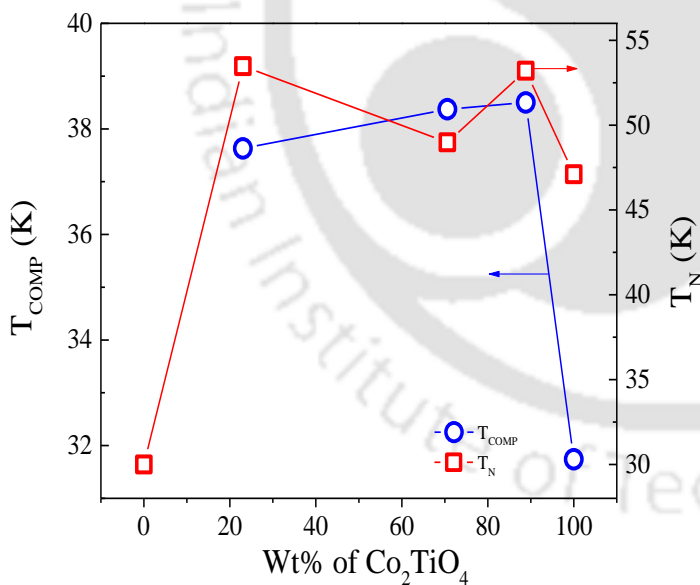
The magnitude of the atomic sensitivity factor ‘F’ can be obtained from the relation  $F = \sigma \xi T \lambda$ , where ‘ $\sigma$ ’ is the ionization constant, ‘ $\xi$ ’ is the spectrometer angular acceptance, ‘T’ is the spectrometer transmittance and ‘ $\lambda$ ’ is the inelastic mean free path [257]. The experimentally obtained values of atomic % together with the theoretically obtained values are compared in the Table 6.2 in which the theoretical results are consistent with the experimental data. We also determined the content of  $\text{Co}^{2+}$  and  $\text{Co}^{3+}$  present for both the cases  $x = 0$  and 1 (Table-6.2). For  $x = 1$ , the ratio of  $\text{Co}^{3+}$  and  $\text{Co}^{2+}$  turns out to be 1 : 2 but the content of  $\text{Co}^{3+}$  present in  $\text{Co}_2\text{TiO}_4$  is almost matches with that of  $\text{Ti}^{3+}$  ( $\text{Co}^{3+} : \text{Ti}^{3+} = 1:1.1$ ).



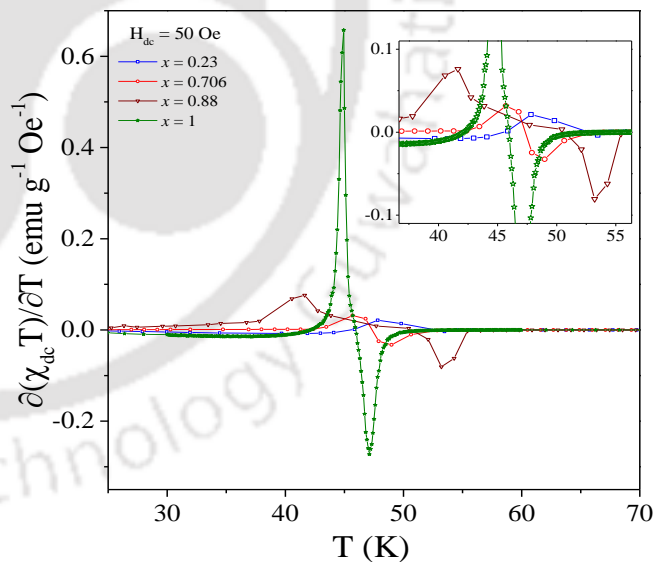
**Figure 6.14:** Temperature dependence of dc-magnetic susceptibility  $\chi_{dc}(T) = M/H_{dc}(T)$  for (a)  $x = 0.23$ , (b)  $x = 0.706$  (c)  $x = 0.882$  (d)  $x = 1.0$  measured under both zero-field-cooled (ZFC) and field-cooled (FC) conditions recorded at magnetic field  $H_{dc} = 50$  Oe.

### 6.3.6 Tailoring the Compensation Point ( $T_{\text{COMP}}$ ) and Néel Temperature ( $T_{\text{N}}$ ):

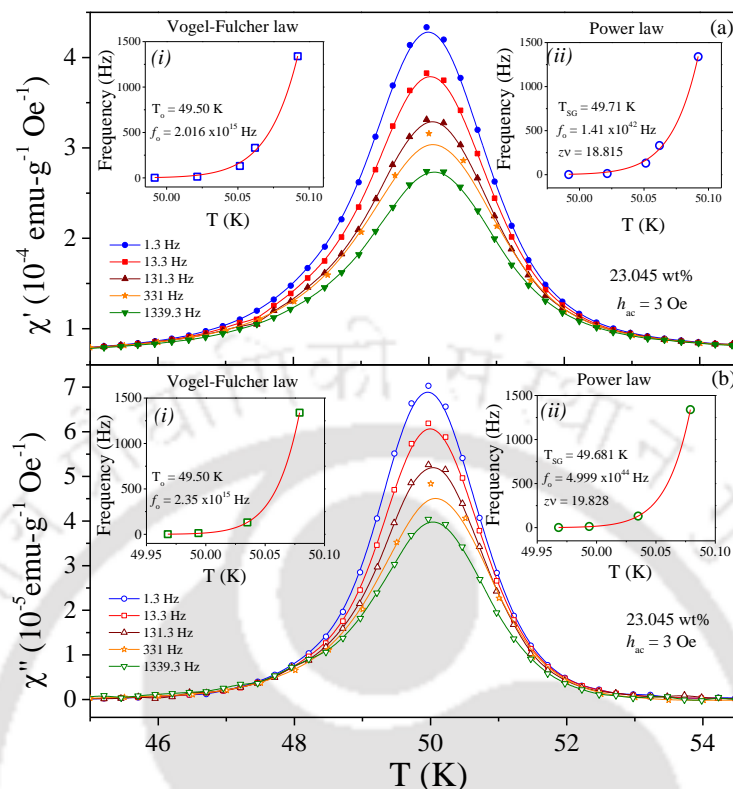
Figure 6.14 depicts the temperature dependence dc-magnetic susceptibility  $\chi_{\text{dc}}$  ( $=M/H_{\text{dc}}$ ) for various compositions of  $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$  ( $0.23 \leq x \leq 1$ ) recorded under both zero-field-cooled (ZFC) and field-cooled (FC,  $H @ 50$  Oe) conditions. For all the compositions both the curves  $\chi_{\text{ZFC}}(T)$  and  $\chi_{\text{FC}}(T)$  exhibits a characteristic peak  $T_{\text{P}}$  ( $\sim 49$  K(ZFC) and  $\sim 46$  K(FC) for  $x = 0$ ) corresponding to the ferrimagnetic Néel temperature  $T_{\text{N}}$ ; while a slight variation in the peak position was noticed with increasing the  $\text{Co}_2\text{TiO}_4$  content. Below the characteristic peak, both the  $\chi_{\text{ZFC}}(T)$  and  $\chi_{\text{FC}}(T)$  curves exhibits magnetic-compensation ( $T_{\text{COMP}}$ ) effect, where,  $\chi(T)$  approaches to zero due to the complete balance of two sublattices magnetizations. Needless to say that the magnetic behavior of the two phase composites is dominated by negative magnetization character of  $\text{Co}_2\text{TiO}_4$  (as discussed in chapter 4 section 4.3.3). Figure 6.15 shows the variation of the  $T_{\text{N}}$  (obtained from  $\partial(\chi_{\text{dc}}T)/\partial T$  plots shown in figure 6.16) and  $T_{\text{COMP}}$  as a function of  $\text{Co}_2\text{TiO}_4$  wt% (i.e.,  $x$ ). One can clearly see from the figure that  $T_{\text{N}}$  attains a maximum value  $\sim 53.3$  K for  $x = 0.882$  (88.2 wt%) whereas  $T_{\text{COMP}}$  decreases from  $\sim 38$  K to  $\sim 32$  K as the system transform to complete inverse spinel structure. These results are consistent with the magnetization data of  $\text{Co}_2\text{TiO}_4$  reported by Hubsch *et al.* [77]. In order to probe the glassy behavior, in these composites we have further investigated the temperature variation of the dynamic magnetic susceptibility.



**Figure 6.15:** The compositional variation of compensation temperature ( $T_{\text{COMP}}$ ) and ferrimagnetic Néel temperature ( $T_{\text{N}}$ ).



**Figure 6.16:** The plots of  $\partial(\chi_{\text{dc}}T)/\partial T$  versus  $T$  of  $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$  ( $x = 0.23, 0.706, 0.882$  and  $1.0$ ) sample at external fields  $H_{\text{dc}} = 50$  Oe. The inset shows the zoomed view of peak variation of various composites.

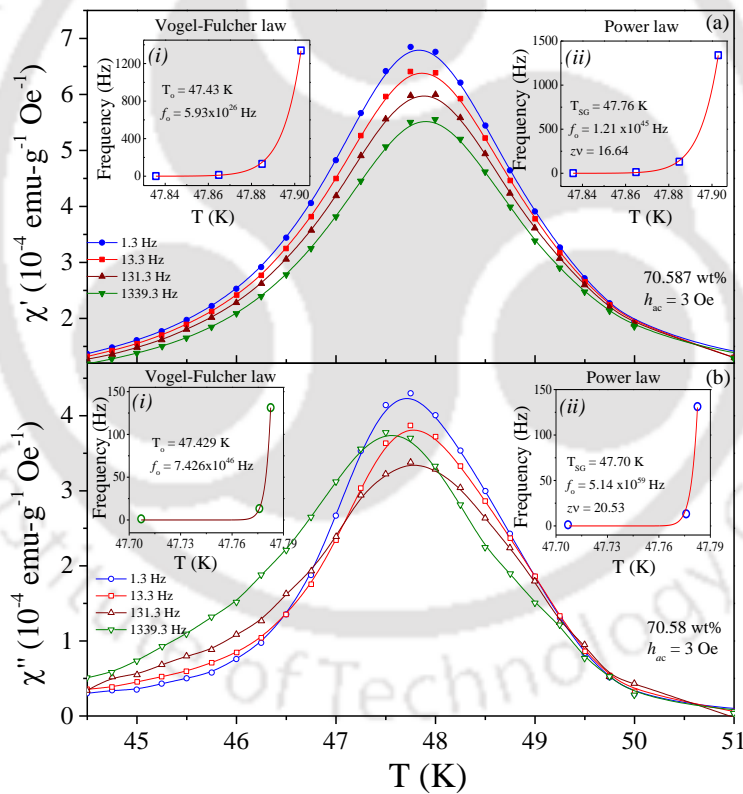


**Figure 6.17:** Temperature dependence of the ac-magnetic susceptibility of the composite system  $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$  for  $x = 0.23$  with (a) the real component  $\chi'(T)$ , and (b) the imaginary component  $\chi''(T)$  recorded at various frequencies ( $1.3 \text{ Hz} \leq f \leq 1339.3 \text{ Hz}$ ) under warming condition using  $h_{ac} = 3 \text{ Oe}$  and zero static magnetic field. The scattered symbols shown in the inset (i) of figure (a), and inset (i) of figure (b) represents the frequency dependence of peak position whereas the solid line shows the Vogel-Fulcher law fit of experimental data. The inset (ii) of figure (a) and inset (ii) of figure (b) shows the frequency dependence of peak positions in  $\chi'(T)$  and  $\chi''(T)$ , respectively. The solid line shows the theoretical fit to the experimental data.

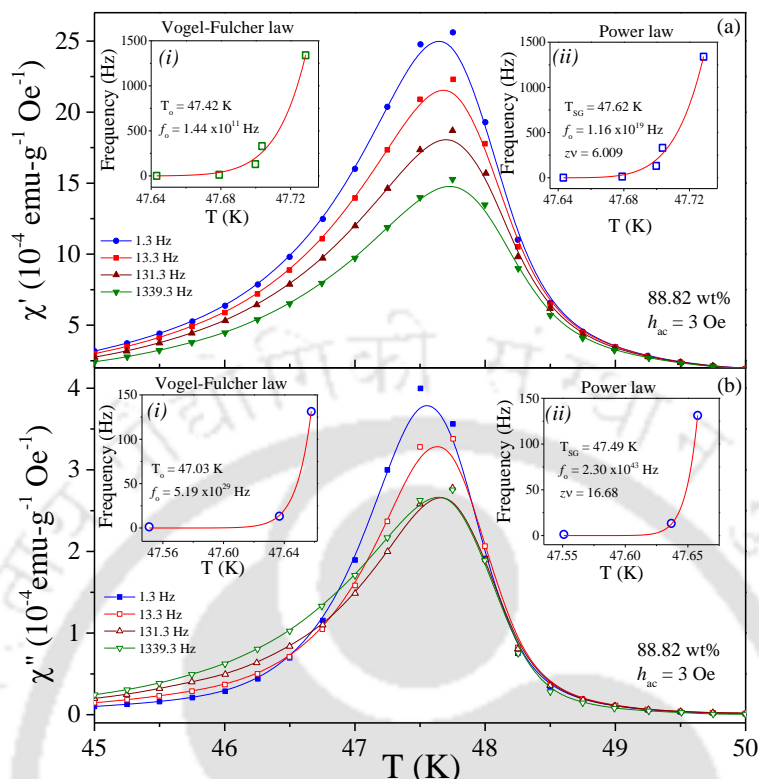
Figures 6.17 - 6.19 show the temperature dependence of in-phase (real component  $\chi'(T)$ ) and out-of-phase (imaginary component  $\chi''(T)$ ) of the ac-magnetic susceptibilities  $\chi_{ac}(T)$  for three different compositions ( $x = 0.23, 0.706$  and  $0.882$ ) measured at various frequencies ( $f$ ) between the temperatures 45 K and 55 K. For all the frequencies, a broad cusp was noticed with very feeble shift of the peak position towards higher temperature side with increasing ' $f$ ' from 1.3 Hz to 1339.3 Hz. Nevertheless, the peak shift in  $\chi'(T)$  and  $\chi''(T)$  does not follow neither Vogel-Fulcher law nor Power law of critical slowing down for interacting particle system (insets of these figures). The parameters obtained from the fitting analysis are listed in table 6.3. The large values of ' $f_0$ ' indicates the absence of spin-glass phase transition below  $T_N$  [67]. It is interesting to note that the M-H loops (Figure 6.20) measured under field cooled (@ 20 kOe) mode for all the three compositions at 10 K exhibits large coercivity ( $H_C$ ) and exchange-bias ( $H_{EB}$ ). Figures 6.21(a) shows the magnitude of  $H_C$  and  $H_{EB}$  plotted as a function of ' $x$ '. One can clearly observe from the figure that  $H_C^{\text{Max}} \sim 19 \text{ kOe}$  at 10 K for  $x = 1$ , whereas,  $H_{EB}(x)$  shows a maximum 887 Oe at  $x = 0.23$  due to the dominant role of  $\text{Co}_2\text{TiO}_4$  over  $\text{Co}_3\text{O}_4$ , and these results were consistent with the composition

**Table-6.3:** The fitting parameters obtained from Vogel-Fulcher law and Power law of  $(1-x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  ( $x = 0, 0.706(70.6)$  and  $0.882(88.2 \text{ wt}\%)$  sintered at  $1200^\circ\text{C}$ .

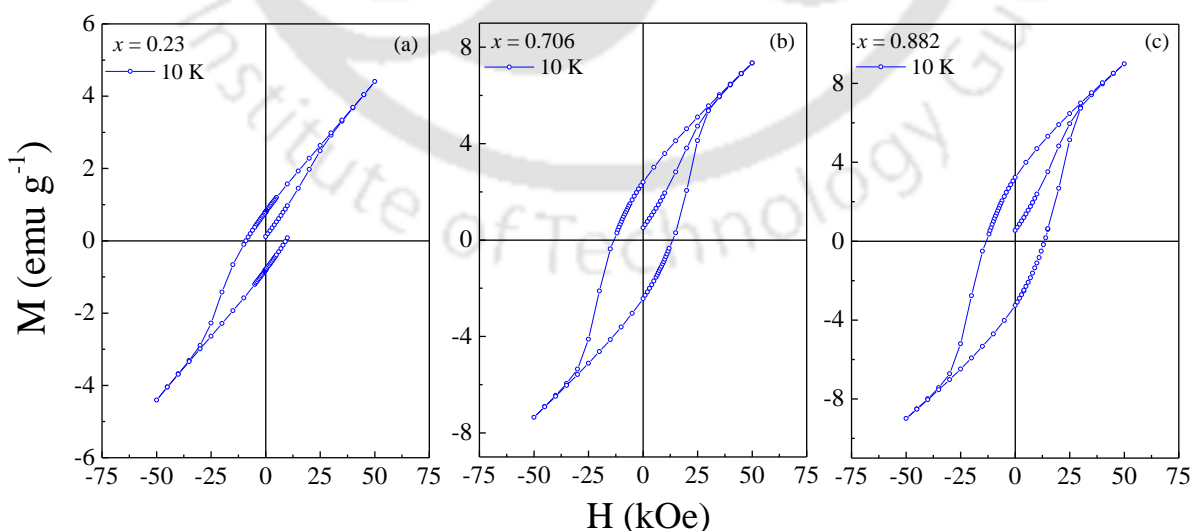
$x$		Vogel-Fulcher law		Power-Law		
		$f_o$ (Hz)	$T_o$ (K)	$f_o$ (Hz)	$T_{SG}$ (K)	$z\nu$
0.23	From $\chi'$	$2.01 \times 10^{15}$	49.5	$1.41 \times 10^{42}$	49.71	18.81
	From $\chi''$	$2.35 \times 10^{15}$	49.5	$4.99 \times 10^{44}$	49.68	19.82
0.706	From $\chi'$	$5.93 \times 10^{26}$	47.43	$1.21 \times 10^{45}$	47.76	16.64
	From $\chi''$	$7.43 \times 10^{46}$	47.43	$5.14 \times 10^{59}$	47.70	20.53
0.882	From $\chi'$	$1.44 \times 10^{11}$	47.42	$1.16 \times 10^{19}$	47.62	6.009
	From $\chi''$	$5.19 \times 10^{29}$	47.03	$2.30 \times 10^{42}$	47.49	16.68



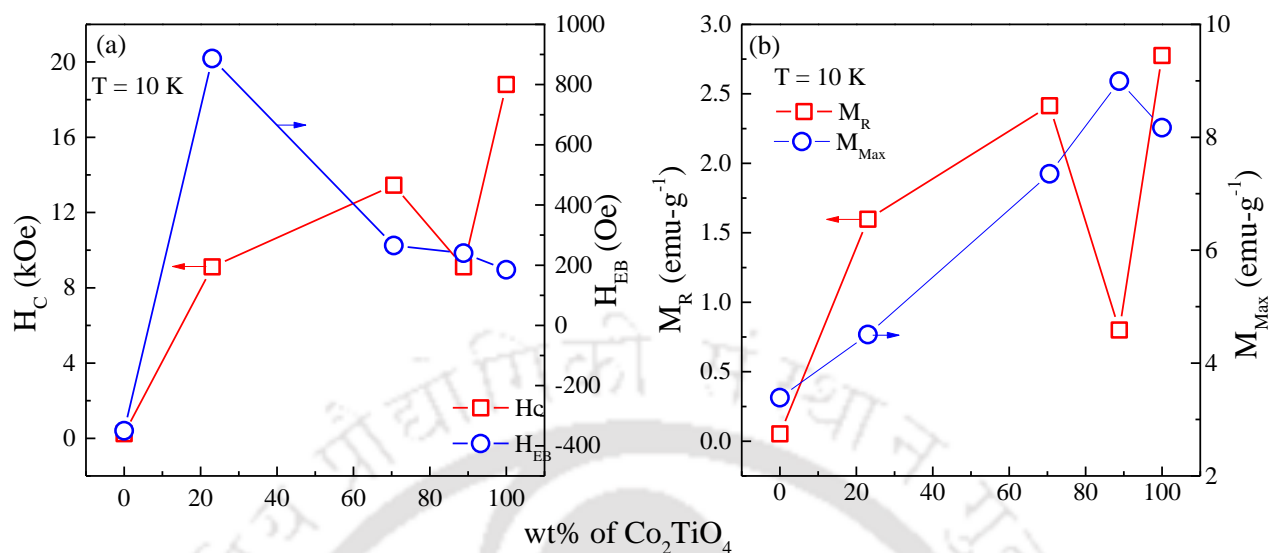
**Figure 6.18:** Temperature dependence of the ac-magnetic susceptibility of the composite system  $(1-x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  for  $x = 0.706$  with (a) the real component  $\chi'(T)$ , and (b) the imaginary component  $\chi''(T)$  recorded at various frequencies ( $1.3 \text{ Hz} \leq f \leq 1339.3 \text{ Hz}$ ) under warming condition using  $h_{ac} = 3 \text{ Oe}$  and zero static magnetic field. The scattered symbols shown in the inset (i) of figure (a), and inset (i) of figure (b) represents the frequency dependence of peak position whereas the solid line shows the Vogel-Fulcher law fit of experimental data. The inset (ii) of figure (a) and inset (ii) of figure (b) shows the frequency dependence of peak positions in  $\chi'(T)$  and  $\chi''(T)$ , respectively. The solid line shows the theoretical fit to the experimental data.



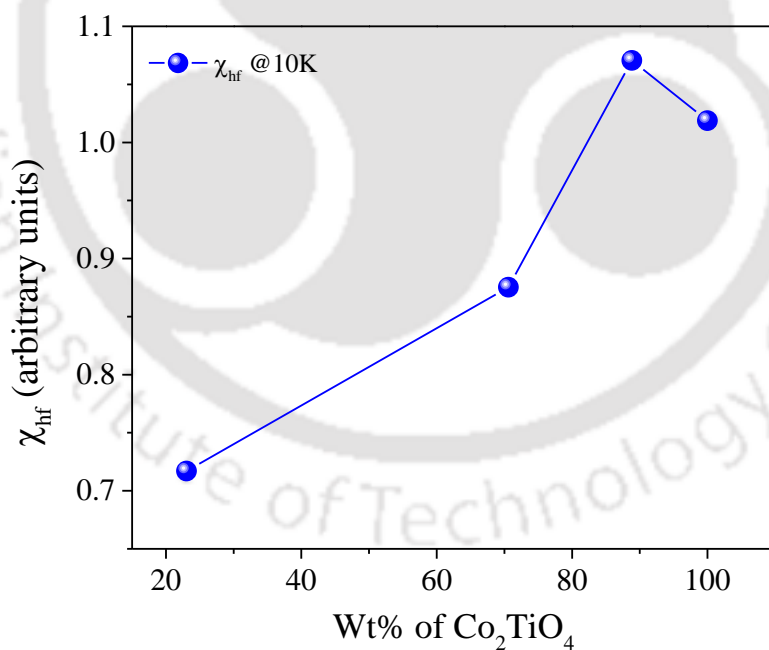
**Figure 6.19:** Temperature dependence of the ac-magnetic susceptibility of the composite system  $(1 - x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  for  $x = 0.882$  with (a) the real component  $\chi'(T)$ , and (b) the imaginary component  $\chi''(T)$  recorded at various frequencies ( $1.3 \text{ Hz} \leq f \leq 1339.3 \text{ Hz}$ ) under warming condition using  $h_{ac} = 3 \text{ Oe}$  and zero static magnetic field. The scattered symbols shown in the inset (i) of figure (a), and inset (i) of figure (b) represents the frequency dependence of peak position whereas the solid line shows the Vogel-Fulcher law fit of experimental data. The inset (ii) of figure (a) and inset (ii) of figure (b) shows the frequency dependence of peak positions in  $\chi'(T)$  and  $\chi''(T)$ , respectively. The solid line shows the theoretical fit to the experimental data.



**Figure 6.20:** Magnetization versus field ( $M$  vs.  $H$ ) hysteresis loops recorded under field-cooled (FC) conditions at constant temperature  $T = 10 \text{ K}$  for  $(1 - x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  (a)  $x = 0.23$  (b)  $x = 0.706$  (c)  $x = 0.882$ .



**Figure 6.21:** (a) The composition variation of the coercive field  $H_c(x)$  [LHS] and exchange bias  $H_{EB}(x)$  [RHS] estimated from the M-H curves measured at 10 K under 20 kOe field cooled (FC) condition (b) The composition variation of the remanence magnetization  $M_R(x)$  [LHS] and maximum magnetic moment @ 50 kOe ( $M_{MAX}(x)$ ) [RHS] obtained from the M-H curves measured at 10 K under 20 kOe field cooled (FC) condition.



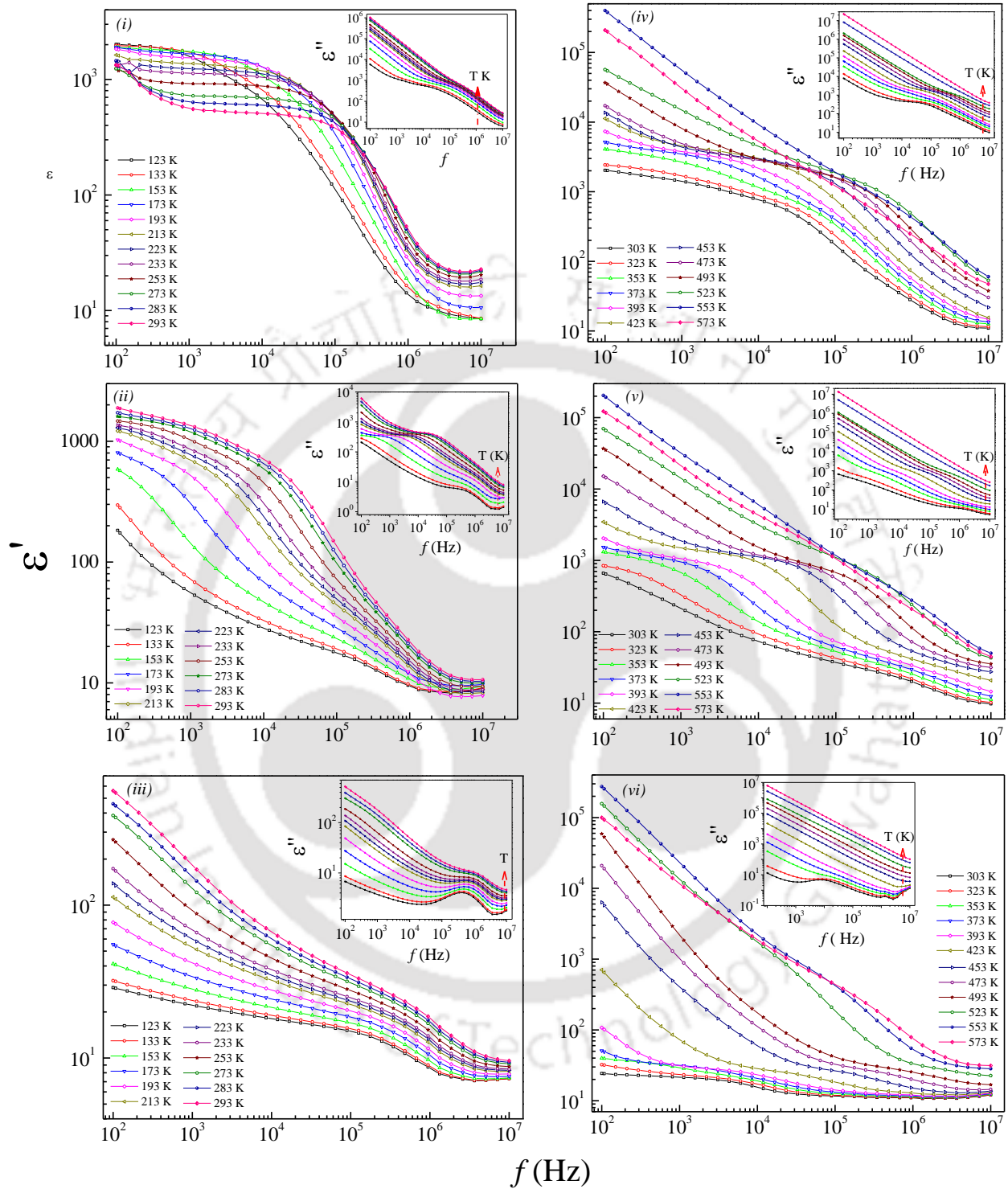
**Figure 6.22:** Composition variation of high field susceptibility  $\chi_{hf}(x)$  calculated from the 50 kOe M-H loops measured at 10 K under field-cooled (FC) condition.

variation of remanence magnetization  $M_R(x)$ , maximum magnetization at 50 kOe  $M_{MAX}(x)$ , and high field ac-magnetic susceptibility  $\chi_{hf}(x)$  (Figure 6.21(b) and 6.22).

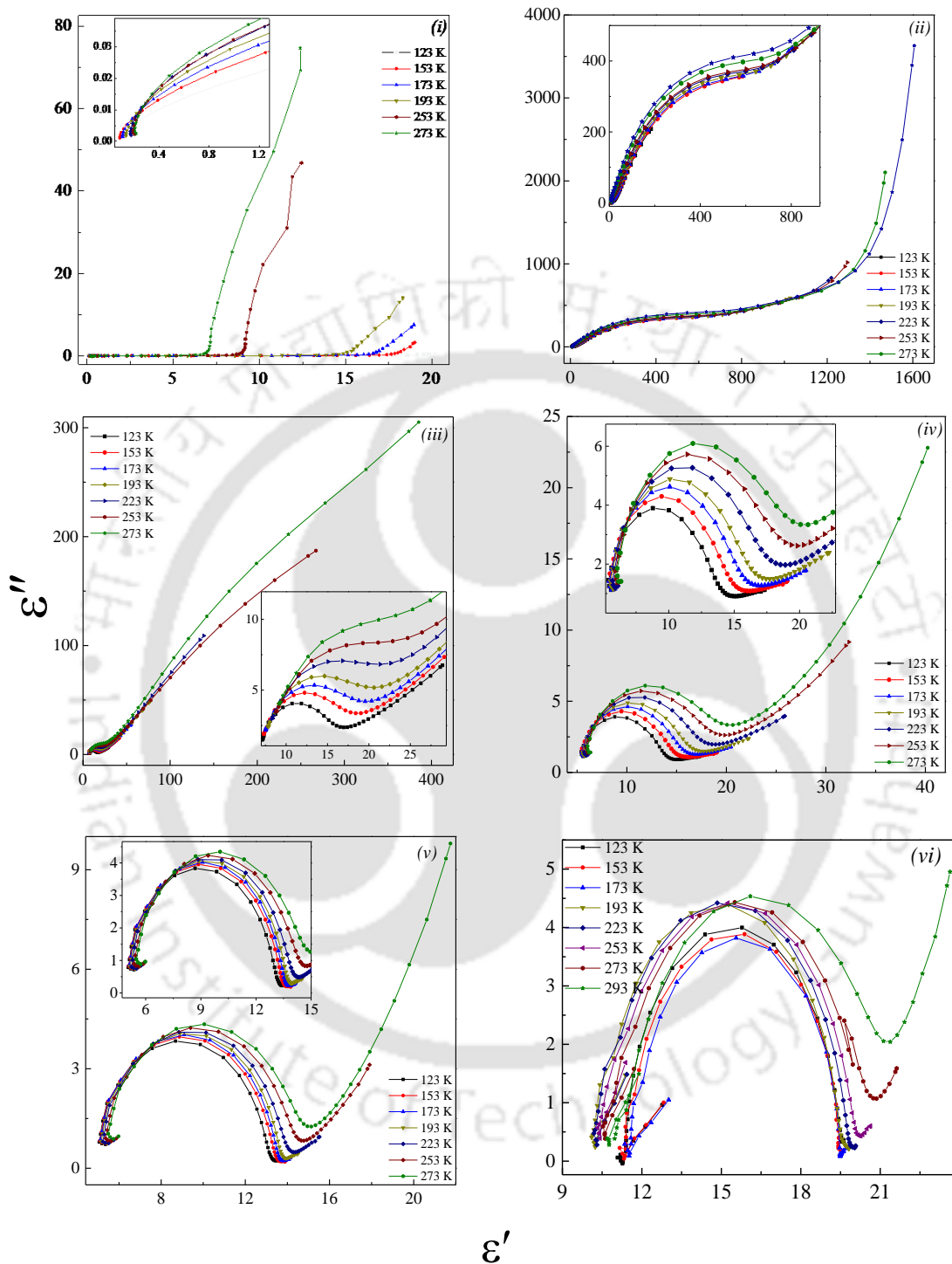
### **6.3.7 Dielectric Permittivity and AC-Conductivity:**

Figures 6.23 show the frequency variation of real component of dielectric permittivity ( $\epsilon'(f)$ ) for  $x = 0.23, 0.46$  and  $1.0$  (insets show imaginary component ( $\epsilon''(f)$ ). These measurements are performed systematically below the room temperature ( $125 \text{ K} \leq T \leq 290 \text{ K}$ ) and above room temperature ( $303 \text{ K} \leq T \leq 573 \text{ K}$ ). From the figure we observed that the value of dielectric constant decreases as we increase frequency due to effect of interfacial and dipolar polarization at low frequency. The decrease of dielectric constant with increase of frequency is quite common in any insulating spinel system. Lazarevic *et al.* observed similar kind of frequency variation in  $\epsilon'(f)$  for the case of nickel ferrites in which a robust interaction is expected among the free charge carriers (either electrons or holes) with potential barrier at grain boundaries [258]. Such process may result to enhancement of conductivity across the grain boundaries which will be discussed later [258, 259]. Moreover, decrease in the value of  $\epsilon'$  with increasing frequencies is more prominent at high temperature as compared to lower temperature. We observe anomalous change in  $\epsilon'(f)$  between the frequencies  $10^4$  and  $10^5$  Hz due the electronic and ionic polarization. From the figures we also noticed that, as the temperature rises,  $\epsilon'$  slowly increases with increase in temperature for whole frequency range. The sharp rise in both  $\epsilon'$  and  $\epsilon''$  at low frequencies can be attributed to LC-resonance like features arising from the electrode and sample [260, 261]. Figures 6.24 and 6.25 represents the Cole-Cole plots (Nyquist plot  $\epsilon''$  versus  $\epsilon'$ ) of  $(1-x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  ( $0 \leq x \leq 1$ ) for high temperature and low-temperature regimes. For dilute compositions  $x < 0.3$ , Nyquist plot does not takes semi-circular shape, rather it present straight line with large slope suggesting the domination of grain boundary effect [262]. As  $x$  increases, depressed semi-circular behavior of the Cole-Cole plots was noticed (figures 6.24 (iii) and (iv)). Such depressed semi-circle behavior signifies the contribution of grain interior (bulk) as well as grain boundary contribution. For higher  $x$  values ( $> 0.8$ ), perfect semi-circle arcs are observed (figures 6.24 (v) and (vi)). Such type of Cole-Cole plots suggest a single relaxation process dominates over the conduction mechanism, which can be identified as grain-effect. Small grain boundary effect was also noticed from these plots, as, they exhibited a straight line behavior after the termination of the semi-circle. Therefore, from the Cole-Cole analysis we conclude that, for lower ' $x$ ' values, the conduction mechanism is dominated by the grain-boundary effect, whereas with increasing ' $x$ ' the grain effect starts dominating and the plots are perfect semi-circular in shape.

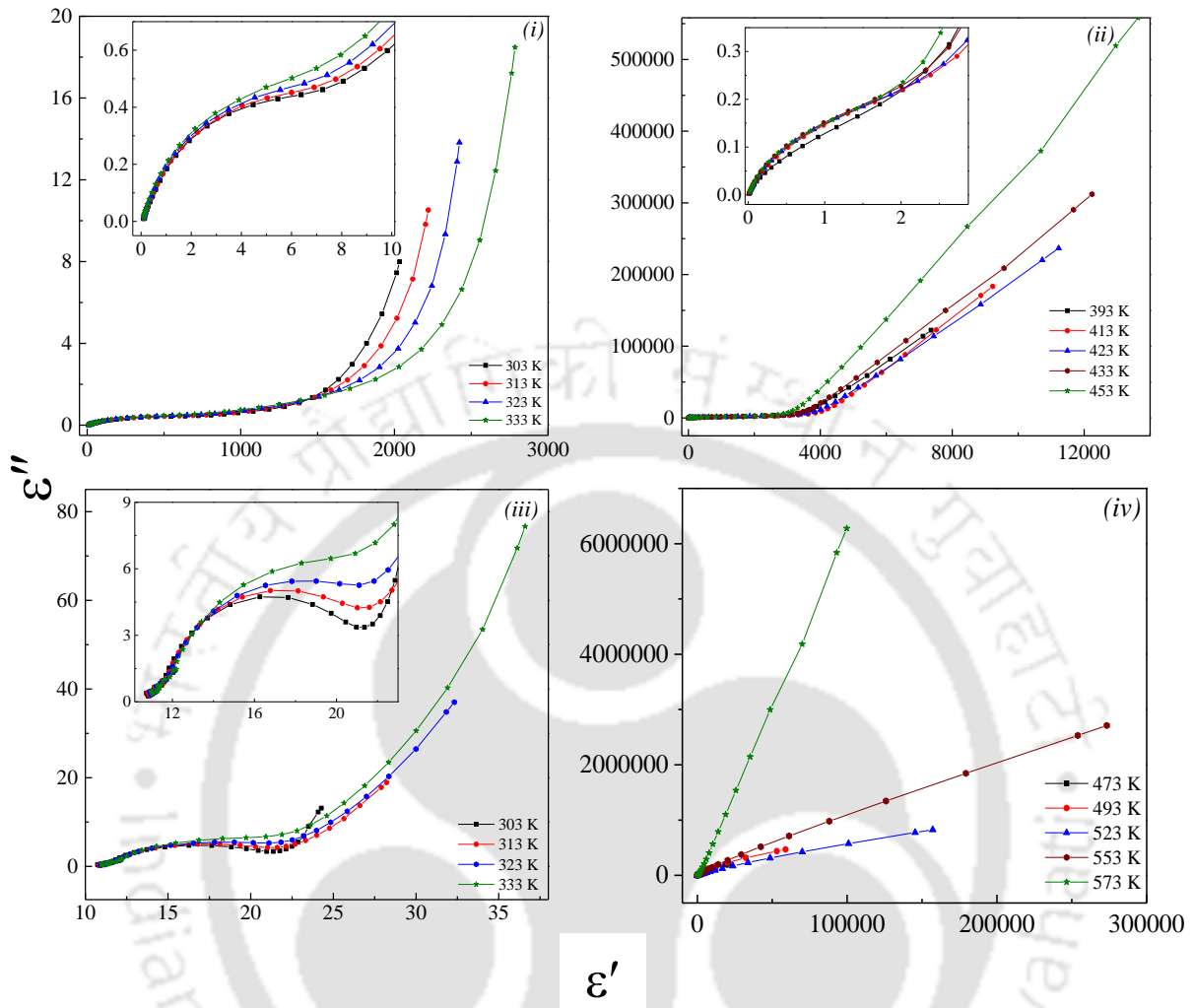
In order to understand the ac-electrical transport in these two phase composites, we calculate the ac-electrical conductivity ( $\sigma_{ac}$ ) using the following relation:  $\sigma_{ac}(\omega) = \omega \epsilon'' \epsilon_0$  [263]. In this equation  $\epsilon_0$  is free space permittivity ( $8.854 \times 10^{-12} \text{ F/m}$ ). Figures 6.26 and 6.27 shows the frequency variation of ac-conductivity  $\sigma_{ac}(\omega)$  over a wide temperature range,  $120 \text{ K} \leq T \leq 293 \text{ K}$  and  $303 \text{ K} \leq T \leq 573 \text{ K}$ . As one can see from the figures that conductivity curve for a particular temperature is characterized by a frequency independent plateau region (lower frequency side) and a frequency dispersive region at higher frequency. The frequency independent plateau region (dc conductivity) at low frequency can be attributed to long range translation motion of charge carriers due to the



**Figure 6.23:** The frequency dependence of real component of complex permittivity ( $\epsilon'$ ) for different compositions (i)  $x = 0$  (ii)  $x = 0.23$  (iii)  $x = 0.46$  of two-phase composites ( $(1-x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$ ) measured between the temperatures 123 K and 293 K; and (iv)  $x = 0$  (v)  $x = 0.23$  (vi)  $x = 0.46$  of two-phase composites ( $(1-x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$ ) measured between the temperatures 303 K and 573 K. Insets shows the corresponding frequency dependence of imaginary component of complex permittivity ( $\epsilon''$ ).



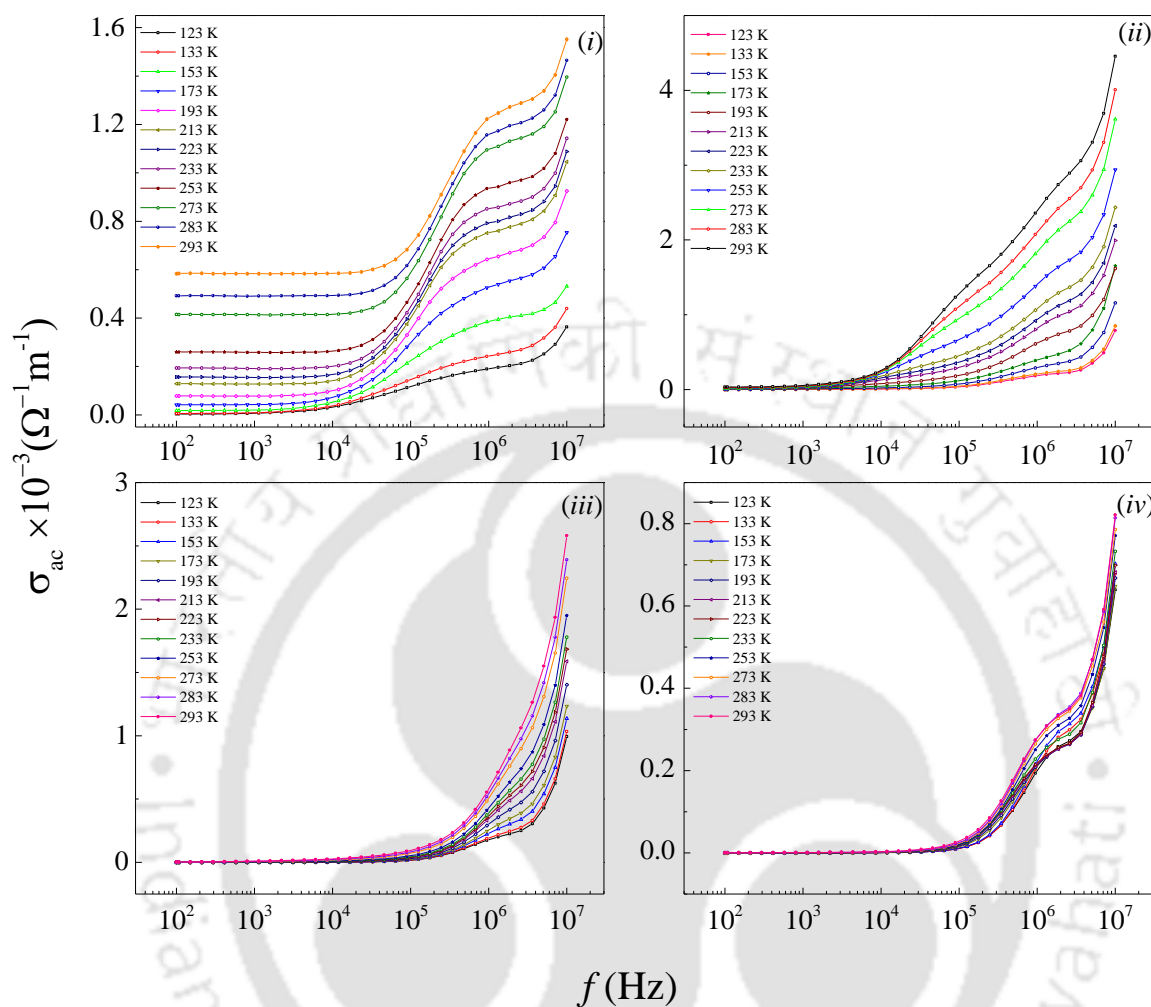
**Figure 6.24:** Cole-Cole plots ( $\epsilon''$  vs.  $\epsilon'$ ) recorded at different temperatures between 123 K and 273 K for different compositions (i)  $x = 0$ , (ii)  $x = 0.23$ , (iii)  $x = 0.46$ , (iv)  $x = 0.706$ , (v)  $x = 0.882$ , and (vi)  $x = 1.0$ . Insets show the zoomed view of the selected region.



**Figure 6.25:** Cole-Cole plots ( $\epsilon''$  vs.  $\epsilon'$ ) recorded at different temperatures between 303 K and 573 K for different compositions (i)  $x = 0$ , (ii)  $x = 0.23$ , (iii)  $x = 0.46$ , (iv)  $x = 0.706$ , (v)  $x = 0.882$ , and (vi)  $x = 1.0$ ). Insets show the zoomed view of the selected region.

successful hopping to neighborhood vacant sites. In 1993, Funke *et al.*, successfully explained such kind of hopping mechanism using Jump-Relaxation model [264]. According to this model, there could be two process at high frequency region: (i) successful hopping and (ii) unsuccessful hopping. In the case of unsuccessful hopping, the jumping ion may come back to its initial position, whereas, for successful hopping the neighborhood ions become relaxed with respect to the jumping ions position and the jumping ion occupies a new site. With increase in frequency the ratio of the successful to unsuccessful hopping increases, as a result the dispersive conductivity increases at higher frequencies. Such frequency dependent conductivity can be explained mathematically by Jonscher's Power Law (JPL) [265]:

$$\sigma_{ac} = \sigma_{dc} + A\omega^s \quad (6.4)$$

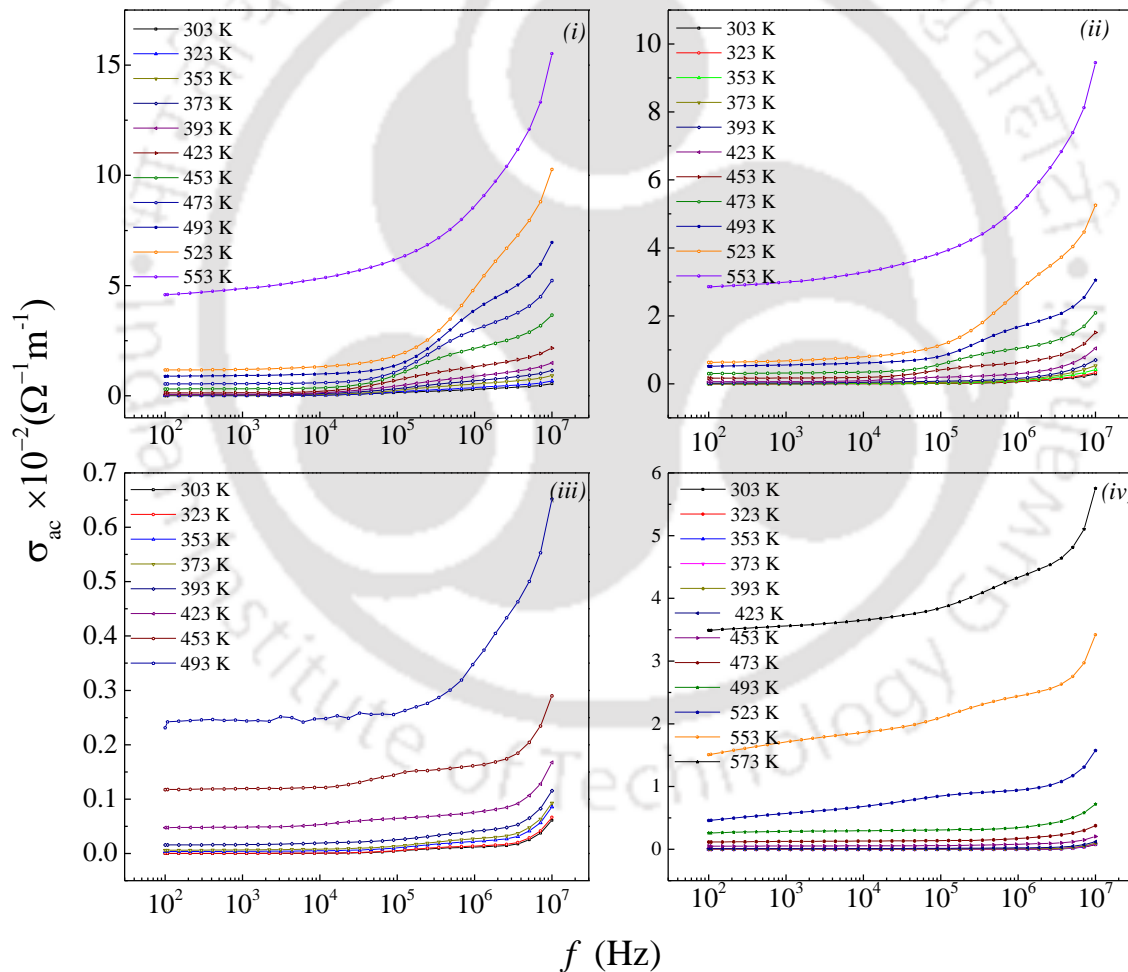


**Figure 6.26:** Frequency dependence of ac-electrical conductivity of  $(1-x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  for different compositions (i)  $x = 0$ , (ii)  $x = 0.23$ , (iii)  $x = 0.46$ , and (iv)  $x = 0.706$  measured at various temperatures between 123 K and 293 K.

where  $\sigma_{dc}$  is the frequency independent conductivity of the material, ‘A’ is the dispersion parameter and ‘s’ is the dimensionless frequency exponent factor, which represents the measure of the degree of interaction. Using the above equation, we evaluated the magnitude of ‘s’ (0.2 - 2.9) for different compositions of the two phase composites and plotted as a function of ‘x’ (Figure 6.28). Within the JPL framework, the ‘s’ values usually lie between 0 and 1 ( $0 \leq s \leq 1$ ) for semiconductors, polymers, ceramics, ion conducting glasses and heavily doped ionic crystals [265]. Nonetheless,  $s > 1$  is also reported for few ion-conducting glasses [266, 267], single crystals of  $\text{K}_2\text{SO}_4$  [268],  $\text{K}_3\text{H}(\text{SeO}_4)$  [269], perovskite compound such as  $\text{Pr}_{0.6}\text{Sr}_{0.4}\text{Mn}_{0.6}\text{Ti}_{0.4}\text{O}_{3\pm\delta}$  [270],  $\text{Ca}_{1-x}\text{Sr}_x\text{TiO}_3$  [271],  $\text{BaZr}_{0.05}\text{Ti}_{0.95}\text{O}_3$  [272], and in multiferroic layer thin films of  $\text{PbZr}_x\text{Ti}_{1-x}\text{O}_3/\text{CoFe}_2\text{O}_4$  [272]. In the present case ‘s’ values lie in both less than and greater than unity. The less than unity value of ‘s’ can be attributed to the hopping conduction of mobile charge carriers through the energy barrier between two sites [273]. Whereas the ‘s’ value

greater than 1 can be attributed to the motion of charge carriers or oxygen vacancies from site to site with quantum mechanical tunneling between asymmetric double-well potential [274].

The Arrhenius ac-conductivity plots of  $\ln\sigma_{ac}$  versus  $1000/T$  at different frequencies are shown in figure 6.29 and 6.30 for low temperature region ( $123 \text{ K} \leq T \leq 293 \text{ K}$ ) and high temperature region ( $303 \text{ K} \leq T \leq 573 \text{ K}$ ), respectively. A change in the slope of the curve clearly reflects from the figures. It is believed that slight change in the slope corresponds to a specific transition in the compound. But in the present case, there is no phase transitions in the temperature range shown in the figures. The change in the slope can be due to the contribution of different regions in the polycrystalline samples, such as grains, grain boundaries etc. [275] Therefore, the change in the slope is a reflection of different conduction mechanism. From this variation it is clear that the



**Figure 6.27:** Frequency dependence of ac-conductivity of  $(1-x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  (i)  $x = 0.23$ , (ii)  $x = 0.46$  (iii)  $x = 0.706$ , and (iv)  $x = 1.0$  measured at various temperatures between 303 K and 573 K.

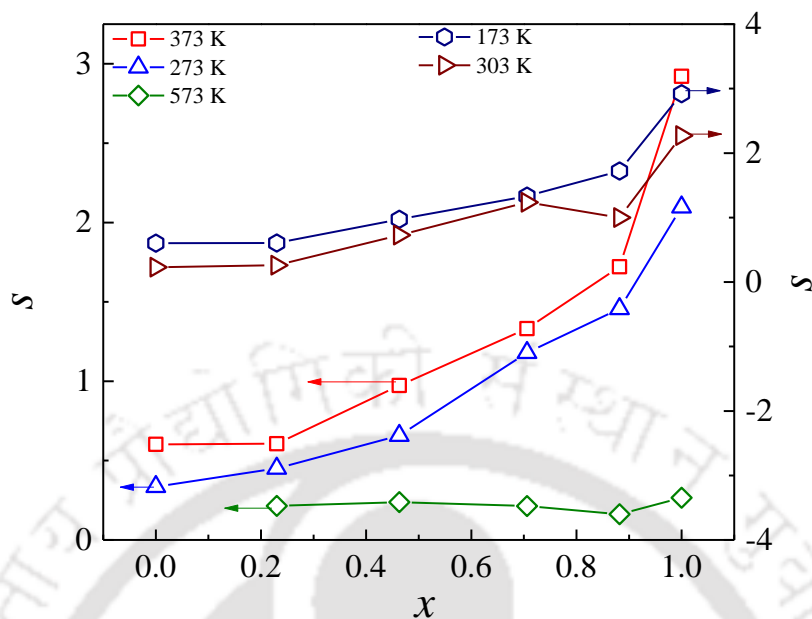


Figure 6.28: Frequency exponent ( $s$ ) plotted as a function of composition ( $x$ ) measured at selected temperatures.

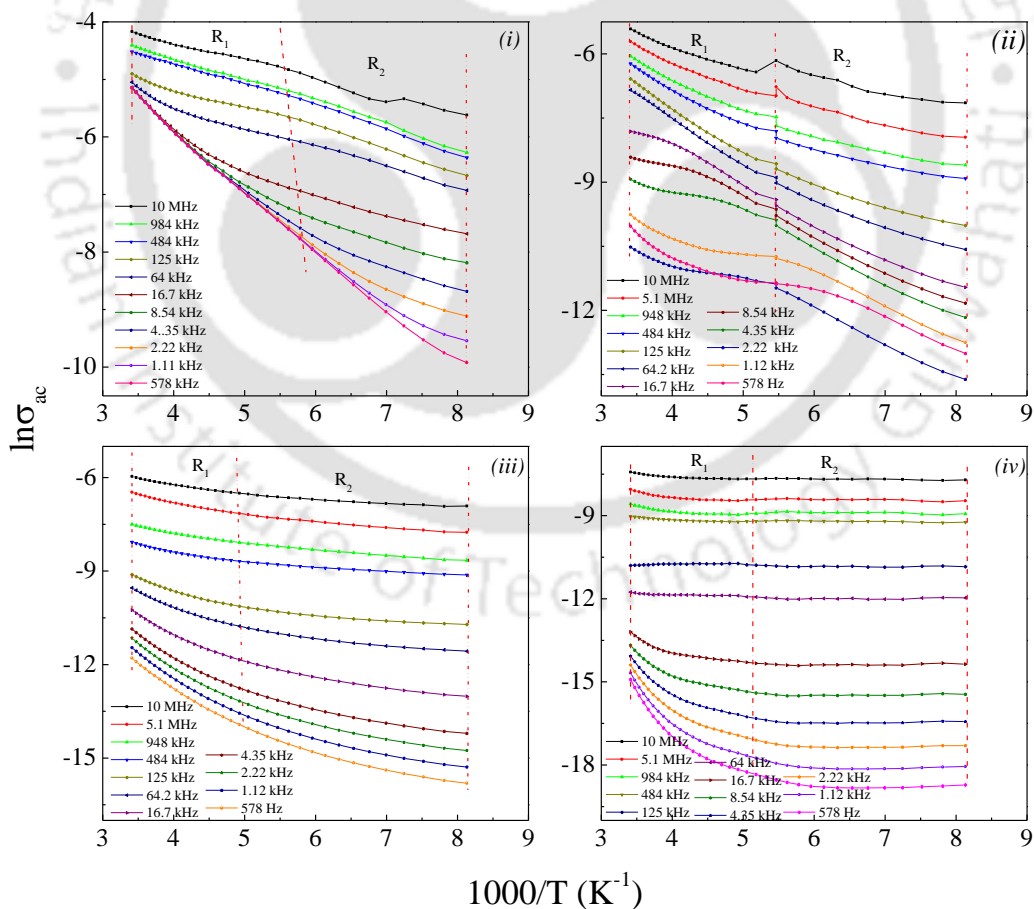
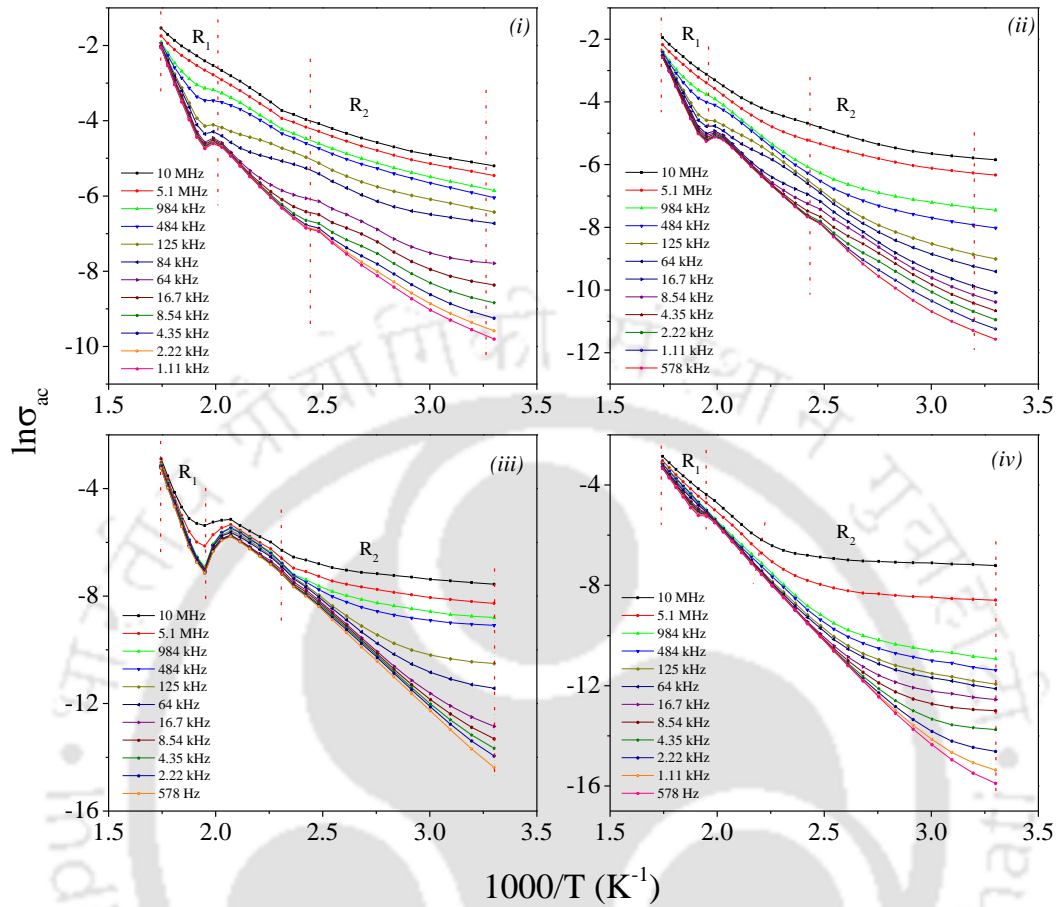


Figure 6.29: Logarithmic variation of  $\sigma_{ac}$  versus  $1000/T$  for the compositions (i)  $x = 0.0$ , (ii)  $x = 0.23$ , (iii)  $x = 0.46$ , and (iv)  $x = 0.882$  calculated at different frequencies.



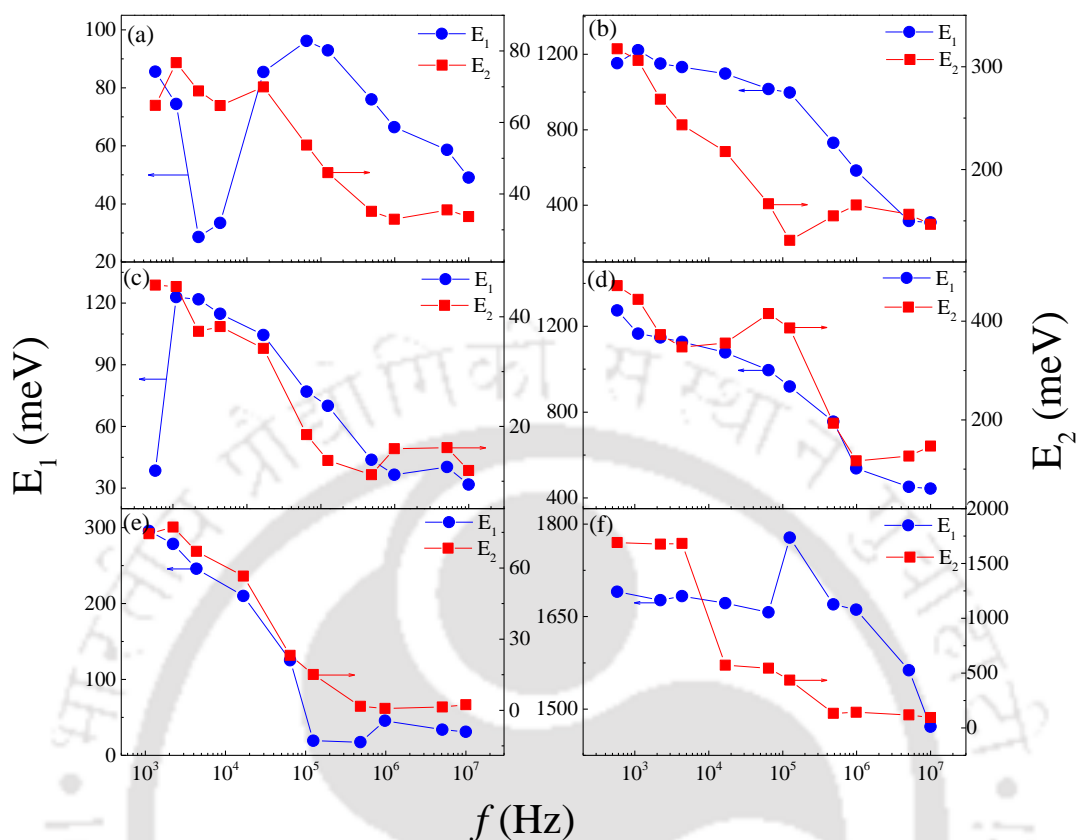
**Figure 6.30:**  $\ln\sigma_{ac}$  versus  $1000/T$  for (i)  $x = 0.0$ , (ii)  $x = 0.23$ , (iii)  $x = 0.46$ , and (iv)  $x = 0.882$  composites; measured at different frequencies.

conductivity variation in the composites is a thermally activated process. The activation energy ( $E_a$ ) of the thermally activated process can be calculated by the Arrhenius equation:

$$\sigma = \sigma_o \exp\left(-\frac{E_a}{k_B T}\right) \dots (6.5)$$

Where  $\sigma_o$  is the pre-exponent factor,  $E_a$  is the activation energy,  $k_B$  is the Boltzman constant and ‘T’ is the measurement temperature.

Figure 6.31 shows the frequency variation of  $E_a$  [ $E_1$ ; in region 1 ( $R_1$ ) and  $E_2$  in region 2 ( $R_2$ )] for  $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$  ( $0 < x < 1$ ) two phase composites. From the figure we observed that the activation energy has a tendency to decrease with increase in frequency due to the enhancement of the electronic jumps between localized states as the frequency increases. We also study the variation of activation energy ( $E_a$ ) as a function of ‘x’ for two selected frequency 125 kHz and 16.7 kHz (figure 6.32). For all the samples we obtained lower values of activation

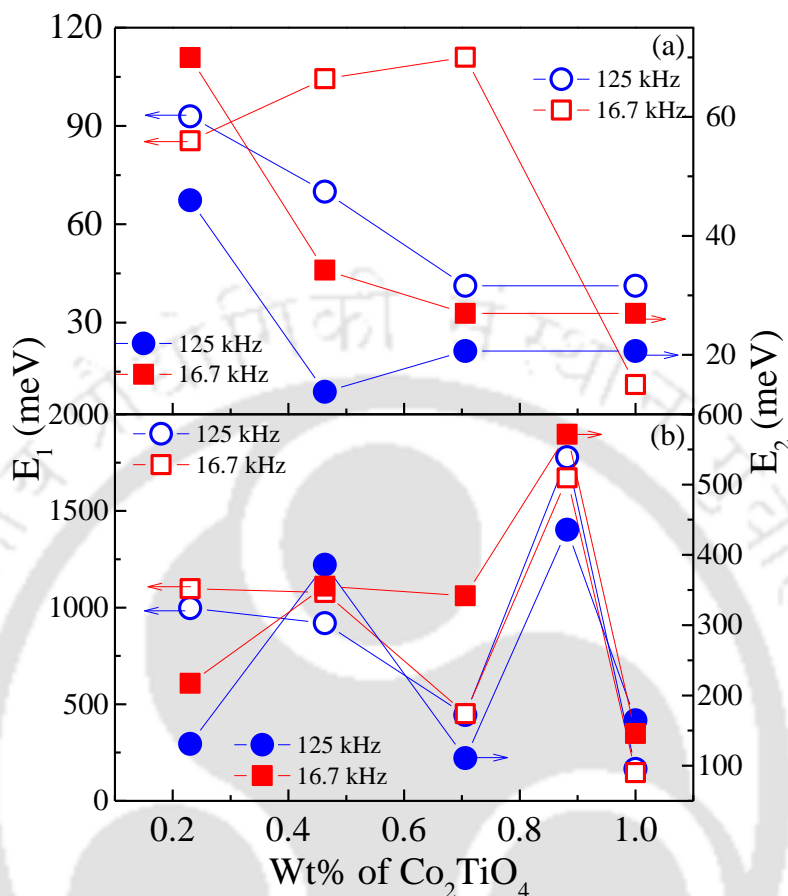


**Figure 6.31:** Frequency dependence activation energies ( $E_1$  and  $E_2$ ) of various compositions (a)  $x = 0.23$ , [for  $123\text{K} \leq T \leq 293\text{K}$ ] (b)  $x = 0.23$  [for  $303\text{K} \leq T \leq 573\text{K}$ ], (c)  $x = 0.46$  [for  $123\text{K} \leq T \leq 293\text{K}$ ], (d)  $x = 0.46$  [for  $303\text{K} \leq T \leq 573\text{K}$ ], (e)  $x = 0.882$  [for  $123\text{K} \leq T \leq 293\text{K}$ ], (f)  $x = 0.882$  [for  $303\text{K} \leq T \leq 573\text{K}$ ].

energies. Such low value of activation energy can be attributed to the influence of electronic contribution to the overall conductivity [276].

### 6.3.8 Summary:

In summary, we studied the structural, vibrational, magnetization, dielectric behavior of  $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$  ( $0 \leq x \leq 1$ ) two-phase composites. Major changes in the bond-angles and bond-lengths were noticed for various compositions of the solid-solutions  $(1-x)\text{Co}_3\text{O}_4 + x\text{Co}_2\text{TiO}_4$ . The bond angle A-O-B exhibits a maximum value of  $130.35^\circ$  for  $x = 0.706$  as compared to  $122.7^\circ$  for dilute compositions. Conversely, the B-O-B bond angle shows its minimum value of  $82.6^\circ$  for  $x = 0.706$ . On the other hand, the bond lengths of A-O and B-O varies from  $1.854 \text{ \AA}$  to  $1.984 \text{ \AA}$  and  $1.958 \text{ \AA}$  to  $2.025 \text{ \AA}$ , respectively as the system transforms from normal spinel ( $x = 0$ ) to inverse spinel ( $x = 1$ ). Such changes are associated with the higher ionic sizes of 'Ti' ions ( $1.34 \text{ \AA}$ ) as compared to the Co ions ( $1.09 \text{ \AA}$ ).

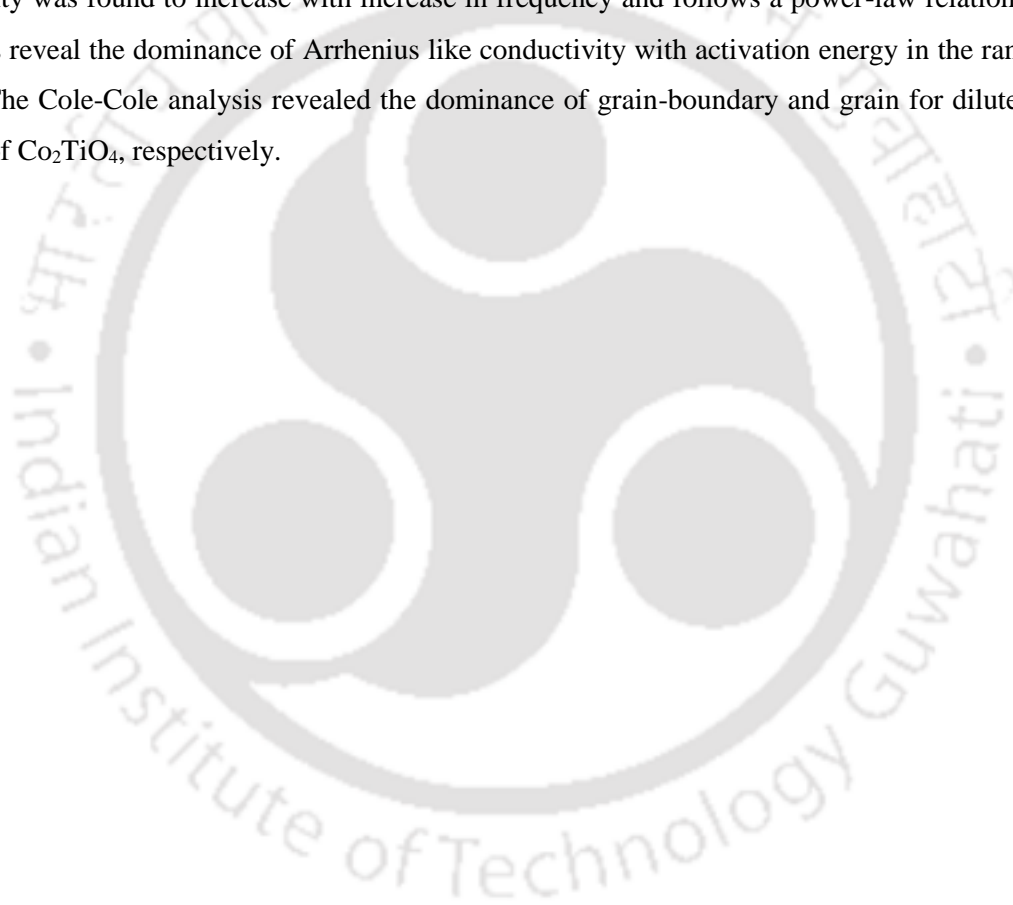


**Figure 6.32:** Activation energies ( $E_1$  and  $E_2$ ) plotted as a function of compositions measured at two different frequencies (16.7 kHz and 125 kHz).

Five Raman-active modes centered at  $194.6\text{ cm}^{-1}$ ,  $480\text{ cm}^{-1}$ ,  $517.8\text{ cm}^{-1}$ ,  $617.7\text{ cm}^{-1}$ ,  $688.1\text{ cm}^{-1}$  were observed for all the compositions 'x' which are associated to the  $F_{2g}(3)$ ,  $E_g(1)$ , and  $A_{1g}(1)$  vibrational modes. The substitution of  $\text{Co}_2\text{TiO}_4$  grains within the  $\text{Co}_3\text{O}_4$  matrix leads to hypsochromic-shift of  $6.3\text{ cm}^{-1}$  of  $A_{1g}$  vibrational modes due to the smaller atomic mass and larger ionic radius ( $0.67\text{ \AA}$ ) of  $\text{Ti}^{3+}$  than  $\text{Co}^{3+}$  ions ( $0.545\text{ \AA}$ ). A giant bathochromic-redshift ( $\sim 25.23\text{ cm}^{-1}$ ) of  $F_{2g}$  mode was noticed when the system crossovers from normal-spinel ( $\text{Co}_3\text{O}_4$ ) to inverted-spinel ( $\text{Co}_2\text{TiO}_4$ ). The third Raman active mode  $F_{2g}$  located at  $617.7\text{ cm}^{-1}$  vanishes totally in the  $\text{Co}_2\text{TiO}_4$  system due to the complete occupation of octahedral sites by  $\text{Ti}^{3+}$  ions. The temperature variation of peak positions of  $A_{1g}$  and  $F_{2g}$  phonon modes show clear anomalies across 25 K to 55 K which are associated with the change in the paramagnetic to antiferromagnetic ordering. For lower 'Ti' compositions the characteristic binding energies of  $\text{Co-}2p_{3/2}$ ,  $2p_{1/2}$  reveals the trivalent and divalent oxidation states of Co at the octahedral and tetrahedral sites, respectively. However, for  $x \geq 0.706$  typical signatures of trivalent character of 'Ti' ions at the octahedral sites of

inverse spinel structure was observed instead of tetravalent 'Ti' ions. Also, a weak ' $\text{Co}^{3+}$ ' character together with ' $\text{Co}^{2+}$ ' (major component) at the octahedral sites of  $\text{Co}_2\text{TiO}_4$  was noticed.

Magnetic characterization reveals dominant ferrimagnetic interaction in all these composites below 50 K with different magnetic moments of 'Co' on the A sites ( $3.87 \mu_B$ ) and B sites ( $5.19 \mu_B$ ) for  $x = 1$ . For  $T < T_N$ , both the  $\chi_{ZFC}(T)$  and  $\chi_{FC}(T)$  curves exhibit magnetic-compensation ( $T_{\text{COMP}}$ ) phenomena where  $\chi(T)$  approaches to zero value due to the complete balance of two sublattices magnetizations. A gradual increase of  $T_{\text{COMP}}$  from 31.74 K to 37.72 K was noticed when ' $x$ ' changes from 1 to 0.23. Below  $T_N$  large magnitudes of  $H_C$  ( $\sim 19$  kOe for  $x = 0.23$  at  $T = 10$  K) and exchange bias  $H_{\text{EB}}$  ( $\sim 887$  Oe for  $x = 1$  at  $T = 10$  K) was observed. The frequency variation of ac-conductivity was found to increase with increase in frequency and follows a power-law relation ( $\sigma_{\text{ac}} \sim A\omega^s$ ). These studies reveal the dominance of Arrhenius like conductivity with activation energy in the range 2 meV to 1800 meV. The Cole-Cole analysis revealed the dominance of grain-boundary and grain for dilute and heavily substitution of  $\text{Co}_2\text{TiO}_4$ , respectively.

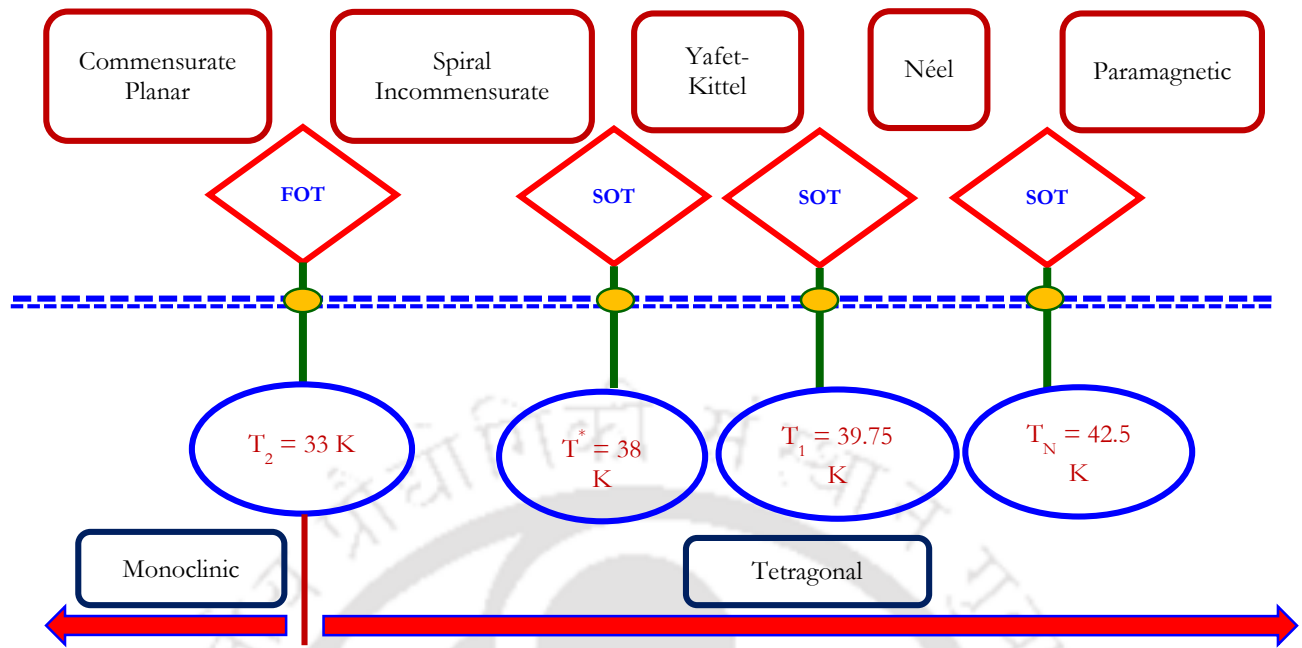


## Lock-in Transition at 38 K in Tetragonally Distorted Frustrated Spinel $\text{Mn}_3\text{O}_4$

### 7.1 Literature Survey:

Strongly correlated systems are characterized by a competing magnetic interaction involving spin, charge, lattice, and orbital degrees of freedom, which often leads to a near degeneracy between competing phases [277]. Such degeneracy can also cause the coexistence of phases, giant magneto-dielectric and magneto-thermal properties in response to external perturbations such as magnetic field and temperature [89, 278 - 288]. Spinel oxides exhibit strong correlations between spin, charge, orbital, and lattice degrees of freedom due to a magnetically frustrating sublattice and anisotropy. Consequently, a wide variety of phenomena have been reported for spinels, including charge ordering [289, 290], heavy fermion behavior [291], and multiferroicity [292 - 296]. Magnetic frustration in spinel oxides with orbital degeneracy provides an exciting platform for some novel ordered as well as spin-disordered states often called as spin liquid-like states [297 - 299]. This chapter is dedicated to highly frustrated tetragonally distorted ferrimagnetic spinel  $\text{Mn}_3\text{O}_4$  (hausmannite), which, exhibits novel phenomena in the magnetically ordered state; such as large magnetodielectric, magnetoelastic responses, field-induced structural changes in the low-frequency dielectric constant and giant atomic displacement [85, 89, 90]. All these changes in  $\text{Mn}_3\text{O}_4$  have been attributed to the field-induced transitions between two distinct magnetostructural phases [85, 89, 90]. In  $\text{Mn}_3\text{O}_4$ , the di- and tri-valent Mn-ions ( $\text{AB}_2\text{O}_4$ ;  $\text{A} = \text{Mn}^{2+}$ ,  $\text{B} = \text{Mn}^{3+}$ ) arrange in a tetragonally distorted array below 1433 K above which it shows perfect cubic spinel [21, 139, 300 - 308]. Its magnetic properties were investigated long ago but still the subject of active research because of new observations [85 - 91, 307, 309 - 313]. The most significant findings being: (a) magnetic field dependent tetragonal-to-monoclinic structural phase transformation below 33 K, [91] (b) new magnetic anomaly of lock-in transition at 38 K, [312] (c) Giant atomic displacement of 0.25 Å without breaking inversion symmetry and colossal magnetic anisotropy,[300](d)strong magneto-dielectric coupling,[89, 90] and (e) large magnetic entropy difference of  $\sim 11 \text{ J K}^{-1} \text{ kg}^{-1}$  for a field change of 20 kOe at 43 K [313].  $\text{Mn}_3\text{O}_4$  is a normal-spinel with  $\text{Mn}^{2+}$  and  $\text{Mn}^{3+}$  ions in  $3d^5$  and  $3d^4$  configuration, respectively, but exhibits very complex magnetic ordering (figure 7.1). Also, it undergoes several magnetic phase transitions below the ferri-magnetic Néel temperature  $T_N \sim 43 \text{ K}$  [138, 140]. Another important characteristic is the prevalence of strong anti-ferromagnetic interaction between  $\text{Mn}^{3+}$  ions vis-a-vis  $\text{Mn}^{2+} - \text{Mn}^{3+}$ , which happens to be unfavorable to collinear structure leading to geometrical frustration [85, 140, 314]. However, some improvement in understanding the unique physical properties of  $\text{Mn}_3\text{O}_4$  has been possible due to the novel characterization techniques like magnetic-field dependent Raman scattering,  $^{55}\text{Mn}$  nuclear magnetic resonance (NMR), neutron diffraction, etc.[88, 93, 311, 314, 315].

The first-order phase transition, associated with tetragonal to monoclinic structural transformation, observed by Kim *et al.* at  $T_2 = 33 \text{ K}$  using temperature and field dependent Raman scattering experiments motivated several



**Figure 7.1:** The schematic representation of magnetic and structural transitions observed in polycrystalline  $Mn_3O_4$  below the Néel temperature  $T_N$ . The abbreviations FOT and SOT correspond to first- and second-order transitions, respectively [312, 313].

researchers to re-investigate the physical properties of  $Mn_3O_4$  [86, 91]. Previous studies reported four magnetic transitions below  $T_N$  along with a well-defined magneto-dielectric coupling [89, 90, 93, 138, 140, 307, 312, 314, 315]. The magnetic ordering follows the sequence given in figure 7.1. On the other hand, magnetic field and temperature dependence of dielectric permittivity  $\{\epsilon_r(H,T)\}$  and strain  $\{\Delta L/L(H,T)\}$  data of  $Mn_3O_4$  single crystals revealed three distinctly different characteristics below  $T_N$  with large anisotropic magneto-capacitance [103]. Also, the evidence of magneto-dielectric coupling associated with the spin-phonon interaction has been reported in polycrystalline  $Mn_3O_4$  [103].

Although numerous studies exist on  $Mn_3O_4$ , its dynamic behavior of magnetism at small ac-magnetic fields of varying frequencies were lacking in the literature when we initiated this problem. Therefore, the present chapter is devoted to the ac-magnetic response of all the phase transitions occurring below  $T_N$  under the superimposition of various dc-bias fields. In addition, the nature of these transitions has been studied under both cooling and heating cycles of magnetic-field dependent dielectric permittivity with special emphasis on the lock-in transition at 38 K [312, 313].

## 7.2 Experimental Details and Growth of Hausmannite:

Oxalate based sol-gel process has been chosen to synthesize  $Mn_3O_4$  polycrystalline sample. Thermal decomposition of the oven-dried product ( $MnC_2O_4 \cdot 2H_2O$ ) (Alfa Aesar, purity 99.99%) at  $500^\circ C$  for 2 h duration

yields Mn<sub>2</sub>O<sub>3</sub> as a major product; further annealing of this sample at 1100°C for 4 h in air leads to the formation of Mn<sub>3</sub>O<sub>4</sub> powder. This powder is grounded in an agate mortar, pressed into bars and finally sintered at 1100°C for 12 h. During the sintering process abrupt quenching was done from 1473 K to 77 K using liquid nitrogen. Since the melting temperature of Mn<sub>2</sub>O<sub>3</sub> is 1213 K one can expect the formation of Mn<sub>3</sub>O<sub>4</sub> at any temperature  $T > 1213$  K depending on the availability of oxygen content. Thus, abrupt quenching from 1473 K to 77 K will avoid the formation of Mn<sub>2</sub>O<sub>3</sub> (i.e. preventing the memory retrace) and pure Mn<sub>3</sub>O<sub>4</sub> will remain intact as primary product. The crystallinity of the sample and the structure has been studied using a Panalytical X'pert Pro diffractometer using Cu-K $\alpha$  radiation, which indicate monophasic nature of this compound consistent with the hausmannite Mn<sub>3</sub>O<sub>4</sub> reported in the literature [313]. A superconducting quantum interference device (SQUID) based magnetometer (Quantum design MPMS-XL5) has been used for the temperature dependent magnetization measurements  $M_H(T)$  in low-field, while magnetic isotherms  $M_T(H)$  up to 90 kOe were recorded by means of an extraction technique in a “physical property measurement system” (PPMS, Quantum design). The heat capacity curves  $C_P(T)$  (for  $H = 0$  and 20 kOe) were recorded from 2 K to 100 K by using a semi-adiabatic relaxation technique in the PPMS.

### **7.3 Experimental Results and Analysis:**

#### **7.3.1 Structural and Morphological Characterization:**

The X-ray diffraction pattern recorded at room temperature using the Cu-K $\alpha$  X-ray source of wavelength  $\lambda = 1.5406$  Å along with the Rietveld refinement data (performed by FullProf program) of Mn<sub>3</sub>O<sub>4</sub> sample (without quenching) is shown in figure 7.2 (a). The diffractogram contains mainly Mn<sub>3</sub>O<sub>4</sub> phase. However, a detailed analysis of the X-ray diffraction pattern reveals a tiny peak near the Bragg angle  $2\theta = 32.027^\circ$  corresponding to the 100% intensity peak of (222) reflection from Mn<sub>2</sub>O<sub>3</sub> (inset of the figure 7.2(a)). This analysis indicates that the synthesized sample contains a tiny amount of unreacted Mn<sub>2</sub>O<sub>3</sub> as secondary phase. From this result we can conclude, that Mn<sub>3</sub>O<sub>4</sub> retraces its memory by forming Mn<sub>2</sub>O<sub>3</sub> phase while cooled naturally. The weight % of secondary phase i.e. Mn<sub>2</sub>O<sub>3</sub> present in the sample can be quantitatively estimated using the following formula [110].

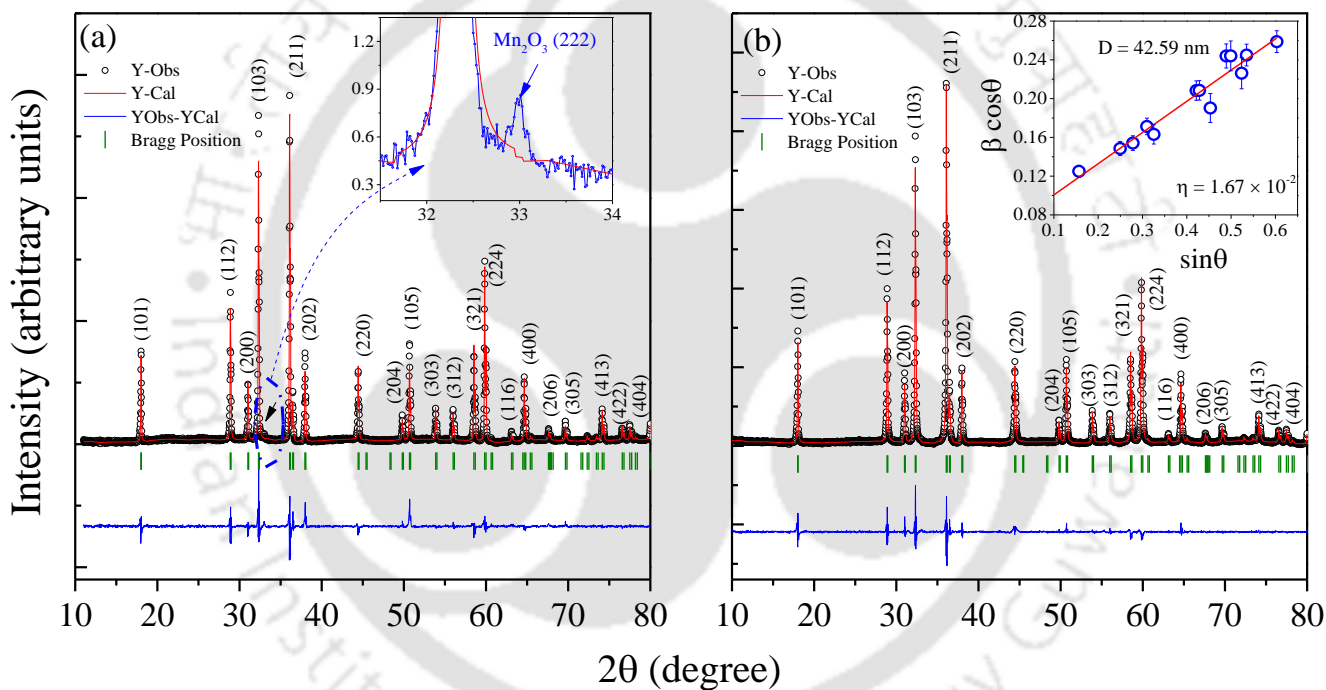
$$W_{Mn_2O_3} = [1/\{1 + 1.265 (I_{Mn_3O_4}/ I_{Mn_2O_3})\}] \times 100 \quad \dots (7.1)$$

where  $W_{Mn_2O_3}$  indicates the weight fraction of the Mn<sub>2</sub>O<sub>3</sub> phase, and  $I_{Mn_2O_3}$  and  $I_{Mn_3O_4}$  represents the strongest X-ray diffraction line intensities of the Mn<sub>2</sub>O<sub>3</sub> and Mn<sub>3</sub>O<sub>4</sub>, respectively. In the present case, intensities of (211) peak for Mn<sub>3</sub>O<sub>4</sub> phase and (222) peak for Mn<sub>2</sub>O<sub>3</sub> were considered as maximum intense Miller Indices of reflections. Using the above equation we found that ~ 2.35 wt% of Mn<sub>2</sub>O<sub>3</sub> present in the sample as a secondary phase.

In order to avoid the formation of Mn<sub>2</sub>O<sub>3</sub> phase we quenched the temperature of sintered sample from 1100°C to liquid-nitrogen temperature 77 K. The X-ray diffraction pattern of the sintered Mn<sub>3</sub>O<sub>4</sub> pellet after quenching indicates monophasic nature of this compound (figure 7.2(b)). The lattice parameters obtained from the Rietveld

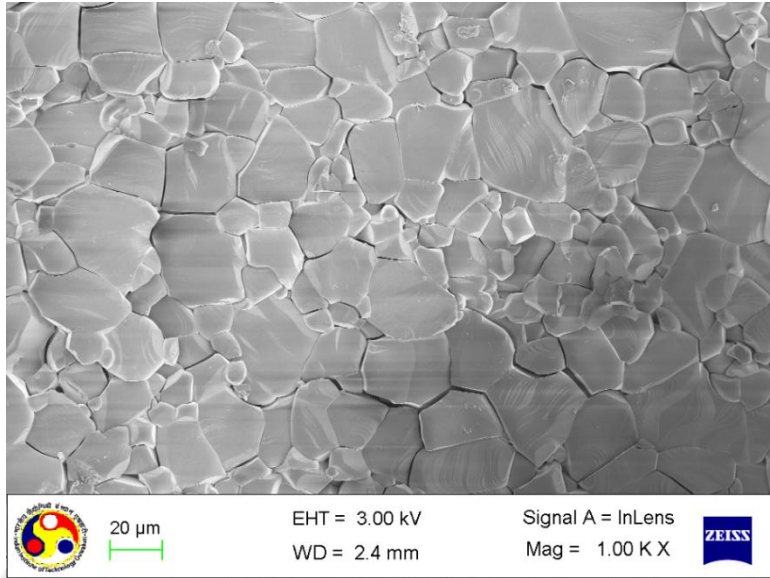
**Table 7.1:** List of various crystal structure parameters (i) lattice parameter, (ii) bond Length and (iii) bond angles of both quenched and without quenched Mn<sub>3</sub>O<sub>4</sub> samples obtained from the refinement process.

System	Lattice Parameter		Interaxial angles $\alpha = \beta = \gamma$	Bond Length		Bond Angle	
	$a = b$	$c$		A-O	B-O	A-O-B	B-O-B
Mn <sub>3</sub> O <sub>4</sub> (without uenching)	$5.76 \pm 0.01 \text{ \AA}$	$9.47 \pm 0.01 \text{ \AA}$	90°	$2.03 \pm 0.01 \text{ \AA}$	$1.92 \pm 0.02 \text{ \AA}$	$120.68^\circ \pm 0.61^\circ$	$94.16^\circ \pm 0.48^\circ$
Mn <sub>3</sub> O <sub>4</sub> (with quenching)	$5.76 \pm 0.01 \text{ \AA}$	$9.47 \pm 0.01 \text{ \AA}$	90°	$2.03 \pm 0.02 \text{ \AA}$	$1.93 \pm 0.02 \text{ \AA}$	$119.79^\circ \pm 0.62^\circ$	$94.86^\circ \pm 0.47^\circ$



**Figure 7.2:** XRD pattern and the corresponding Rietveld refined data of Mn<sub>3</sub>O<sub>4</sub> polycrystals prepared from the thermal decompositions of the oven dried precursors followed by (a) sintering at 1100°C without quenching and (b) after quenching from 1100°C to liquid nitrogen temperature (77 K). The inset of (a) shows zoomed view of the reflection pattern between  $2\theta = 31.5^\circ$  and  $34^\circ$  depicting the reflection of (222) peak of Mn<sub>2</sub>O<sub>3</sub> which is presented as minor phase and inset of (b) shows the Williamson hall plot.

refinement process using FullProf suit are  $a = b = 5.76 \text{ \AA}$  and  $c = 9.46 \text{ \AA}$  with space group  $I4_1/amd$ . Table-7.1 summarizes the parameters of both quenched and without quenched samples obtained from the refinement process. Using these lattice parameters we have estimated the unit-cell density  $\rho = 4.83 \text{ g/cm}^3$  for polycrystalline Mn<sub>3</sub>O<sub>4</sub> sample, which is consistent with the standard reported value ( $4.86 \text{ g/cm}^3$ ) in the literature. Using



**Figure 7.3:** Field Emission Scanning Electron Microscope image of Mn<sub>3</sub>O<sub>4</sub>

Williamson-Hall analysis we have also estimated the average grain size ( $D$ ) and micro-strain ( $\eta$ ) present in the sample. The Williamson-Hall equation can be written as:

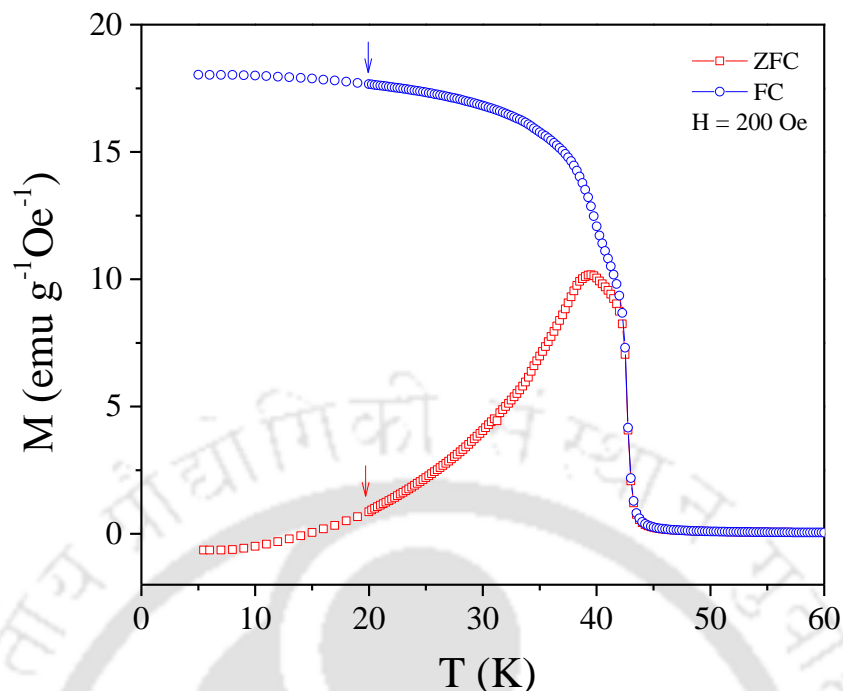
$$\beta \cos \theta = \frac{K\lambda}{D} + 4\eta \sin \theta \dots (7.2)$$

where,  $\beta$  is the full-width-at-half-maximum of diffraction peak and the constant 'K' is shape factor (= 0.89). From the  $\beta \cos \theta$  versus  $\sin \theta$  plot shown in the inset of figure 7.2(b) we have estimated the values of  $D$  and  $\eta$  are 42.59 nm and  $1.67 \times 10^{-2}$ , respectively. This analysis indicates that the contribution from lattice strain is significant (cannot be neglected) due to abrupt quenching of the sample from 1100°C to 77 K. Morphology of Mn<sub>3</sub>O<sub>4</sub> sample sintered at 1100°C has been studied using FESEM. Figure 7.3 represents the FESEM micrograph recorded under secondary electron mode depicting grain sizes in the range 8-20  $\mu\text{m}$ .

### 7.3.2 Magnetic Properties and Evidence for the Lock-in transition:

Figure 7.4 depicted the temperature dependence of the magnetization  $M(T)$  of Mn<sub>3</sub>O<sub>4</sub> sample measured under zero-field cooled (ZFC) and field-cooled (FC) conditions at an external magnetic field  $H_{dc}$  of 200 Oe for  $T < 60$  K. The magnetization data was recorded at a very close temperature interval ( $\Delta T$ ) of 0.1 K from 20 to 60 K and  $\Delta T = 1$  K for  $T \leq 20$  K (marked by arrows in figure 7.4). Note that both  $M_{ZFC}$  and  $M_{FC}$  show a sharp transition across  $T_p \sim 39.5$  K below the ferrimagnetic Néel temperature  $T_N \sim 43$  K with strong irreversibility below  $T_N$  arising due to the local anisotropy effect.

Since the average grain sizes of the Mn<sub>3</sub>O<sub>4</sub> samples after quenching to 77 K are in the range of 8 - 20  $\mu\text{m}$  (figure 7.3), the irreversibilities cannot be due to blocking/spin-glass effects. It is well known that such irreversibilities indicated by the difference between the magnetization under ZFC and FC conditions arise from

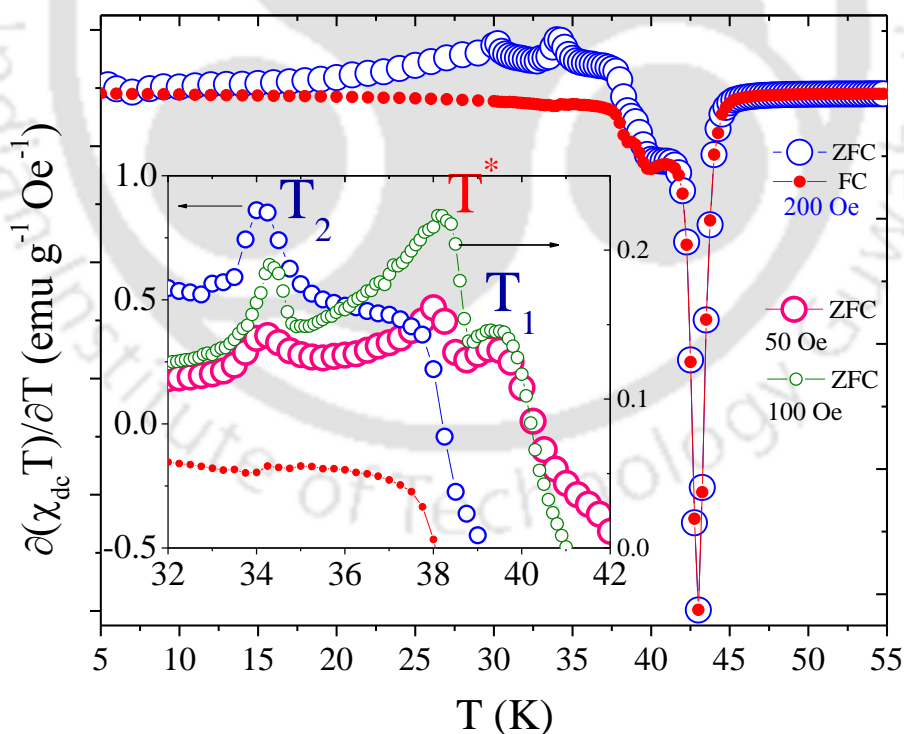


**Figure 7.4:** Temperature dependence of dc magnetization  $M(T)$  recorded under zero-field cooled ZFC and field cooled FC conditions at an external magnetic field 200 Oe.

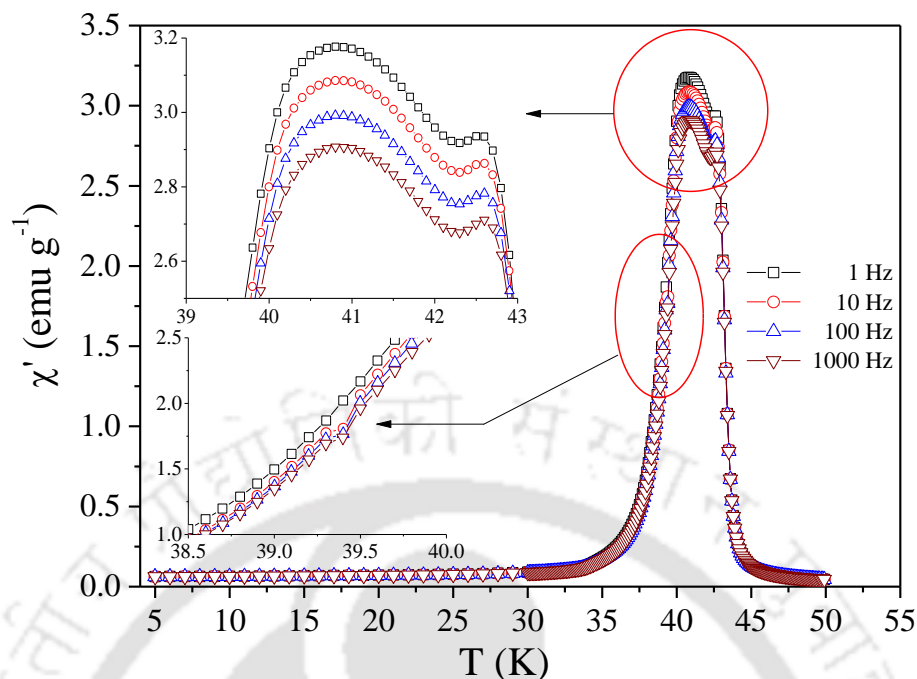
the macroscopic magnetic anisotropy. Both  $M_{ZFC}$  and  $M_{FC}$  are related to each other through the coercivity which is a measure of the anisotropy. For non-interacting magnetic particles, the blocking temperature  $T_B$  is equivalent to  $K_a V / k_B \ln(f_0 / f_m)$  where ' $K_a$ ' is the average anisotropy constant of  $K_{Mn^{2+}}$  and  $K_{Mn^{3+}}$ , ' $V$ ' is the volume of the particles,  $k_B$  is the Boltzmann constant,  $f_0$  is the attempt frequency typically equal to  $10^{11}$  Hz for antiferromagnets and  $f_m$  is the measuring frequency. For  $f_m = 1$  Hz,  $T_B$  approximately equal to  $K_a V / 25 k_B$ . Therefore,  $T_B$  is proportional to not only the anisotropy ' $K_a$ ', but, also to the volume of the particles which is equally important. Although there is some particle size dependence of ' $K_a$ ' due to contribution from surface anisotropy, it is in fact the volume ' $V$ ' of the particles that control the ' $T_B$ ' for a given system. If  $T_B = T_P \approx 39.5$  K observed in  $Mn_3O_4$  where due to blocking effect then using the relation  $T_B \approx K_a V / 25 k_B$ , one can determine the volume of the particles if an estimate of ' $K_a$ ' is known. From the coercivity  $H_c \approx 1.5$  kOe,  $K_a = M_s H_c / 2$ , one can roughly estimate the magnitude of  $K_a$  ( $= 1.66 \times 10^5$  ergs/cm<sup>3</sup> for  $M_s = 45.6$  emu/g at 90 kOe). Since ' $M_s$ ' is far from saturated state, this ' $K_a$ ' is likely underestimated. Using this magnitude and the value of  $T_B \approx 39.5$  K, we obtained the crystallite size  $D \approx 3.4$  nm for spherical particles. Since our measured crystallite size using transmission electron microscopic measurements were about 8-20  $\mu m$  in range, therefore,  $T_P$  couldn't be attributed due to the blocking effects, as, the estimated particle size in such case should be of the order  $\sim 3.4$  nm. The directional dependent magnetization studies reported on the single crystalline  $Mn_3O_4$  reveals that  $c$ -axis is the magnetically hard axis and  $[110]$  direction is the easy axis direction, even though, a negligibly small difference in the magnitude of magnetization value of

M-H curves was observed along [100] and [110] crystallographic directions [103]. The giant magneto-crystalline anisotropy fields of approximately 65 kOe has been reported recently in the  $Mn_3O_4$  system by means of nuclear magnetic resonance NMR measurements [86]. Contrary to the previous reports, Kim *et al.* reported that Yafet-Kittel structure under zero-field condition should entail one  $Mn^{2+}$  moment and two  $Mn^{3+}$  moments lie in the *ab*-plane [86]. However, in the presence of magnetic field along *c*-axis, a  $25^\circ$  tilt of  $Mn^{2+}$  ions from the *ab*-plane has been noticed. The extent of the direction of tilt is decided by the anisotropy constants ( $K_{Mn^{2+}}$  and  $K_{Mn^{3+}}$ ) and the strength of exchange interaction ( $J_{Mn^{2+}}$  and  $J_{Mn^{3+}}$ ).

Usually, the peak in the magnetic susceptibility in antiferro or ferrimagnetic system usually occurs at a few percent higher than the corresponding ordering temperature [117, 118, 134]. Hence the ordering temperature is considered at the peak of the  $\partial(\chi_{dc}T)/\partial T$  versus *T* plot rather than  $\chi_{dc}(=M/H)$  versus *T* plot. In fact, the singular behavior of a magnetically ordered system in the transition region should resemble closely to the function  $\partial(\chi_{dc}T)/\partial T$  and magnetic specific-heat  $C_p(T)$  variation of a typical antiferromagnet [117]. This inference is supported experimentally and its implication on the susceptibility curve near the transition has been studied thoroughly [118]. In order to deduce the exact transition temperature,  $\partial(\chi_{dc}T)/\partial T$  versus *T* plots were drawn using magnetization data under both ZFC and FC protocols at low magnetic fields of 50 Oe, 100 Oe and 200 Oe (figure 7.5). While the minimum occurs at  $T_N = 42.8 \pm 0.2$  K, three peaks  $T_1, T^*, T_2$  observed at 39.75 K, 38 K, and 34 K



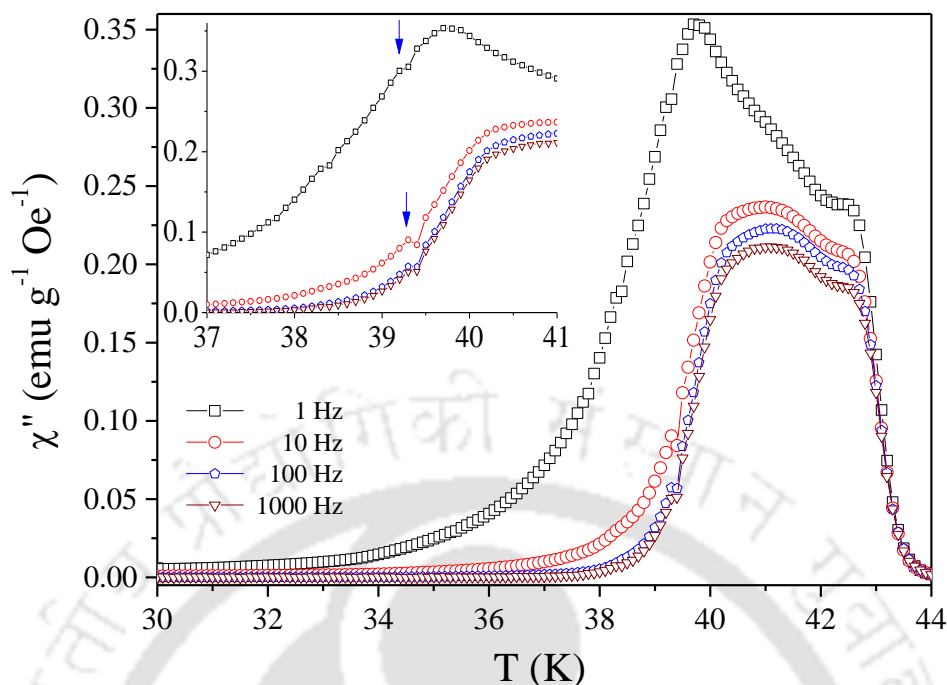
**Figure 7.5:** The temperature variation of the first derivative plots of dc-magnetic susceptibility  $\partial(\chi_{dc}T)/\partial T$  for the magnetic fields  $H = 50$  Oe, 100 Oe and 200 Oe. Inset shows the zoomed view of magnetically ordered regime which clearly depicts all the magnetic transitions.



**Figure 7.6:** Temperature dependence of real component ac-magnetic susceptibility  $\chi'(T)$  recorded at various frequencies under warming condition. The inset shows the zoomed view of the susceptibility cusps within the regime 39 K to 43 K and 38.5 K to 40 K.

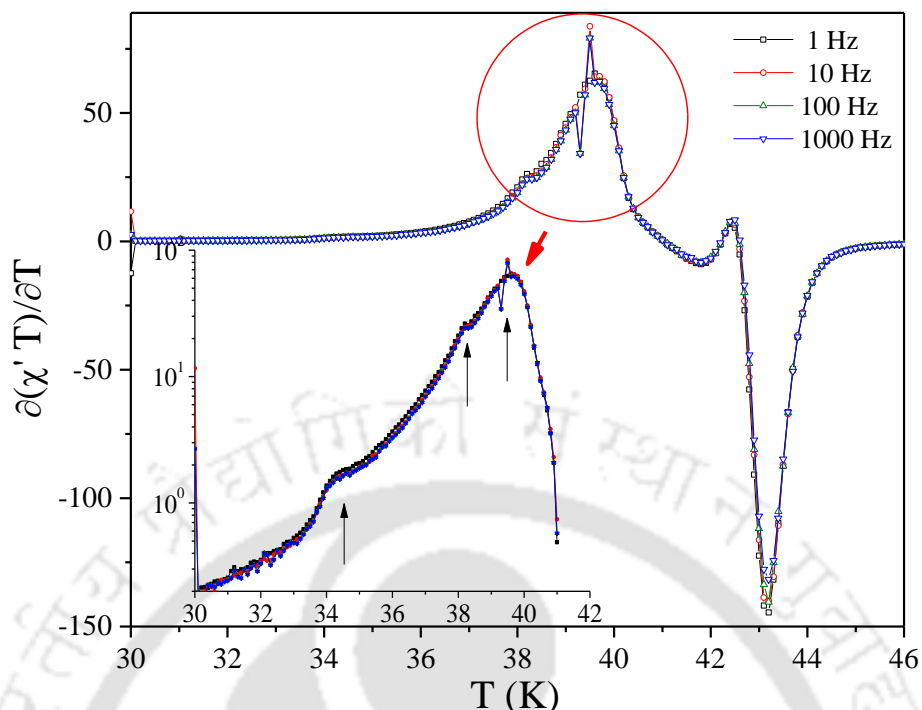
correspond to the triangular Yafet-Kittle to spiral incommensurate transition, lock-in transition, and spiral-incommensurate to cell-doubled commensurate state associated with the field dependent tetragonal to monoclinic structural transition, respectively [91]. The shift in  $T_N$  and  $T_2$  towards higher temperatures results due to saturation of the magnetic moments of a typical ferrimagnet. However, no perceptible changes are noticed in the position of transitions at  $T_1$  and  $T^*$ .

The frequency ( $f$ ) of the ac-magnetic field has significant effect on all the four transitions. Such dynamic variation of the magnetization in  $Mn_3O_4$  is studied for the first time. The in-phase  $\chi'(T)$  and out-of-phase  $\chi''(T)$  components were derived from the temperature variation of ac-susceptibility  $\chi_{ac}(T)$  data recorded at various frequencies in the range 1-10<sup>3</sup> Hz. The peak to peak amplitude  $h_{ac}$  of the ac-magnetic field has been maintained constant at 2 Oe throughout the measurement. The  $\chi'(T)$  curves exhibit two sharp peaks at 40.8 K and 42.6 K with a small kink at 39.4 K (figure 7.6). Figure 7.7 shows the temperature dependence of the imaginary part of the ac-susceptibility  $\chi''(T)$  at different frequencies. At the onset of spiral in-commensurate phase, all these curves exhibits broad maximum. Particularly, the curve  $\chi''(T)$  recorded at 1 Hz shows a sharp peak at 39.8 K, however, with increasing the frequency from 1 Hz to 10 Hz this sharp maximum quickly shifts to 41 K with significant decrease in the magnitude. No major changes were observed on further increasing the frequency from 10 Hz to 10<sup>3</sup> Hz. Such a sharp shift of the peak position of the imaginary-component of the ac-susceptibility with respect to the frequency increasing from 1 Hz to 10<sup>3</sup> Hz, across the onset of incommensurate phase (33 K < T < 39 K), may be



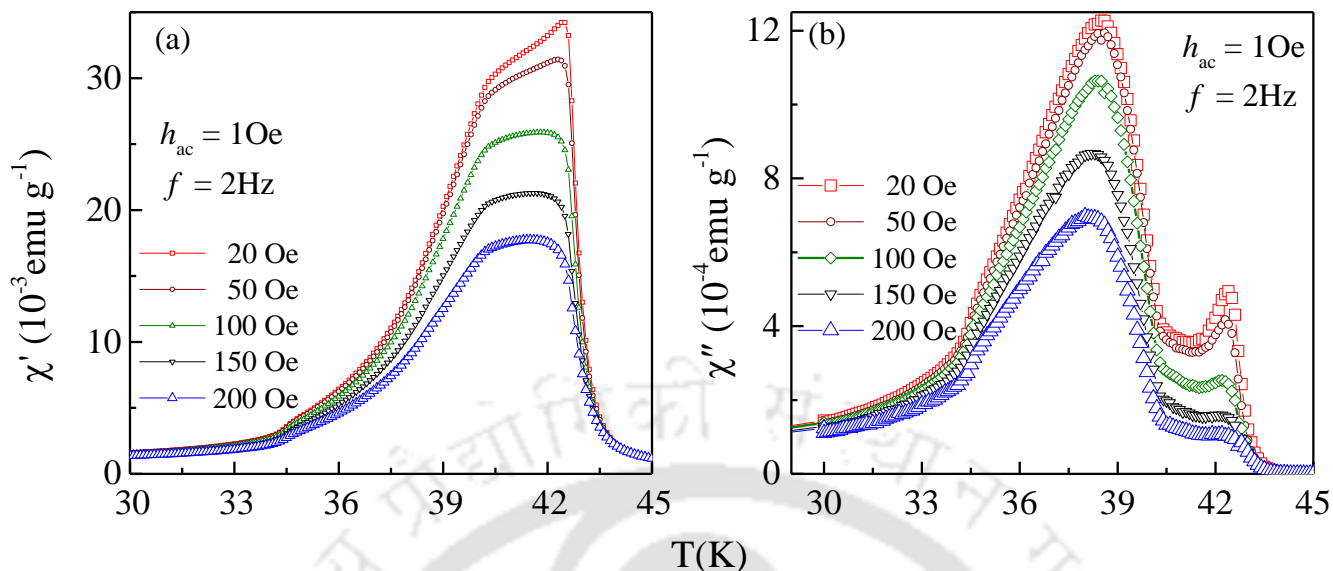
**Figure 7.7:** Temperature dependence of imaginary component ac-magnetic susceptibility  $\chi''(T)$  recorded at various frequencies under warming condition. The inset shows the zoomed view of the susceptibility cusps within the regime 37 K to 41 K.

ascribed to the disturbance of the conical spin structure of the  $Mn^{3+}$  ions. Generally, the  $Mn^{2+}$  spins, which are in the  $ab$  plane, try to orient along the applied field direction. Even though the direction of orientation of the  $Mn^{2+}$  moments ([110]) is determined by the equilibrium condition among the torques due to the competing interactions of anisotropy energy, exchange interactions, and external field. On the contrary, the cone axis (resultant or sum vector of two  $Mn^{3+}$  spins) will try to precesses along the negative applied field direction either it is ac or dc- field i.e, in between the  $[0\ 0\ 1]$  or  $[0\ 0\ -1]$  but canted from  $[-1\ -1\ 0]$  direction. While the low frequency ( $f < 1$  Hz) sinusoidal variation of the  $h_{ac}$  will still keep the  $Mn^{3+}$  conical spin undisturbed in its state intact. But once the ac-magnetic signal frequency increases from 1 Hz to 10 Hz or even higher frequencies  $Mn^{3+}$  spins cannot be able to follow the dynamic variation of  $h_{ac}$  and deviates from the precession along the negative cone axis, rather  $Mn^{3+}$  spins modulate sinusoidally but keep the coplanar structure undisturbed. This may be the reason why all the  $\chi''(T)$  curves for frequencies greater than 1 Hz almost collapse into one trace and peaks almost at the same temperature. This effect is expected to be even more prominent in the case of single crystalline sample. There is another transition occurring at the ferrimagnetic ordering temperature (42.4 K) itself. A close examination of all the  $\chi''(T)$  curves, the lock-in transition ( $T^*$ ) at 38 K can be distinguished which shifts towards higher temperature side with increasing frequency (marked by arrows in the inset of figure 7.7). Also, the minimum value of  $\chi''(T)$  and the peak in the  $\chi'(T)$  occur nearly at the same temperature and correspond to  $T_N$  extracted above using  $\partial\chi_{dc}/\partial T$  versus T curves. No significant changes were observed in the peak positions (though the heights decrease) of the

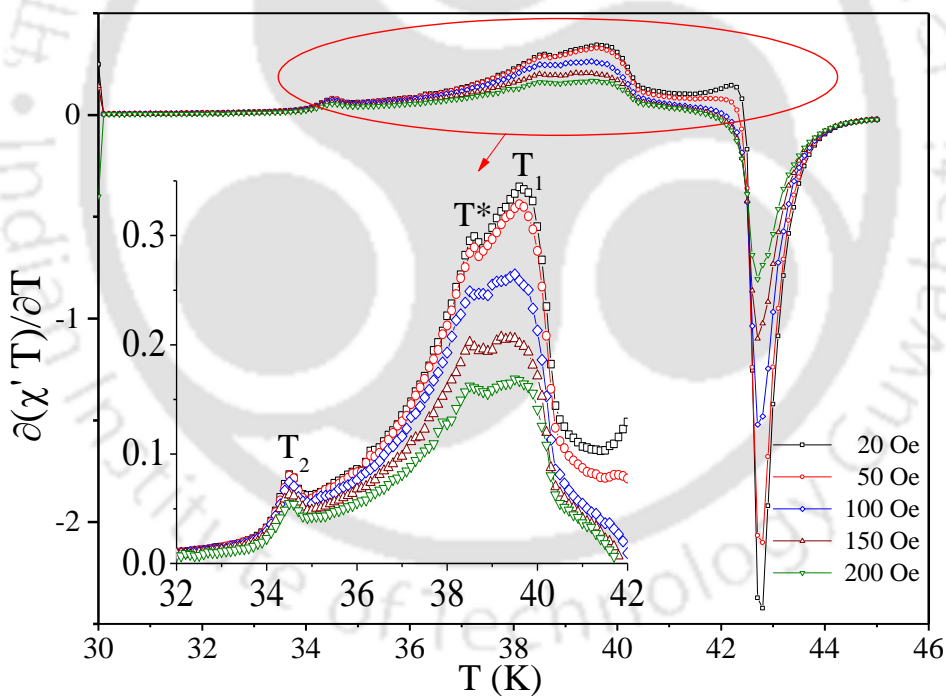


**Figure 7.8:** Derivative plots of  $\chi'(T)$  (i.e.  $\partial(\chi'(T))/\partial T$ ) plotted as a function of temperature for various frequencies. Inset represent the zoomed view of the derivative plots where all the transitions are clearly able to trace (vertical arrows indicates the magnetic transitions).

transitions  $T_1$  and  $T_N$  with increase in the ac-driving frequency. An opposite trend was noticed for  $T^*$ , whose existence can be clearly noticed only at slightly higher frequencies  $f \geq 10$  Hz in the  $\chi''(T)$  curves. Nevertheless, the existence of transition at  $T_2$  is very weak in both  $\chi''(T)$  and  $\chi'(T)$  curves. This result is consistent with the temperature dependent field induced structural data reported by Kim *et al.* [86, 91]. Such crystallographic transitions are prominent only at the moderate applied field (typically  $\sim 10$  kOe). Therefore, the applied ac-signal (magnitude and its frequency) is not sufficient here to probe the commensurate cell-doubling transition and observe intensity variation in the ac-susceptibility at  $T_2$ . The temperature variation of  $\chi''$  and  $\partial(\chi'(T))/\partial T$  resembles closely with each other and reported in various systems earlier with theoretical justification [117, 118]. In fact, identical peaks should be observed in  $\chi''$  and  $\partial(\chi'(T))/\partial T$  versus (T) curves near the magnetic-phase transition [117, 118]. In the present case, such an analysis yields all the complex magnetic phase transitions including the features not observed in the  $\chi''(T)$  data in ferrimagnetic  $Mn_3O_4$ . Figure 7.8 shows  $\partial(\chi'(T))/\partial T$  versus T plots with a sharp minimum at  $T_N$  (43.2 K) coinciding with the temperature at which  $\chi''(T)$  drops to zero. The inset depicts positive values of  $\partial(\chi'(T))/\partial T$  on a logarithmic scale. From this graph one can clearly demonstrates the transitions at 34 K, 38 K and 39.7 K associated with the field induced structural transition ( $T_2$ ), lock-in transition ( $T^*$ ), and crossover from Néel type ferrimagnetic arrangement to triangular Yafet-kittle type spin ordering, respectively. While the transition at  $T_2$  is first-order and associated with the tetragonal to monoclinic structural phase change, the other two are second-order in nature [91, 312, 313].



**Figure 7.9:** The temperature dependence of the (a) real component  $\chi'(T)$  (b) imaginary component  $\chi''(T)$  of the ac-magnetic susceptibility recorded under the superposition of different weak static bias magnetic fields for constant frequency 2 Hz and constant ac-field amplitude  $h_{ac} = 1$  Oe



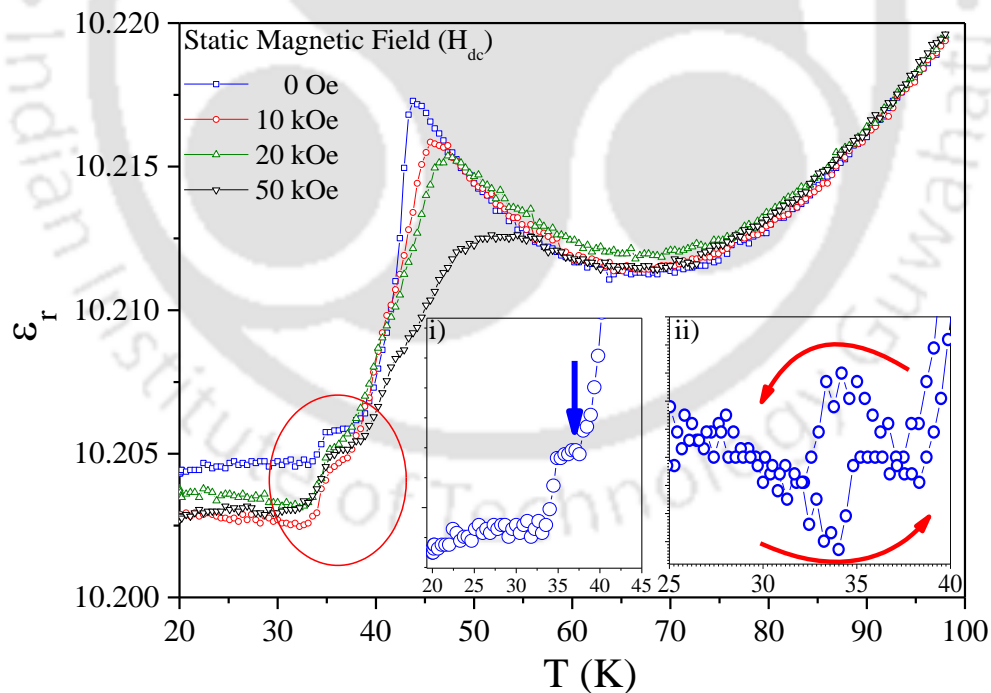
**Figure 7.10:** The temperature dependence of the  $\partial(\chi'T)/\partial T$  plots for various static magnetic fields ( $H_{dc}$ ). The inset shows zoomed view of the graph depicting the magnetic transitions at  $T_2$ ,  $T_1$  and  $T^*$ .

In order to probe the above discussed sequential transitions, we have carried out the dc-bias field dependent  $\chi_{ac}(T)$  studies. Figure 7.9(a) and (b) shows the real-part  $\chi'(T)$  and imaginary parts  $\chi''(T)$  of the ac-magnetic susceptibilities for  $f = 2$  Hz with amplitude  $h_{ac} = 2$  Oe superimposed with various dc-bias fields ( $20 \text{ Oe} \leq H_{dc} \leq$

200 Oe). This analysis is very useful to examine the effect of dc-magnetic field on all the sequence of transitions below the onset of long-range ordering. Two major peaks at 42.4 K and 40.4 K along with a small hump at 34 K are evident in the  $\chi'(T)$ . Also, the extent of splitting between 42.4 K and 40.4 K increases progressively with increasing applied dc-field ( $H_{dc}$ ). While these two peaks are well resolved in case of out-of-phase component, but, sharp decrease in intensity with almost no shift in peak position was noticed in the transition occurring at 40 K. Also, the peak at 42.4 K associated with  $T_N$  shifts towards higher temperatures with increase in  $H_{dc}$ . Nonetheless, the analysis of  $\partial(\chi'T)/\partial T$  versus T plots (figure 7.10) clearly demonstrates the existence of magnetic transitions corresponding to  $T_2, T^*, T_1,$  and  $T_N$ , but with a shift of + 0.6 K. Obviously, the temperature variation of  $\partial(\chi'T)/\partial T$  provides more insight about the complex magnetic transitions than the direct measurements of  $\chi'(T)$ .

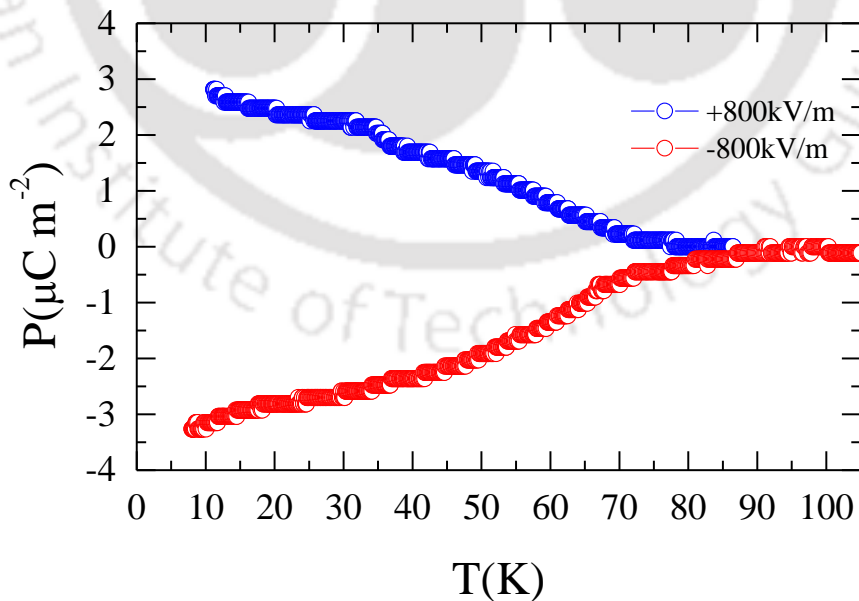
### 7.3.3 Dielectric and Magneto-dielectric Properties:

The dielectric anomalies associated with the spin-ordering transitions in  $Mn_3O_4$  both in the form of single crystal and polycrystalline samples were observed earlier [89, 90]. However, a detail investigation of all the magnetic transitions (mentioned above at  $T_2, T^*, T_1$  and  $T_N$ ) at a very small temperature interval (0.1 K) is still remains open. To address this issue, magneto-dielectric effects in  $Mn_3O_4$  are studied in detail. Figure 7.11 shows the temperature dependence of the relative of dielectric permittivity  $\epsilon_r(T)$  of polycrystalline  $Mn_3O_4$  under different



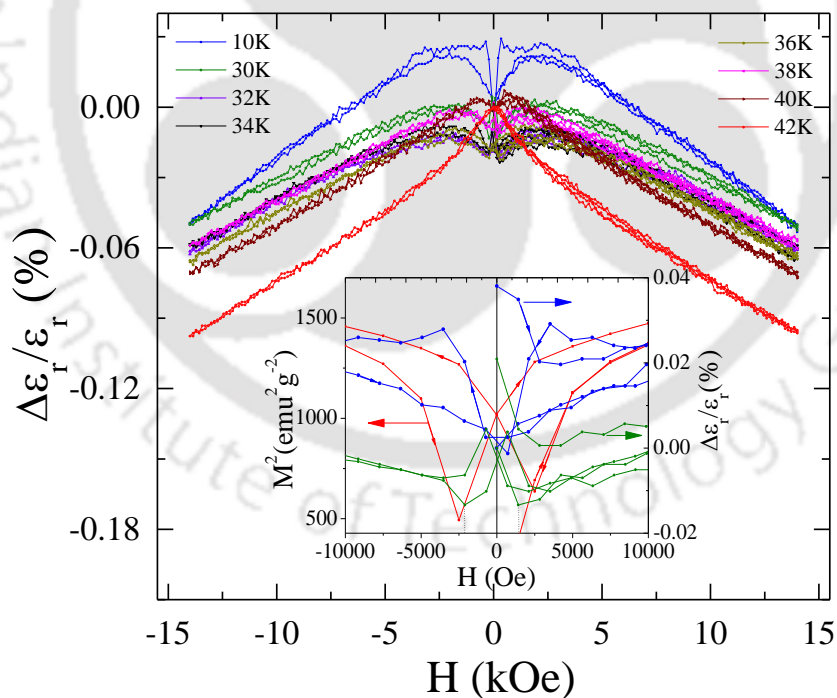
**Figure 7.11:** The temperature dependence of the relative dielectric permittivity  $\epsilon_r(T)$  measured under zero-magnetic field. The inset (i) shows the dielectric anomaly corresponding to the transition  $T^*$ . The inset (ii) shows the hysteresis lag in  $\epsilon_r(T)$  measured during cooling and heating cycles as represented by the red color arrow marks.

magnetic fields (0 - 5 T) at a constant ac-electric field having frequency 1 kHz. The data is recorded during warming after cooling the system down to 7 K. Under zero field condition, a sharp peak was observed in  $\epsilon_r(T)$  across the  $T_N$  as reported previously [89, 90]. Besides this, a step like transition occurs at 37.7 K, i.e., close to the second order lock-in transition at  $T^*$  as discussed in the above section. The inset of figure 7.11(i) clearly shows the dielectric anomaly around the lock-in transition at  $T^*$ . For further clarification, the zero field dielectric measurements were repeated under both cooling and heating cycles at different frequencies (1 kHz- 100 kHz) of the ac-electric field. A significant shift of the step like behavior is noticed with a broad hysteresis of about  $\sim 5.15$  K across  $T_2$ , confirming the first order nature of the transition (inset of figure 7.11(ii)). Such hysteresis shift is 8 time large as compared to the  $\sim 0.6$  K lag observed in heat capacity measurements recorded under cooling and heating cycles [17]. The dielectric permittivity remains almost constant up to 35 K and drops suddenly at 34 K, i.e., near the onset of first order transition at  $T_2$ . This step like feature is more clearly able to trace in  $\epsilon_r(T)$  under zero-field condition. Beyond the saddle point ( $\sim 65 - 70$  K), the dielectric permittivity increases monotonically. All the anomalies together with the sharp peak around  $T_N$  shifts towards the high temperature as the magnetic field strength increases to very high values  $H \rightarrow 14$  kOe. Although the change in relative dielectric permittivity values is very small at all the temperatures but all the anomalies can be resolved clearly and these results are highly reproducible. The magnitude and trend of the  $\epsilon_r(T)$  obtained in the polycrystalline samples are nearly equal to the values obtained with the out-of-plane ( $E \parallel [100]$ ) dielectric constant versus temperature of single crystalline  $Mn_3O_4$  [90]. Since the global dielectric response is closely resembles with the data recorded with the ac-electric-field applied under out-of-plane configuration, one can expect that majority of the crystals aligned along [100] direction even though the current sample is in the polycrystalline form.



**Figure 7.12:** The positive and negative branches of the Polarization (P) versus temperature (T) curves measured in the temperature range 7 K - 100 K after poling with the static-electric field of strength  $\pm 800$  kV/m.

In order to see the presence of electric polarization in magnetically order state we have measured the remnant polarization ‘ $\mathbf{P}$ ’ as a function of temperature. Figure 7.12 shows the  $\mathbf{P}$  versus  $T$  measurements after poling the sample by means of a static poling-electric field as mentioned in the experimental section. This is the first report dealing with the temperature dependence of the polarization measurements in  $Mn_3O_4$  polycrystals. The remnant polarization value decreases continuously with raising the temperature and becomes zero above 70 K. This shows a clear paraelectric to ferroelectric transition. Very small values of remnant polarization was noticed ( $P_r \sim 3 \times 10^{-6}$  C/m<sup>2</sup> at 10 K) in  $Mn_3O_4$  system even though a giant atomic displacement (0.25 Å) was observed below  $T_N$  [311]. Small values of remnant polarization could be due to the possible formation of opposite polarization clusters in a different direction than the adjacent domains, and in a polycrystalline sample the resultant polarization will be the average of polarization from different directions. Nonetheless, the observed resultant polarization is very small and the anomalies as observed in dielectric results are very difficult to trace in the electric polarization measurements. Figure 7.13 shows the five cycle hysteresis mode of  $\Delta\epsilon_r/\epsilon_r(\%)$  versus  $H$  recorded at various temperatures below  $T_N$ . All the magnetic transitions occurring between the Yafet-Kittel and the incommensurate phase display significant variation in the magnetic field dependence ( $-14 \text{ kOe} \leq H \leq 14 \text{ kOe}$ ) of the relative change of permittivity  $\Delta\epsilon_r/\epsilon_r(\%)$ . For low magnetic fields ( $H < \pm 5 \text{ kOe}$ ), the magnitude of  $\Delta\epsilon_r/\epsilon_r(\%)$  ( $\sim 3 \times 10^{-3}$ ) are in close agreement with the relative shift of the permittivity measured in  $Mn_3O_4$  single crystals



**Figure 7.13:** The relative dielectric permittivity  $\Delta\epsilon_r/\epsilon_r(\%)$  scanned as a function of static magnetic field  $H_{dc}$  under decreasing and increasing cycles ( $\pm 15 \text{ kOe}$ ) of magnetic field at various temperatures. Here  $\Delta\epsilon_r/\epsilon_r = ([\epsilon_r(H=0) - \epsilon_r(H)]/\epsilon_r(H=0))$ . The inset shows the square of the magnetization value  $M^2$  in red colored data points plotted on the left hand side scale as a function of magnetic field and a zoomed view of the low field hysteresis response of  $\Delta\epsilon_r/\epsilon_r(\%)$  versus magnetic field  $H_{dc}$ .

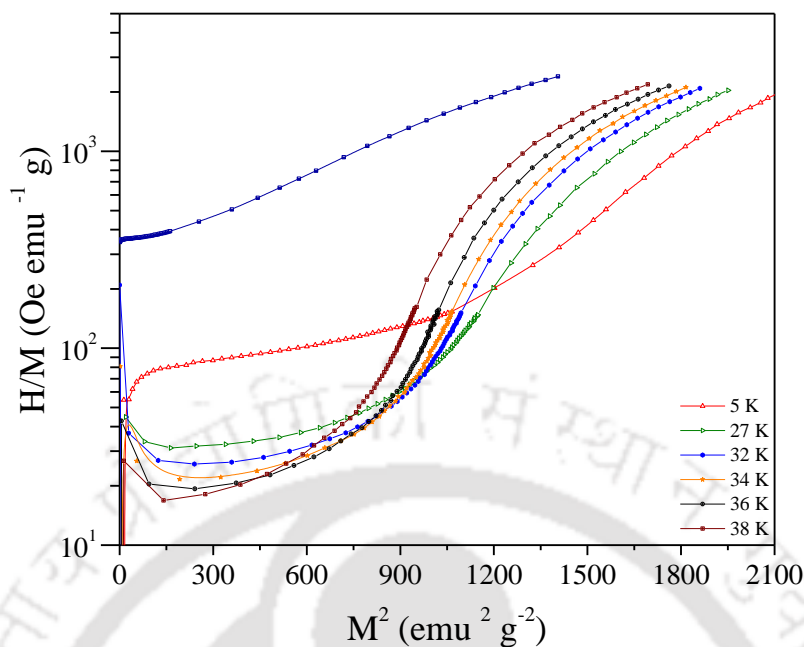
under out-of-plane configuration, that is both H, E are parallel to crystallographic direction [001]. The hysteresis is significant at very low temperatures ( $< 10$  K) where  $\Delta\epsilon_r/\epsilon_r(\%)$  reaches a maximum value at  $H \sim 5.2$  kOe and decreases thereafter. However, as the temperature approaches to the commensurate planar temperature regime, hysteresis decreases gradually and  $\Delta\epsilon_r/\epsilon_r$  varies linearly with the ramping field. This effect becomes more significant in the paramagnetic regime for  $T > T_N$  (inset of figure 7.13). Except for the case of  $T = 10$  K, all  $\Delta\epsilon_r/\epsilon_r$  versus H plots exhibit negative values but with a positive curvature up to a critical field of  $H_T \sim 5.2$  kOe and changes to negative curvature thereafter (as shown by the dotted lines in the inset of figure 7.13). Inset of figure 7.13 shows the comparative behavior of the relative shift obtained in dielectric permittivity at  $T = 10$  and 30 K and the square of the magnetization ( $M^2$ ) at  $T = 30$  K (plotted on the left-hand-side scale) for five hysteresis cycles protocol shown by the arrows. It is expected that the relative dielectric permittivity at moderate electric field frequencies ( $\sim 1$  kHz) is dominated by the optical phonons [90]. The force constant between the ions  $Mn^{2+}-O^{2-}$  significantly influenced by the external magnetic field direction which will cause variation of the phonon frequency and finally leading to the magnetic field dependence of capacitance [90]. Thus, the magneto-capacitance is driven by the effective change of the optical-phonon frequency controlled by the externally applied magnetic field direction.

For temperatures below  $T_N$  and magnetic fields below  $H_T$ , one-to-one correspondence is observed between the  $M^2$  versus H and  $\Delta\epsilon_r/\epsilon_r$  versus H in  $Mn_3O_4$ . The dotted line shows identical minimum in both curves in the final cycle, where, all the magnetic domains reach the same state at the coercive field. Such a relationship of low temperature hysteresis behavior between the dielectric permittivity and magnetization is prominent in magnetically ordered regime only. For all the temperatures the magnetodielectric curves  $\Delta\epsilon_r/\epsilon_r(H)$  are symmetric about the  $H=0$  axis contrary to the asymmetric magnetodielectric behavior observed in Ref [89]. Except this difference all the present observations are in-line with those of Tackett *et al.* and Suzuki *et al.* who explained the origin of magneto-dielectric effects using the spin-phonon coupling [89, 316].

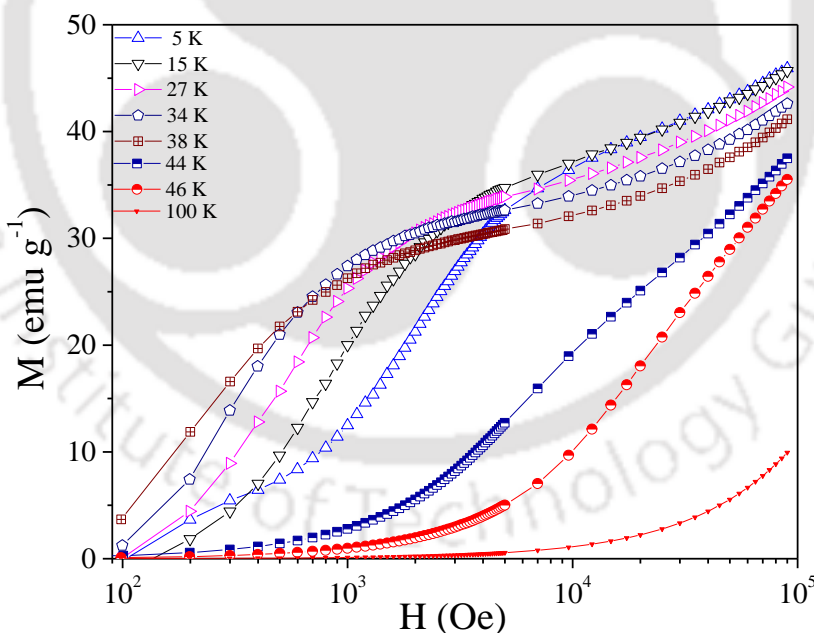
### **7.3.4 Isothermal Magnetization:**

In this section we explored the correlation between the isothermal magnetic field dependent magnetization and dielectric behavior. Figure 7.14 shows the ratio of magnetic field (H) to the value of magnetization (M) versus square of the magnetization ( $H/M$  versus  $M^2$ ) curves (i.e., Arrott plots) extracted from the isothermal magnetization ( $M-H_{1st\text{-quadrant}}$ ) curves recorded at various temperatures in the range 5-40 K (figure 7.15). In both figures 7.14 and 7.15 we have shown only few curves at characteristic temperatures in order to avoid the overcrowding. The temperature was brought to 300 K each time to ensure that the measurement should begin from a virgin magnetic state (without any magneto-thermal history) followed by a zero-field cooling.

Also, the temperature difference ( $\Delta T$ ) between the two successive isotherms was set low in the region of the transitions (i.e., 27 - 46 K) whereas  $\Delta T$  was maintained high at other transitions (5 - 25 K and 48 - 65 K). The

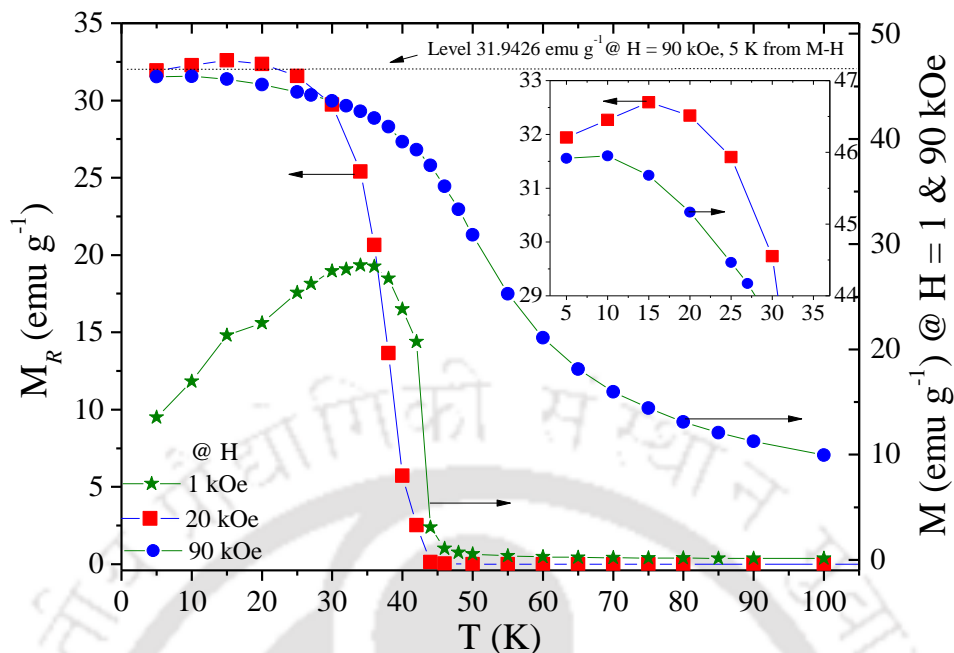


**Figure 7.14:** The ratio of magnetic field ‘H’ and its corresponding magnetization ‘M’ values ( $H/M$ ) plotted as a function of the square of magnetization ( $M^2$ ) for different temperature  $T < T_N$  (Arrott plots). Note: Only selected M-H curves and  $H/M$ - $M^2$  plots are shown at characteristic temperature intervals.



**Figure 7.15:** The magnetization versus field ( $M$ - $H$ ) isotherms recorded at various temperatures  $T < T_N$ . Note: Only selected  $M$ - $H$  curves are shown at characteristic temperature intervals.

magnetization data was recorded by increasing the magnetic field from zero to 90 kOe. The deviation from positive slopes can be clearly noticed in the Arrott plots within the magnetically ordered regime. The isotherms recorded between 10 and 38 K show decreased negative slope in the  $H/M$  versus  $M^2$  plots confirming the magnetic field



**Figure 7.16:** Temperature dependence of remanence magnetization  $M_r(T)$  shown on the left-hand-side scale and the right-hand-side scale depicts the magnetization values recorded at  $H=1$  kOe and 90 kOe during the hysteresis loop measurements at various temperatures. The inset shows zoomed view of the low-temperature regime of  $M_r(T)$  depicting the down turn of the  $M_r$  values below 15 K.

induced first-order discontinuous transition across  $T_2$  in the polycrystalline  $Mn_3O_4$  [168, 169, 317, 318]. This observation is further confirmed by the existence of weak meta-magnetic-like character of the isotherms represented in the logarithmic scale as shown in figure 7.14 [317, 318]. Since the Arrott plots in other temperature regimes exhibit no negative slope, indicating that the transitions are of second-order continuous nature [168, 169]. This type of transition occurring at  $T_N$  is supported by ac-susceptibility  $\chi_{ac}(H, T)$  versus  $T$  plots at various fixed dc-magnetic fields under warming condition [167, 318 - 320]. It has been demonstrated in the literature that Arrott plot criterion can be capable of establishing the order of both sequential transitions as well as isolated phase transitions [167]. The applicability of Arrott criterion for both first- and second-order transitions possibly replicates the fact that magnetization at low fields drops across the temperatures below the structurally coupled transition (i.e. incommensurate-to-commensurate transition at  $T_2$ ). Such transitions are well described on the basis of ‘interaction component mechanism’ [312]. According to this mechanism the incommensurate-to-commensurate transition must be first-order in nature. Such predictions were experimentally proved in the case of  $CoCr_2O_4$ ,  $Ni_3V_2O_8$ , and  $CuO$  [312].

Figure 7.16 shows the temperature dependence of remanence magnetization  $M_r(T)$  obtained from the M-H isotherms for a ramping field of 1 kOe and 90 kOe. The value of  $M_r(T)$  drops abruptly across the  $T_N$  as expected. It assumes a maximum value of 32.6  $emu\ g^{-1}$  and decreases below 15 K to 31  $emu\ g^{-1}$  at 5 K as shown in the inset figure 7.16. Such a low value of remanence magnetization is connected with the low temperature first order meta-

magnetic behavior of the Mn<sub>3</sub>O<sub>4</sub> system. As the magnetic field increases beyond 1 kOe the significant diffusiveness in the M<sub>r</sub>(T) behavior is noticed owing to the saturation effects. The nature of magnetic transitions in Mn<sub>3</sub>O<sub>4</sub> described above are consistent with the heat capacity measurements reported earlier [312, 313]. Across 90 kOe, M<sub>r</sub>(T) shows a tail above T<sub>N</sub> which persist up to 70 K and matches with the onset of polarization (Figure 7.12). Such consistency between the temperature variation of polarization and remanence magnetization indicates that the existence of weak magnetic ordering even above 42 K; this inference is further supported by the ε<sub>r</sub>(T) which gradual increasing for T > 42 K.

### **7.3.5 Summary:**

The complex magnetic ordering in polycrystalline Mn<sub>3</sub>O<sub>4</sub> was investigated by means of ac-magnetic susceptibility  $\chi_{ac}(f_{ac-Mag}, H_{dc}, T)$  and relative dielectric permittivity  $\epsilon_r(f_{ac-Elec}, H_{dc}, T)$ . All the transitions occurring below the ferrimagnetic Néel temperature including the fine lock-in transition at 38 K was successfully probed by means of  $\chi_{ac}(f_{ac-Mag}, T)$  superimposed with a small static-bias magnetic field in the range 20 - 200 Oe. Mn<sub>3</sub>O<sub>4</sub> exhibits isokaps in the field dependent ac susceptibility curves  $\chi_{ac}(H_{dc}, T)$ , which displays a succession of peaks corresponding to each transition except T<sub>2</sub> that decrease in amplitude with increase in temperature as the magnitude of the static magnetic-field increases. Such humps are unequivocal signature of a continuous second-order transition. While the M-H isotherms near to T<sub>2</sub> display the S-shaped feature associated with meta-magnetic like first-order transition. The zero-field temperature dependence of the dielectric permittivity curves exhibits a large hysteresis of about ~ 5.15 K in consonance with the first order nature of spiral incommensurate to commensurate planar transition occurs at 34 K. The magnetic and dielectric properties show clear evidence of magneto-electric coupling in Mn<sub>3</sub>O<sub>4</sub> and finite electric polarization in magnetically order state.

## Conclusions and Scope for Future Research

### 8.1 Conclusions:

A summary of important findings of the present thesis is presented in this concluding chapter. This thesis is mainly focused on the similarities and differences of the magnetic structure of three different inverse spinel oxides. The structural, magnetic, dielectric, specific-heat, and other physical properties of: (i) Cobalt-Orthostannate ( $\text{Co}_2\text{SnO}_4$ ) (ii) Cobalt-Orthotitanate ( $\text{Co}_2\text{TiO}_4$ ) (iii) Hausmannite ( $\text{Mn}_3\text{O}_4$ ), and (iv) the two phase composites comprising of  $\text{Co}_3\text{O}_4 - \text{Co}_2\text{TiO}_4$  are recapitulated here. Magnetic measurements in these polycrystalline samples have shown several interesting features including semi-spin-glass behavior, bipolar exchange bias, and spin-liquid type structure at low-temperatures. Following a brief summary of the key results, we concluded this chapter by identifying a few possible frontiers of future research work related to the tailoring of the exchange interactions.

The nature of magnetic ordering and electronic structure of  $\text{Co}_2\text{SnO}_4 = [\text{Co}^{2+}][\text{Co}^{2+}\text{Sn}^{4+}]\text{O}_4$  was investigated by measuring the temperature dependence of its dc, ac-susceptibilities and X-ray photo electron spectroscopy, respectively. We have shown that the ferrimagnetic (FiM) ordering was originated from different magnetic moments of  $\text{Co}^{2+}$  on A sites ( $3.87 \mu_B$ ) and B-sites ( $4.91 \mu_B$ ) with the antiferromagnetic molecular constants  $N_{AA} = 21.56$ ,  $N_{AB} = 33.02$  and  $N_{BB} = 10.68$ . The analysis of the frequency dependence ac-magnetic susceptibility data using Vogel-Fulcher Law and the Power-Law of the critical slowing down suggests the existence of spin-glass (SG) phase  $T_{SG} \sim 39$  K. The FiM is associated with the longitudinal spin component, whereas, the SG is arising due to the freezing of the transverse spin component. These observations confirm the prediction of Villain [40] in magnetic insulators with non-magnetic substituents such as Sn, Ti, and Al. Random distribution of the  $\text{Sn}^{4+}$  ions on the B-sites are the main source of weakening of the A-B exchange coupling, thereby producing random canting of the  $\text{Co}^{2+}$  moments below FiM ordering. Application of magnetic field reduces the random canting, thereby shifting  $T_{SG}$  to lower temperatures and dwindles the SG phase.

Next we have studied the role of 'Ti' dilution at the octahedral sites of  $\text{Co}_2\text{TiO}_4$  by analyzing the temperature and magnetic field dependence of its magnetization, specific heat ( $C_P$ ), ac susceptibilities  $\chi'$  and  $\chi''$  measured at different frequencies, and the hysteresis loop parameters. X-ray diffraction of the sample synthesized by the solid-state reaction route confirmed the cubic spinel structure without any secondary phases. However, we observed trivalent nature of 'Ti' instead of tetravalent state from the X-ray photo electron spectroscopy; unveiling the electronic structure of  $\text{Co}_2\text{TiO}_4$  equivalent to  $[\text{Co}^{2+}][\text{Co}^{3+}\text{Ti}^{3+}]\text{O}_4$ . Analysis of the dc magnetic susceptibilities combined with the weak anomalies in the  $C_P$  versus T data shown the existence of quasi-long range ferrimagnetic state below 47.8 K and a compensation effect across 32 K. From the analysis of Néel fitting of the inverse-paramagnetic susceptibility we obtained the magnetic moments  $\mu(A) = 3.87 \mu_B$  and  $\mu(B) = 5.19 \mu_B$  on the A and B sites in  $\text{Co}_2\text{TiO}_4$ . These magnitudes are different from  $\text{Co}_2\text{SnO}_4$  which are resulting from the different electronic

structure. Additional noteworthy features in  $\text{Co}_2\text{TiO}_4$  are (a) lack of perfect spin-glass phase transition below 48 K, (b) negative slopes of Arrott plots below 32 K, (b) zero-crossover of isothermal magnetic-entropy-changes ( $\Delta S$ ) signifying the presence of pseudo first order discontinuous magnetic phase transition in the low temperature regime ( $5 \text{ K} \leq T \leq 32 \text{ K}$ ), (c) large coercivity  $H_C \sim 20 \text{ kOe}$  and sign-reversal exchange bias  $H_{EB} (= -20 \text{ kOe}$  for  $T < 15 \text{ K}$ ).

We have studied the effect of ‘Sn’ doping (at octahedral ‘Ti’ sites) on the global magnetic properties of  $\text{Co}_2\text{TiO}_4$  polycrystalline system. We found the co-existence of longitudinal FiM behavior with Néel temperature  $T_N = 46.1 \text{ K}$  and re-entrant transverse spin-glass state at 44.05 K in  $\text{Co}_2\text{Ti}_{0.6}\text{Sn}_{0.4}\text{O}_4$  system. The magnetic compensation temperature  $T_{\text{COMP}}$  shifts from 31.74 K to 27.1 K when 40 at% ‘Sn’ substitutes ‘Ti’ at B-sites. For  $T > T_N$ ,  $\chi_{\text{dc}} (= M/H_{\text{dc}})$  fits well with the Néel’s expression for the two-sublattice model with antiferromagnetic molecular field constants  $N_{\text{BB}} \sim 15.44$ ,  $N_{\text{AB}} \sim 32.01$ , and  $N_{\text{AA}} \sim 20.88$ . The frequency dependence of ac-magnetic susceptibility ( $\chi_{\text{ac}}$ ) data follows the Vogel-Fulcher law and the power-law of critical slowing-down with ‘ $z\nu$ ’ = 6.01 suggests the existence of spin-clusters. This system exhibits unusual hysteresis loops with large  $H_{EB} \sim 13.6 \text{ kOe}$  (at 7 K) after zero-field cooling process from an un-magnetized state, and a dramatic collapse of remanence ( $M_R$ ) and coercive field ( $H_C$ ) across  $T_{\text{COMP}}$ . Such anomalous  $H_{EB}$  under zero-field cooled condition originates from the ferrimagnetic/spin-glass interface. We have also studied the temperature dependence of micro-Raman spectroscopy of  $(1-x) \text{Co}_3\text{O}_4 + x \text{Co}_2\text{TiO}_4$  ( $0 \leq x \leq 1$ ) two-phase composites. Five Raman active modes are observed at 689, 618, 518, 480, and 195  $\text{cm}^{-1}$  for all the lower and intermediate compositions, these modes are associated with  $A_{1g}$ ,  $E_g$  and  $3F_{2g}$  phonon symmetries. Conversely, pure  $\text{Co}_2\text{TiO}_4$  exhibits a broad spectrum of width  $\sim 93.3 \text{ cm}^{-1}$  without any signatures of the  $F_{2g}(3)$  mode. At 25 K the  $A_{1g}$  and  $F_{2g}$  modes shift towards high frequency side with anomalies across the FiM and antiferromagnetic ordering temperatures of  $\text{Co}_2\text{TiO}_4$  and  $\text{Co}_3\text{O}_4$ . All the compositions exhibit two distinct bands at 576  $\text{cm}^{-1}$  ( $B_1$ ) and 665  $\text{cm}^{-1}$  ( $B_2$ ) in the Fourier transform infrared spectra recorded at 310 K which are associated with the vibrational stretching of the metal-oxygen bonds of length  $\sim 195.8 \text{ pm}$  (B-O) and  $\sim 185.4 \text{ pm}$  (A-O) respectively. The intensity of these sharp bands gradually smeared-off as the crystal structure transforms from normal-spinel ( $a = 8.07 \text{ \AA}$ ) to inverse-spinel structure ( $a = 8.45 \text{ \AA}$ ). The  $\chi_{\text{dc}}(T)$  data of these composites shows increase of  $T_N$  from 47.4 K to 53.5 K, and  $T_{\text{COMP}}$  from 31.74 K to 37.72 K with increasing  $x$  from 1 to 0.23. We also observed lack of spin-glass transition in these two-phase composites. For  $T < T_N$  we observed large magnitude of  $H_C$  ( $\sim 19 \text{ kOe}$  for  $x = 0.23$  at  $T = 10 \text{ K}$ ) and  $H_{EB}$  ( $\sim 887 \text{ Oe}$  for  $x = 1$  at  $T = 10 \text{ K}$ ) which were tailored with respect to the composition ‘ $x$ ’. The temperature and frequency dependence of ac-conductivity  $\sigma(T, \omega)$  studies confirms the possibility of Arrhenius like behaviour in  $\sigma(T)$  and Jonscher’s power law ( $\sigma_{\text{ac}} \sim A\omega^s$ ) behaviour which signifies the fact that the motion of charge carriers from site to site with quantum mechanical tunneling between asymmetric double-well potential dominated at  $T > 300\text{K}$ . These studies yield activation energy ( $E_A$ ) in the range 2-1800 meV. The Cole-Cole analysis revealed the dominance of grain-

boundary effects for dilute compositions whereas conductivity within grains play a major role in heavily substituted  $\text{Co}_2\text{TiO}_4$ .

In chapter 7, we have studied the magnetic, dielectric and magneto-dielectric properties of tetragonally distorted normal spinel  $\text{Mn}_3\text{O}_4$ . Various complex magnetic transitions occur below the ferrimagnetic ordering of  $\text{Mn}_3\text{O}_4$  are successfully probed by the ac-magnetization dynamics ( $\chi_{ac}(T)$ ), relative dielectric permittivity  $\epsilon_r(T)$  and magneto-dielectric ( $\Delta\epsilon_r/\epsilon_r(H)$ ) measurements. Besides the known sequence of transitions ( $T_N$  at 42.75 K and field-induced structural transition at 32 K), a new lock-in transition at 38 K ( $T^*$ ) has been successfully probed by both  $\chi_{ac}(T)$  and  $\epsilon_r(T)$ . We also observed a clear hysteresis of about 5.15 K in the zero-field  $\epsilon_r(T)$  across 34 K which provides evidence to the first-order nature of this transition. Our  $\Delta\epsilon_r/\epsilon_r(H)$  results demonstrates the evidence of magneto-electric coupling in  $\text{Mn}_3\text{O}_4$  system. The temperature dependence of electric polarization takes maximum value ( $P \sim 3 \times 10^{-6} \text{ C/m}^2$ ) below the spiral-incommensurate to commensurate planar transition at 33 K.

### 8.2 Future Scope:

In the current thesis we explored only structural, magnetic and electrical properties of spinel oxides  $\text{Co}_2\text{SnO}_4$ ,  $\text{Co}_2\text{TiO}_4$  and  $\text{Mn}_3\text{O}_4$ . Below we enumerate some possible extensions of the current work.

- One can study the temperature dependence of Neutron diffraction below the ferrimagnetic ordering temperatures which can provide additional information about the magnetic structure. Such studies also verify the conclusions drawn from the magnetic measurements.
- To perform the electronic band-structure calculations using density function theory and make a comparative study with the experimental results obtained from the optical measurements (in UV-Vis-NIR regime) by means of diffusive reflectance spectroscopy.
- To synthesize the low-dimensional nanostructures of  $\text{Co}_2\text{SnO}_4$ ,  $\text{Co}_2\text{TiO}_4$  and  $\text{Mn}_3\text{O}_4$  and make a systematic comparative study of their structural, optical and magnetic properties with their bulk counterpart. Such nanostructures play a major role in the fuel-cells, Li-ion batteries and catalysts.
- This study can be extended with various other doping elements either non-magnetic or magnetic (e.g. Al, Mn, Ru, V, and Cr at 'Ti' and 'Sn' sites) and probe the differences occurring in the structural, optical and magnetic properties as compared the pristine compounds.

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